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4 **Low-Power Gas Microbubble Detection Technology based on Acoustic Resonance**  
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27 **Abstract**  
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31 A novel approach towards developing a micro-bubble detection technology based on using a PZT  
32 transducer to induce an acoustic resonance state within the system under investigation is here  
33 presented. The concept, originally proof-of-concept tested in a cylindrical acoustic resonant  
34 chamber, has proven to be able to detect single microbubbles with diameters in the range of 390  
35 to 600  $\mu\text{m}$  in a swine thigh, with either saline solution or sheep blood as the medium in the  
36 bubble guide. It has shown to be extremely adaptable, capable of accommodating industrial pipes  
37 as well as biological specimens, resilient and extremely energy efficient, able to detect micro-  
38 bubbles with as little as 0.8 mW and potentially less.  
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51 Gas bubble detection is a critical component of the instrumentation needed in many industrial and  
52 medical processes as well as in fundamental research of two-phase flow systems, cavitation  
53 phenomena, sonochemistry, sonoluminescence, and even biophysics of gene transport <sup>[1-9]</sup>. Real-  
54 time information and detection of bubble populations are required for most filling operations in  
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4 the paint, food, detergent, and cosmetic industries where bubbles can compromise the final product  
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6 <sup>[10, 11]</sup>. In Ecology and Climate Science, bubble detection technology is required to understand the  
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8 flux of greenhouse gases such as methane and carbon dioxide between the ocean and the  
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10 atmosphere <sup>[12-16]</sup>. In the field of medicine, the demand for air bubble detectors is surging, as  
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12 healthcare practitioners are increasingly using these devices in combination with infusion pumps,  
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14 dialysis equipment, and other fluid management applications. It is estimated that by 2030 the  
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16 world market for air bubble detectors will be around \$200 million <sup>[17]</sup>.  
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22 Bubble detection based on ultrasonic attenuation is by far the most common technique of current  
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24 bubble detectors <sup>[18-22]</sup>. Ultrasonic bubble detectors are effective and convenient in applications  
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26 when bubbles no smaller than around 800  $\mu\text{m}$  need to be detected in tubings of a specific size.  
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28 But for the detection of smaller bubbles and in systems more complicated than a vinyl tube, the  
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30 power requirements steeply increase, and the overall hardware and setup becomes prohibitively  
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32 complicated and costly <sup>[11, 16, 22]</sup>.  
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37 We report on our recent results obtained from a novel bubble detection technology based on  
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39 acoustic resonance that accommodates any system of any geometry through which bubbles may  
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41 travel and need to be detected. Besides its high degree of adaptability, it has extremely low power  
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43 requirements, it is highly portable and highly sensitive; detecting bubbles as small as  $3 \times 10^{-5}$  mL.  
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45 The technology uses a ring, or segments of a ring, piezoelectric (PZT) transducer attached and  
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47 coupled around the girth of an object. Electrical current, voltage, current-to-voltage phase lag,  
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49 and frequency across the PZT are constantly measured and recorded. Acoustic resonance of the  
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51 coupled PZT – load system is correlated to the electric resonance measured in the PZT. The  
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53 concept was originally developed in a resonant acoustic chamber designed by our group <sup>[9, 23, 24]</sup>.  
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57 Briefly, this acoustic chamber consists of a cylindrical borosilicate glass with diameter of 95 mm  
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4 and 300 mm in length, sandwiched between two square acrylic flanges were all required fittings  
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6 for fluid and bubble injection are installed. An 8mm vinyl tube runs the length of the glass  
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8 cylinder where bubbles are injected, and the rest of the chamber is filled with degassed water. A  
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10 ring PZT is attached to the outer surface of the cylindrical glass. **Figure 1A** shows a schematic  
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12 drawing of the vertical cross-section of the acoustic resonance chamber. A frequency scan is  
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14 conducted in order to establish the acoustic resonance of the system. Once established an  
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16 acoustical pressure standing-wave is generated inside the cavity enclosed by the PZT. The same  
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18 figure also shows the vertical acoustic pressure distribution created when the transducer is driven  
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20 at the resonance frequency. The large peak located at the height of the PZT represents the main  
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22 anti-node of the standing wave and is seen accompanied by several much smaller “satellite”  
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24 antinodes. Any appearance of an inhomogeneity such as a gas bubble will perturb the resonance  
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26 state which should reflect in the recorded electric signals from the PZT.  
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34 In **Figure 1B** the electric analogous of the resonance state is shown. Figure 1B shows the  
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36 conductance measured across the PZT as function of frequency. Driving the PZT at the frequency  
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38 at which conductance is maximum will put the system in mechanical resonance and the pressure  
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40 standing wave of Figure 1A is obtained. Slug flow with a large Taylor bubble of around 7 mm in  
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42 size was introduced into the chamber through the vinyl tube and positioned at the center of the  
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44 cylindrical chamber. After this, a frequency scan of conductance was performed. The results,  
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46 shown in Figure 1B, reveal that the conductance peak obtained without the bubble, shifts towards  
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48 higher frequency and reduces in magnitude when the bubble is inside the chamber at the height of  
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50 the PZT. When a constant voltage amplifier supplies the power, this change in conductance due  
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52 to the presence of the bubble will manifest as a current drop across the PZT and this constitutes  
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54 the bubble detection mechanism.  
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4 This concept was tested on a more challenging system to test for its adaptability, resilience, and  
5 sensibility. First of all, instead of a complete ring PZT, only two ring segments, each shorter than  
6 a semicircle, were used in order to provide flexibility to attach to different geometries and sizes.  
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8 Secondly, these PZT ring segments were wrapped around a freshly cut swine thigh supplied by a  
9 local meat distributor. The segments were kept in place with an elastic band around them and  
10 ultrasonic gel was used to fill out the gaps between the PZT and the swine meat. The ring  
11 segments were then serially connected, and operation as described for the acoustic chamber was  
12 carried out. **Figure 2A** shows a schematic of the swine thigh with the PZT attached. A frequency  
13 scan, as previously described, was carried out to determine the frequency of maximum  
14 conductance. The PZT was driven continuously at the electrical resonant frequency and  
15 measurements with a hydrophone were done to determine whether the swine thigh was in a  
16 mechanical resonant state. As seen in Figure 2A, a clear standing-wave profile with clear nodes  
17 and antinodes was generated inside the swine thigh. Compared to the glass acoustic chamber, the  
18 secondary antinodes, those not at the height of the PZT, are much more pronounced than those in  
19 the acoustic chamber.  
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41 Once we confirmed that the acoustic pressure standing-wave was generated inside the swine  
42 thigh, and that the equivalence between the mechanical resonant state of the PZT-swine thigh  
43 coupled system and the electric resonant state of the PZT hold as it did for the glass cylinder,  
44 bubble detection tests in the swine thigh were performed. The experimental setup required for  
45 this task can be seen in **Figure 2B**. Briefly, a freshly cut swine thigh with a blood-mimicking  
46 prosthetic vessel transversely positioned serving as a bubble guide, was vertically hanged as to  
47 allow an injected bubble to travel the length of the vessel by buoyancy. The end of the vessel  
48 sticking out of the bottom of the swine thigh was connected to a pressure-controlled bubble  
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4 capillary bubble generator, while the upper extreme is submerged in a water-filled “outlet pool”  
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6 (Figure 2B) where any injected bubble is discharged and recorded for image analysis. The 50 fps  
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8 high-speed Cameras 1 and 3 in Figure 2B record injected and discharged bubbles at the pool  
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10 outlet respectively. Finally, the two-segment PZT serially connected is attached to the swine  
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12 thigh as seen in the figure. The PZT is powered by a Keysight 33500B wave generator amplified  
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14 by an E&I 1040L RF power amplifier which increases output power by 55dB. The RMS voltage  
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16 and current across the PZT is monitored while the PZT is operated at the resonant frequency at  
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18 different powers. Typical voltage RMS data of the unperturbed system in the resonant state is  
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20 shown in **Figure 2C**. As expected, the RMS voltage value randomly fluctuates around some  
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22 average value determined by the supplied power and conductance of the PZT.  
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29 With the experimental setup of Figure 2B in place, bubble detection tests were carried out by  
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31 injecting bubbles into the artificial blood vessels in a controlled manner and searching for any  
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33 changes in the measured RMS voltage across the PZT. Again, the hypothesis being that a bubble  
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35 traveling along the swine thigh which is in mechanical resonance will perturb the resonant state  
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37 and this will reflect on the electric resonant state in the form of a change in the RMS behavior.  
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41 **Figure 3A** shows the voltage RMS value as a function of time of two consecutive tests, one  
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43 powered at 20 mW and the other 8 mW and each with a 575  $\mu\text{m}$  in diameter bubble injected.  
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45 Saline solution 0.9%wt was used as the liquid medium filling the vessel bubble guide and the  
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47 outlet pool. The experiment is programmed to begin the data collection process at precisely the  
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49 instant the bubble detaches from the capillary tip. Initially, the bubble will travel a segment of the  
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51 bubble guide between the bubble generator and the swine thigh. During this time, which depends  
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53 on the bubble size, the RMS should behave similar to Figure 2C, and at some point along the  
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55 trajectory inside the swine thigh, an RMS perturbation should be observed. In both consecutive  
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4 tests shown in Figure 3A, we observe a fluctuating RMS baseline for about the first 4 seconds, at  
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6 which point in time a clear, well defined and well above noise level RMS signal can be discerned.  
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8 Several key observations are worth highlighting. First, both consecutive tests present an onset of  
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10 the signal perturbation at exactly the same instant in time, indicating that the measurement is  
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12 reliable and surprisingly reproducible when considering that the system is a hanging dead swine  
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14 thigh. Secondly, the baseline value and short-term behavior can vary significantly, likely due to  
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16 being powered by only 20 mW. However, reproducible features consisting of valleys and peaks  
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18 consistently appearing at the same instant in the signal are visible. However, one of the most  
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20 surprising observations was the fact that the onset of the bubble signal consistently coincide with  
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22 the moment the bubble reached the point in the prosthetic vessel that entered inside the swine  
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24 thigh, and completely died out at the moment the bubble appeared on the other side right before  
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26 reaching the outlet pool. Considering that the moment the microbubble enters the approximately  
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28 38 lbs. swine thigh is at least 1 ft away from the PZT and that with 20mW the resonant state is  
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30 sensitive enough to generate a clear detection signal is quite unprecedented.  
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39 To further test the detection system capabilities, smaller single bubbles (410 and 420  $\mu\text{m}$  in  
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41 diameter) were generated and injected into the swine thigh through the bubble guide with the  
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43 PZT operated at resonance with 3mW supplied power. The results of two consecutive tests of this  
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45 type are presented in **Figure 3B**. Other trials under the same experimental conditions yielded  
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47 similar results. As in the previous experiments, a clear signal can be observed as soon as the  
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49 bubble entered the swine thigh with attributes that consistently appeared in all the experiments  
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51 and that lasted the bubble's entire time of flight inside the swine. The results of both set of  
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53 experiments presented in Figures 3A and 3B suggest that the particular form the voltage RMS  
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55 signal obtains is related to the pressure standing wave profile (Figure 2A) since it also consists of  
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4 a series of peak and valleys distributed along the entirety of the swine thigh. Following the set of  
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6 experiments presented in figure 3, we proceeded to test detection capabilities applying only 0.8  
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8 mW to the PZT, the lowest power possible allowed by the generator. In each test a single bubble,  
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10 with diameters between 402 and 395  $\mu\text{m}$ , was injected with PZT operated at resonance and the  
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12 RMS voltage was recorded. Four consecutive tests under these experimental conditions are  
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14 shown in **Figure 4A**. Just as in previous cases, a distinguishable signal with reproducible features  
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16 appear in the voltage RMS data as soon as the test single bubble enters the swine. Arrows in the  
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18 figure point out the signal's features that consistently appear in all four tests. Baseline RMS  
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20 appears to fluctuate more than in previous cases, but this is expected given that the supplied  
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22 power is only 0.8 mW. Since how the presence of the bubble affects the pressure profile as it  
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24 travels along the swine thigh and goes through each of the antinodes would depend on many  
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26 factors such as bubble size, bubble speed, power applied and many particularities of the swine  
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28 meat that change with time and vary drastically from specimen to specimen, it is not surprising  
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30 that the form of the signal we observed considerably varied in different sets of experiments.  
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32 However, it is clear by looking at Figures 3A, 3B and 4A, that the distinguishable attributes of  
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34 the RMS signal are reproducible to a high degree proving that there is a finite set of factors that  
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36 predetermined the form of the signal. In the case presented in Figure 4A, although the main peaks  
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38 in the RMS data are equally reproducible, the baseline fluctuations observed at both extremes in  
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40 all cases makes it difficult to determine the duration or length of the signal. In order to determine  
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42 the time interval in which the signal is present, a numerical approximation of the data's derivative  
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44 was calculated. The results allowed for a single scale comparison and are presented in **Figure 4B**.  
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46 As seen in the figure, all the reproducible features observed in the RMS signal are confirmed in  
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48 its derivative. However, a clearer determination of the signal onset, at  $t=5.95\text{s}$ , can be established  
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50 as it is when the first signature feature consistently appearing in all tests occurs. Similarly, at  
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4  $t=20.56s$  the RMS derivative quickly settles into fluctuations around 0 V/s and can be considered  
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6 the end of the signal. Overall, the derivative shown in Figure 4B definitively proves that the  
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8 apparatus is detecting single microbubbles all along the length of the swine thigh, which again is  
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10 at least 1 ft long, while consuming only 0.8 mW. As a final test, a 600  $\mu m$  single bubble was  
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12 injected into the swine thigh through the prosthetic vessel, only in this instance, the vessel was  
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14 filled with defibrinated sheep blood purchased from HemoStat Laboratories The voltage RMS  
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16 obtained in this experiment can be seen in **Figure 4C**, where the PZT is driven with 3 mW. Same  
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18 as in the cases where saline solution was used, the bubble traveling along the swine thigh through  
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20 the sheep blood medium generates a perturbation in the acoustic pressure standing wave inside  
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22 the swine thigh that manifests in the recorded RMS voltage. The drag force experienced by the  
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24 bubble is higher in blood than in saline solution and hence the signal in the RMS chart appears  
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26 much later in time than in the previous cases. The signal-to-noise ratio in the blood experiment is  
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28 comparable with that of saline solution and a clear signal can be observed with onset occurring  
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30 around  $t=19s$  and a form that resembles more the pressure profile observed in Figure 2A.  
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34 However, it is extremely difficult at this point to derive any exact association between the voltage  
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36 RMS signal observed and the pressure profile generated at resonance given that the exact  
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38 pressure profile is likely to change with each swine thigh and maybe day by day. Our work is  
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40 currently directed towards understanding the relationship between the pressure profile and  
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42 characteristics of the RMS signal.  
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51 In conclusion, we have reported on a novel approach to developing a bubble detection technology  
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53 based on using a PZT transducer to induce an acoustic resonance state within the system under  
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55 investigation. Based on the hypothesis that if the mechanical resonant state of the system  
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57 corresponds to the electric resonance state of the PZT then the appearance of any inhomogeneity  
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4 such as a microbubble would reflect on the electric response by interacting with the standing  
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6 wave. The concept was tested and confirmed in a cylindrical acoustic resonant chamber.  
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8 Moreover, the technology proved to be able to detect single microbubbles in the range of 390 to  
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10 600  $\mu\text{m}$  in a swine thigh, with either saline solution or defibrinated sheep blood as the medium in  
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12 the bubble guide. Absolute limits of bubble size sensitivity have not been established and based  
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14 on the results here presented, the bubble size range it can detect is likely much larger. The major  
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16 innovative benefits the technology has is its high degree of adaptability, as it can accommodate  
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18 industrial pipes or a biological specimen, consistency, reliability and that it can be operated with  
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20 as little as 0.8 mW (potentially less, the limit has not been established). Additionally, the spatial  
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22 range of detection covered the entire swine thigh in 100% of the cases, and therefore more work  
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24 is required to determine how large is the range of detection.  
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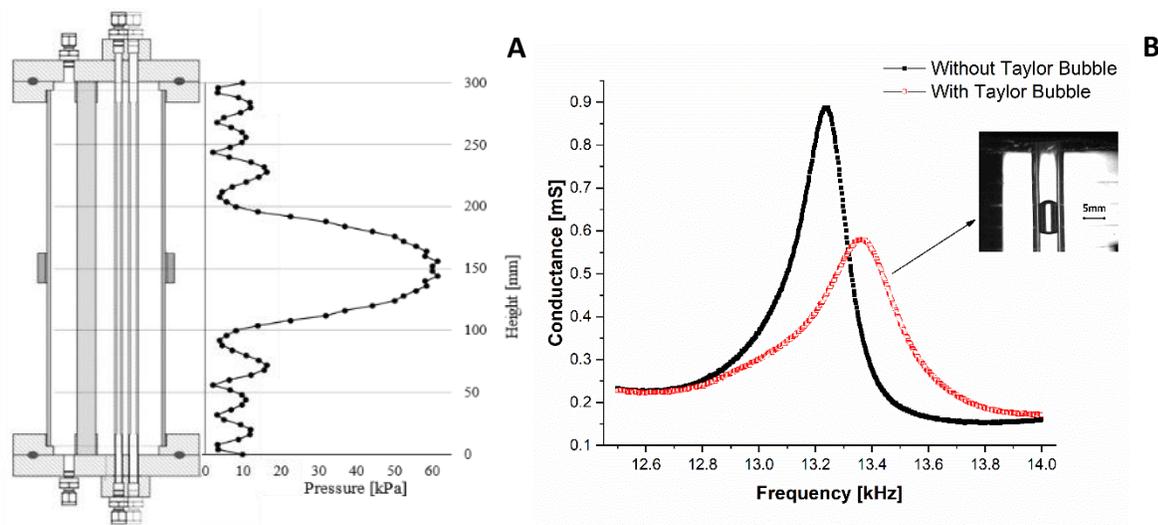
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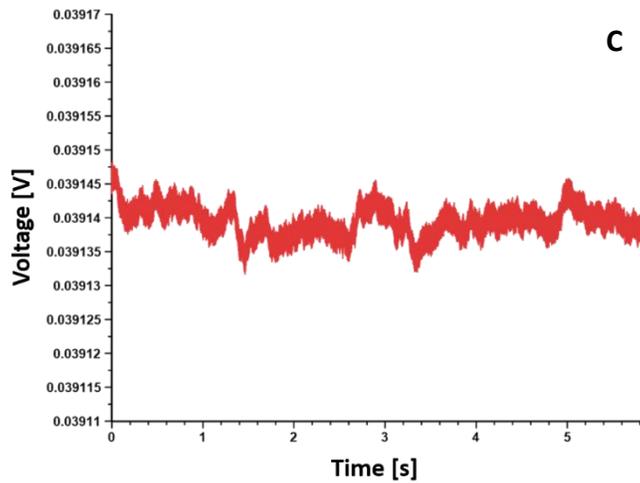
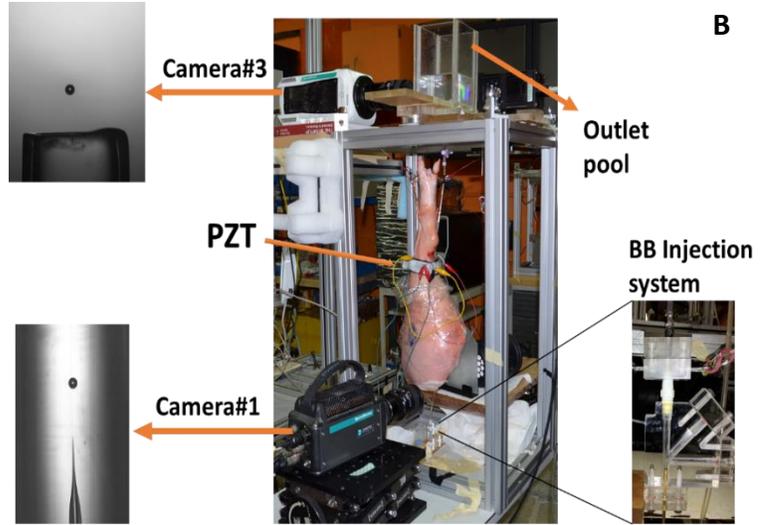
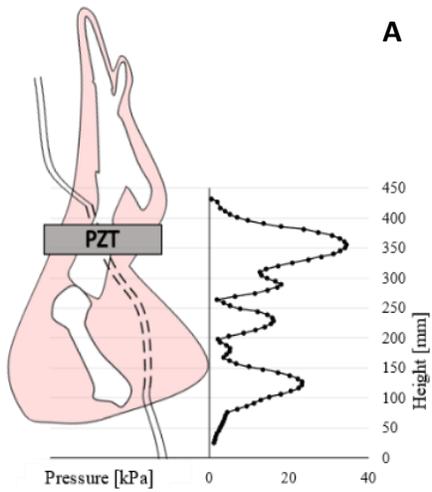
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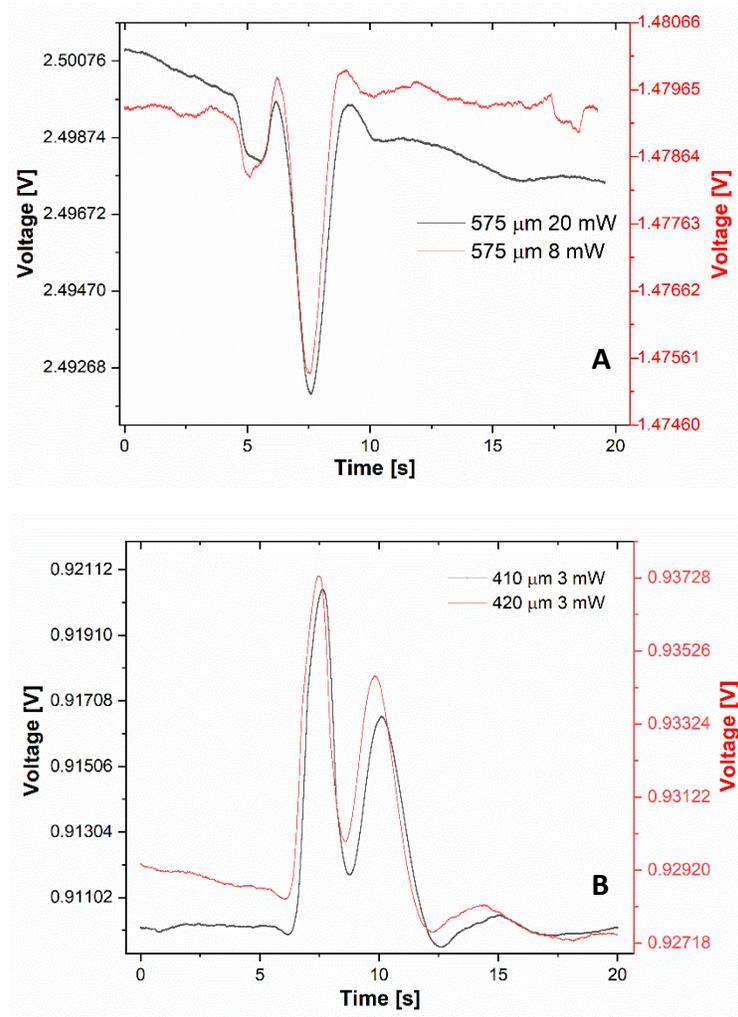


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47 **Figure 1.** A) Schematic drawing of a cross-section of the acoustic resonance chamber along the  
48 pressure profile when chamber is in the resonant state. B) The conductance of the PZT as  
49 function of frequency. Peaks correspond to electric resonance frequency. Black curve represents  
50 the chamber's native state and the red curve corresponds to the chamber with a Taylor bubble  
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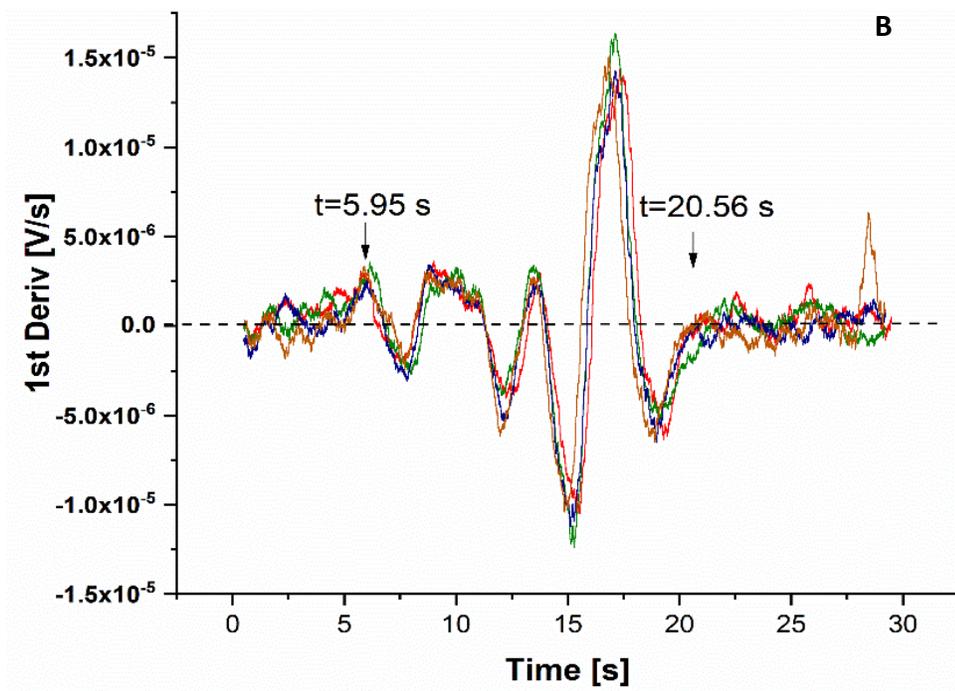
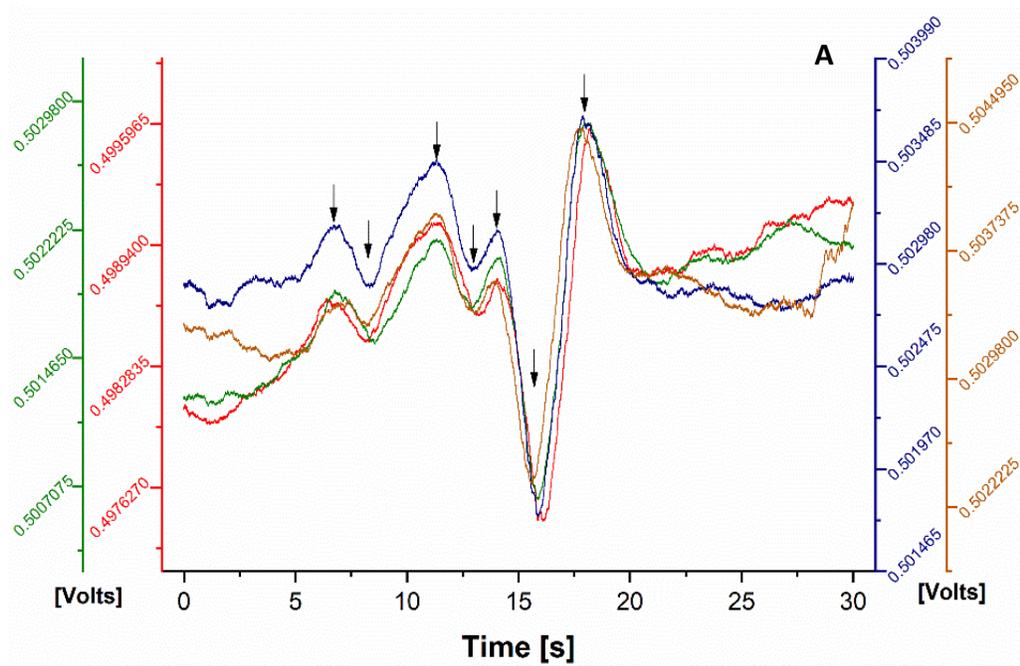
**Figure 2.** A) schematic of the swine thigh with the PZT attached and the pressure standing-wave profile generated within when the PZT is operated at its electric resonance frequency. B) Photograph of the experimental setup required for the bubble detection experiments. C) RMS of voltage monitored across the powered PZT with no bubbles present.

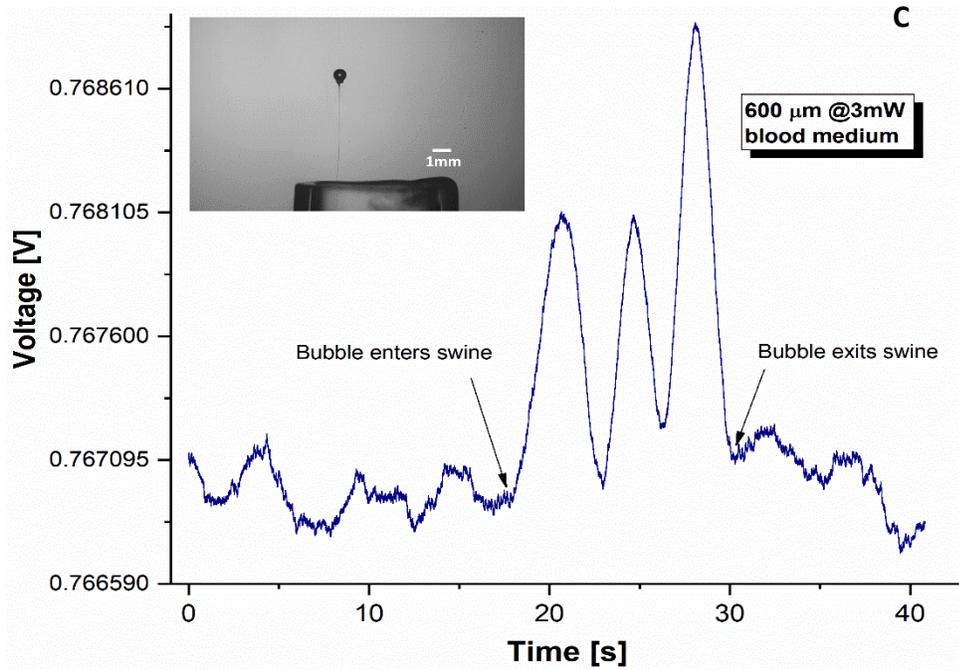
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**Figure 3.** A) Two consecutive tests showing the voltage RMS as function of time using a 575 μm single bubble and two different powers and B) RMS signal of a 410 and 420 μm bubbles powered at 3mW each; the 10 nm is enough to slightly shift the peak of the largest bubble to the left due to having higher speed

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**Figure 4.** A) Four consecutive detection tests performed at 0.8 mW on bubbles around 400  $\mu\text{m}$  in diameter. Arrows indicate reproducible features that constitute the detection signal. B) First derivative numerical approximation of the RMS data in A). C) 600  $\mu\text{m}$  single bubble detection test using defibrinated sheep blood instead of saline solution and operated at 3 mW.