

# Machine learning opportunities to reduce the dimension of uncertain complex geophysical media

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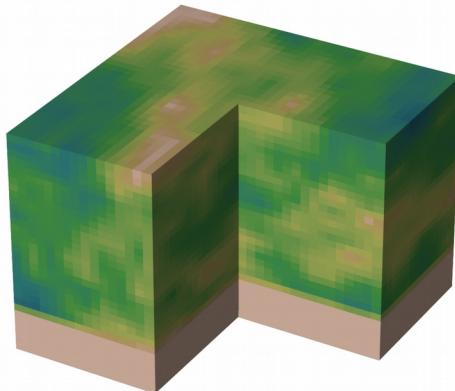
<sup>2</sup> Université Paris-Saclay, ENS Paris-Saclay, CentraleSupélec, CNRS, LMPS - Laboratoire de Mécanique Paris-Saclay, 91190 Gif-sur-Yvette, France



CentraleSupélec

école  
normale  
supérieure  
paris-saclay

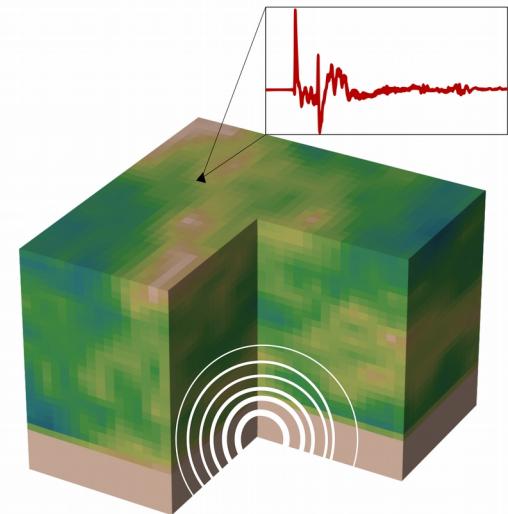
complex 3D  
geophysical medium  
with uncertainties



numerical simulation



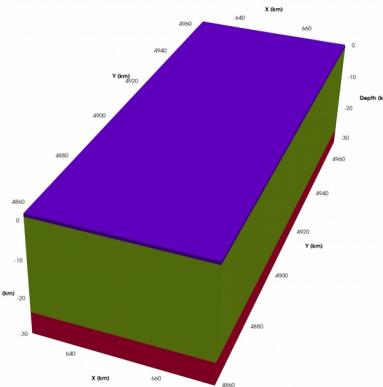
physical output



*Example: seismic wave propagation.*

Goal: Reduce the dimensionality of the media to characterize the relationship between the medium and the problem's output.

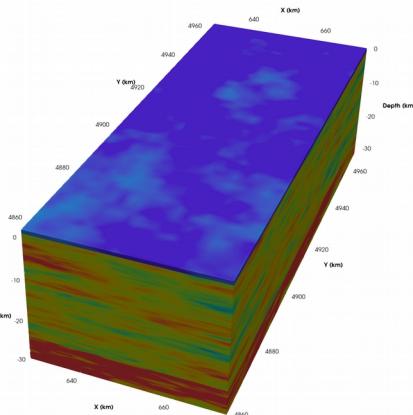
Simplest description of a geophysical medium



Uncertainties model

Random fields  
Correlation lengths on x, y and z  
Coefficient of variation

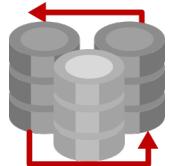
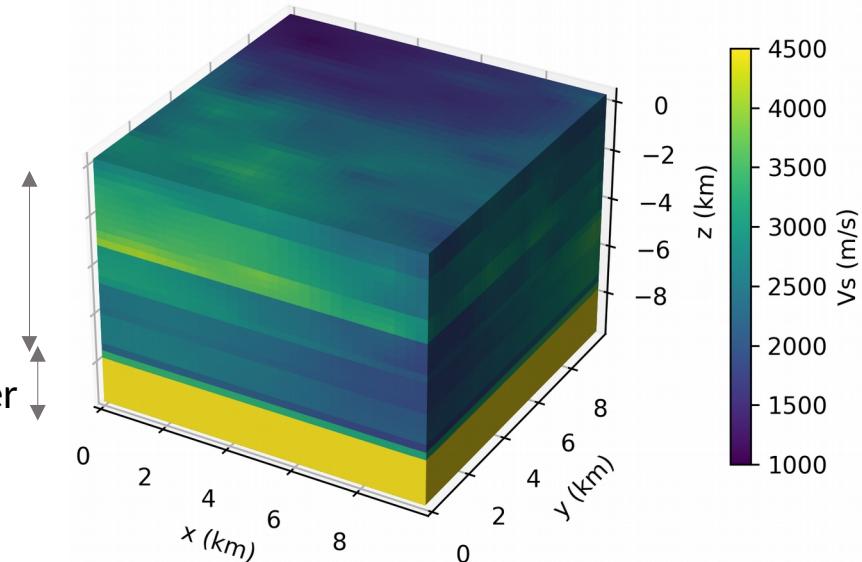
Heterogeneous model



We built a database of 100,000 heterogeneous geophysical media.

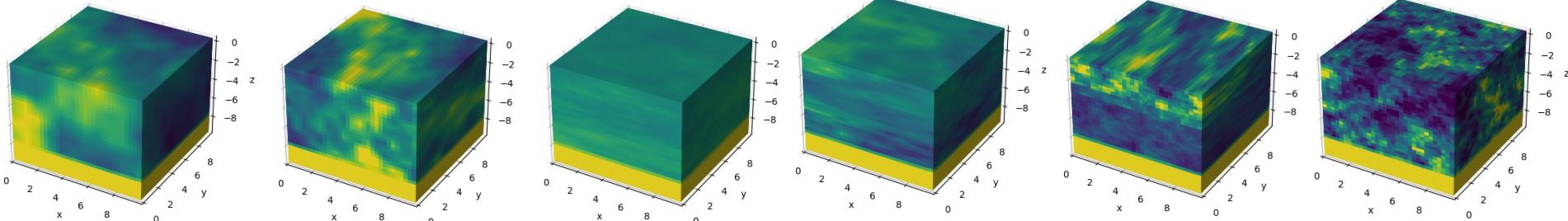
Several layers with varying thickness  
+ random fields with different parameters

constant velocity layer



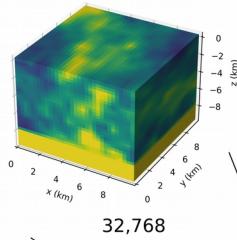
Publicly available! (14Go)

[10.5281/zenodo.6983054](https://zenodo.10.5281/zenodo.6983054)

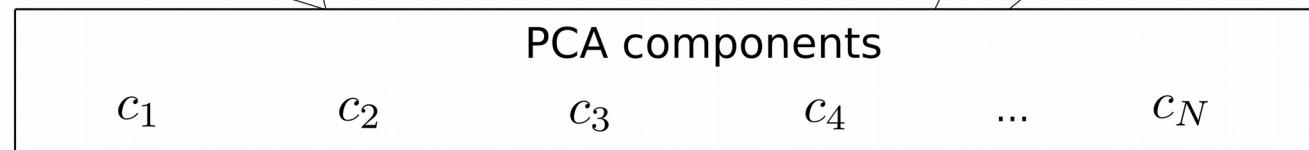


# Method 1 – Principal Component Analysis (PCA)

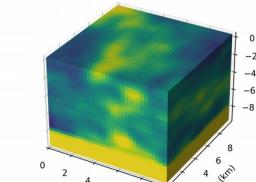
Input



PCA

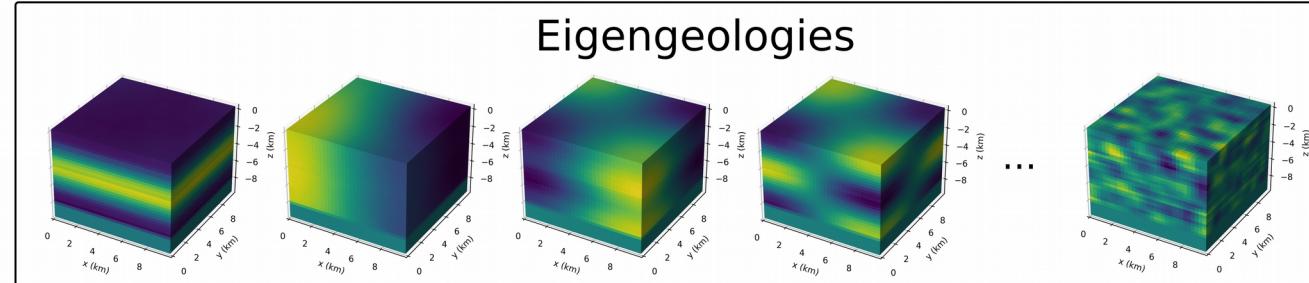


Reconstruction



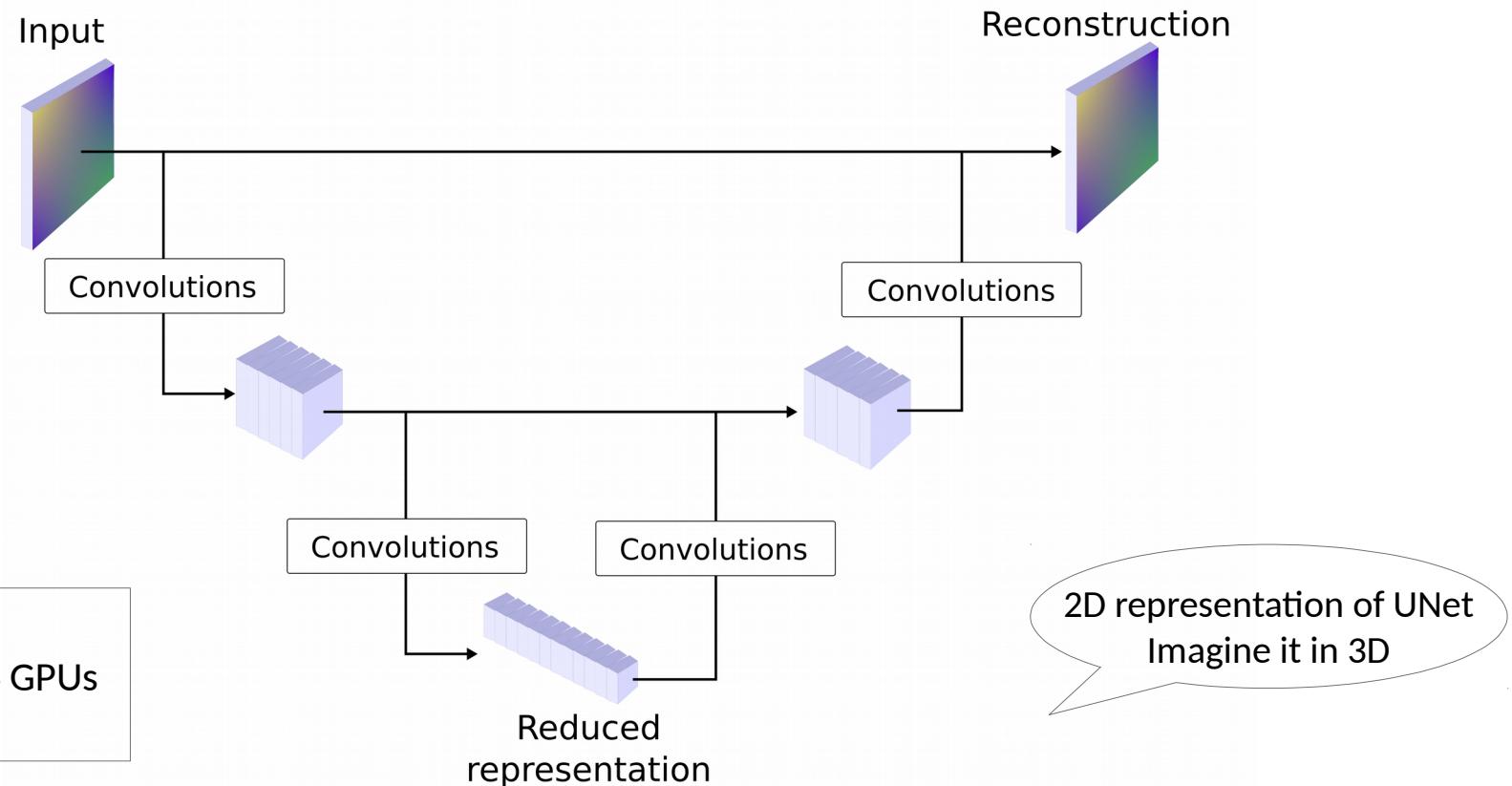
$\Sigma$

Eigengeologies

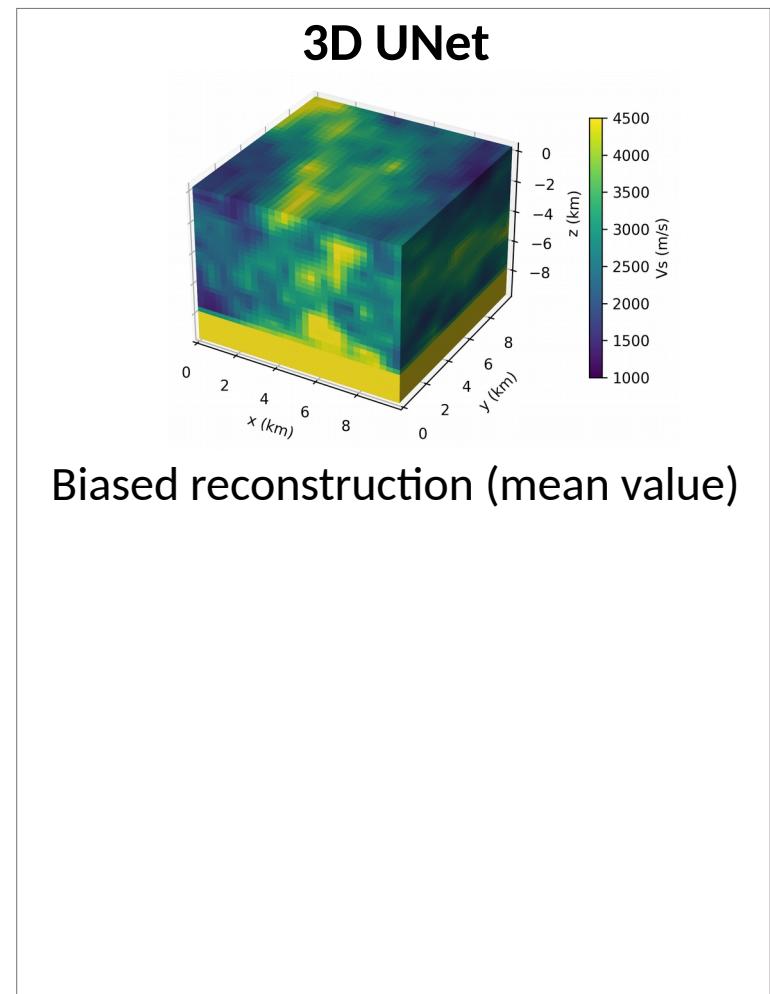
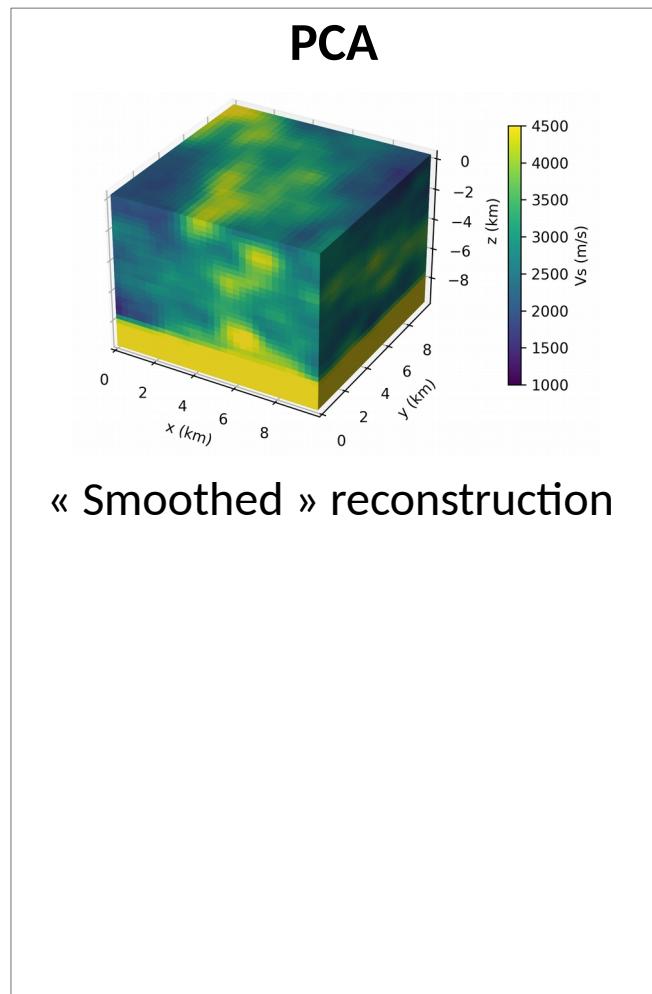
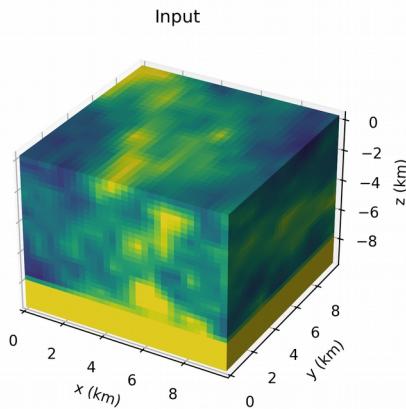


Auto-encoder ~ non-linear extension of the PCA

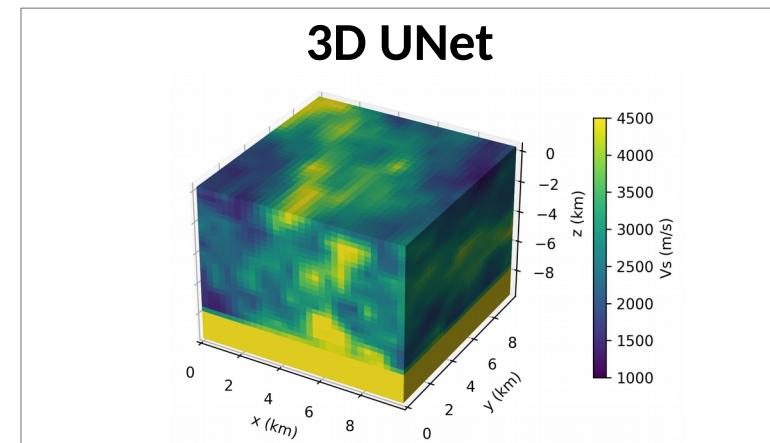
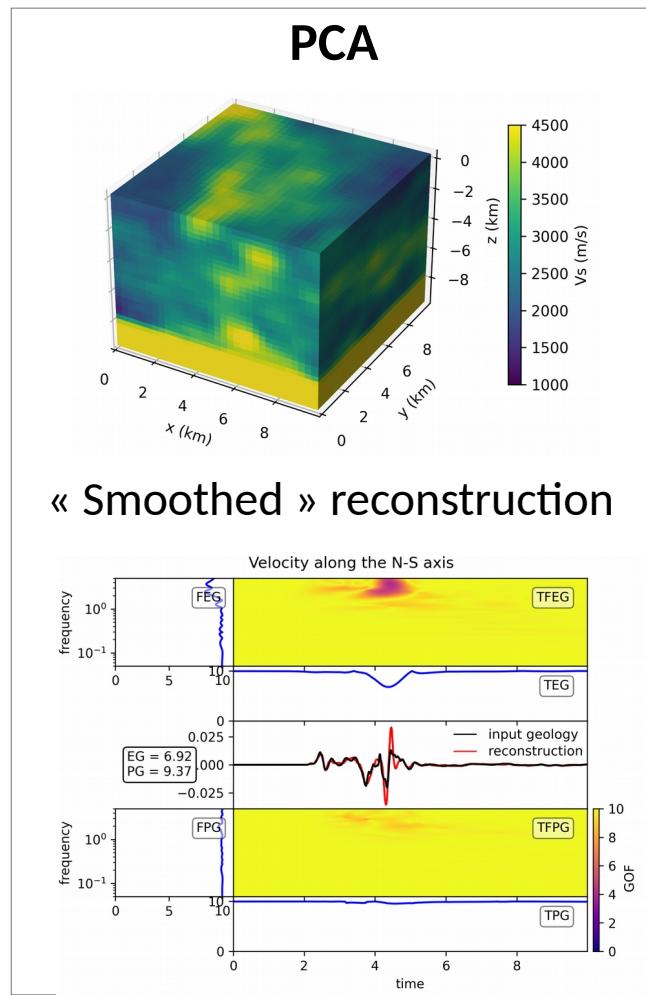
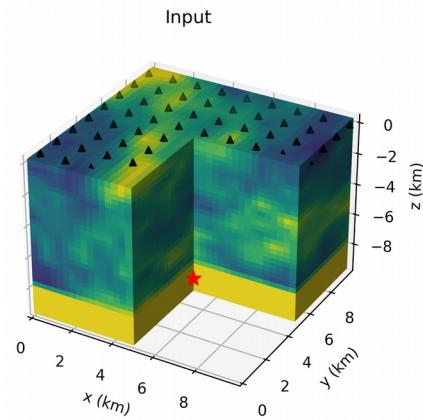
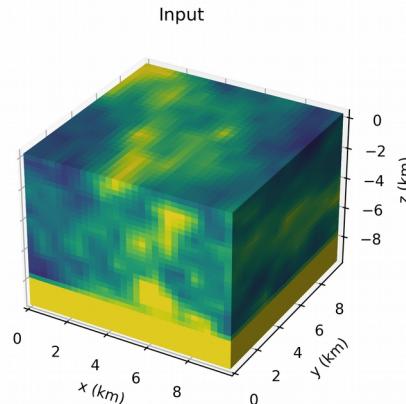
3D UNet [Çiçek et al. 2016], [Wolny et al. 2020]



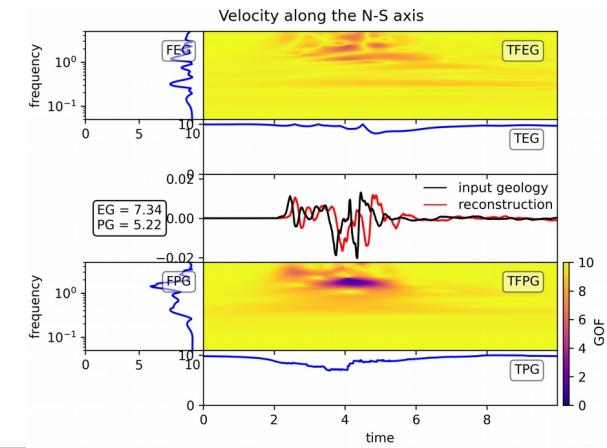
# Results - Reconstruction error



# Results - Influence of the reconstruction on the output



Biased reconstruction (mean value)



# Conclusion

