

1       **Seasonal and hemispheric asymmetries in the cold ion**  
2               **outflow source region: Swarm and CHAMP**  
3               **observations of  $F$ -region polar cap plasma density**

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10       **Key Points:**

- 11       • Statistics of  $F$ -region polar cap plasma density derived from 15 years of measure-  
12               ments exhibit several types of seasonal asymmetries
- 13       • Statistics do not support the conjecture that limited plasma availability is the cause  
14               of observed hemispheric asymmetries in lobe density
- 15       • Southern Hemisphere polar cap plasma densities lag those in Northern Hemisphere  
16               by at least two weeks around local spring and fall equinox

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17 **Abstract**

18 One of the primary mechanisms of loss of Earth’s atmosphere is the persistent “cold”  
 19 ( $T \lesssim 20$  eV) ion outflow that has been observed in the magnetospheric lobes over large  
 20 volumes with dimensions of order several Earth radii ( $R_E$ ). As the main source of this  
 21 cold ion outflow, the polar cap  $F$ -region ionosphere and conditions within it have a dis-  
 22 proportionate influence on these magnetospheric regions. Using 15 years of measurements  
 23 of plasma density  $N_e$  made by the Swarm spacecraft constellation and the CHAMP space-  
 24 craft within the  $F$  region of the polar cap above  $80^\circ$  Apex magnetic latitude, we report  
 25 evidence of several types of seasonal asymmetries in polar cap  $N_e$ . Among these, the tran-  
 26 sition between “winter-like” and “summer-like” median polar cap  $N_e$  occurs one week  
 27 prior to local spring equinox in the Northern Hemisphere (NH), and one week after lo-  
 28 cal spring equinox in the Southern Hemisphere (SH). Thus the median SH polar cap  $N_e$   
 29 lags the median NH polar cap  $N_e$  by approximately two weeks with respect to hemispher-  
 30 ically local spring and fall equinox. From interhemispheric comparison of statistical dis-  
 31 tributions of polar cap plasma density around each equinox and solstice, we find that dis-  
 32 tributions in the SH are often flatter (i.e., less skewed and kurtotic) than in the NH. Per-  
 33 haps of most significance to cold ion outflow, we find no evidence of an  $F$ -region plasma  
 34 density counterpart to a previously reported hemispheric asymmetry whereby cold plasma  
 35 density is higher in the NH magnetospheric lobe than in the SH lobe.

36 **Plain Language Summary**

37 The Earth’s magnetic poles are not perfectly aligned with the Earth’s geographic  
 38 poles, and the degree of misalignment is greater in the Southern Hemisphere. Further-  
 39 more, as a result of the Earth’s elliptical orbit around the Sun, summer and fall in the  
 40 Northern Hemisphere together are approximately one week longer than summer and fall  
 41 in the Southern Hemisphere, because the Earth is very slightly closer to the Sun around  
 42 December solstice (summer in the Southern Hemisphere). These seasonal asymmetries,  
 43 together with the asymmetric displacement of the Earth’s magnetic poles relative to the  
 44 geographic poles, suggest that the plasma density in the topside ionosphere’s geomag-  
 45 netic polar regions may also be subject to seasonal and hemispheric asymmetries. The  
 46 polar regions are the primary site of loss of the Earth’s atmosphere via so-called ion out-  
 47 flow processes that, over geological time scales, are believed to lead to loss of the Earth’s  
 48 atmosphere. Using 15 years of plasma density measurements made by four different satel-

49 lites to statistically study the plasma density of each hemisphere’s geomagnetic polar cap  
 50 ionosphere in the altitude range 350–520 km, we find that the polar cap ionosphere at  
 51 these altitudes exhibits a variety of seasonal and hemispheric asymmetries.

## 52 **1 Introduction**

53 A substantial fraction of the plasma in the Earth’s magnetosphere is supplied by  
 54 the ionosphere (e.g., Chappell et al., 1987, 2000) through ion outflow from the high-latitude  
 55 polar cap regions, where terrestrial magnetic field lines are open and connected to so-  
 56 lar wind magnetic field lines. By the same token, ion outflow is also considered to be a  
 57 primary means of loss of the Earth’s atmosphere (e.g., André, 2015). Ion outflow is the  
 58 result of ionization of atmospheric gases and outward transport due to vertical forces.  
 59 Recent results suggest that low-energy ions from the open polar cap area usually dom-  
 60 inate the ion density and the outward flux in populating large volumes of the magne-  
 61 tosphere. Furthermore, ionization (i.e., availability of free charges) rather than trans-  
 62 port is reported to be the limiting factor for ion outflow (Haaland et al., 2012; André  
 63 et al., 2015).

64 Ionization is primarily driven by solar illumination, although other processes such  
 65 as cosmic rays (e.g., Adams & Masley, 1965; Velinov, 1970) and particle precipitation  
 66 also contribute (e.g., Rees, 1963, 1982). Solar radiation at ultraviolet (UV) and extreme  
 67 ultraviolet (EUV) wavelengths is the most efficient source of ionization in terms of ion-  
 68 izing atmospheric atoms and molecules and producing ion-electron pairs (e.g., Apple-  
 69 ton, 1956; Ivanov-Kholodnyy, 1962; Rees, 1989; Brekke, 1997; Schunk & Nagy, 2009).  
 70 Since the ionosphere as a whole is quasi-neutral, both the electron number density and  
 71 ion number density are often simply referred to as the plasma density.

72 The resulting plasma density in the atmosphere is a balance between production  
 73 (ionization) processes on one hand, and losses by recombination and transport processes  
 74 on the other hand (e.g., Quinn & Nisbet, 1965; Khocholava, 1977; Rees, 1989; Rishbeth,  
 75 1997). Production and loss processes do not necessarily work on the same time scale, so  
 76 at a given location in space, there can be significant variation in the plasma density over  
 77 time.

78 In the terrestrial atmosphere, the peak plasma density is typically located in the  
 79 ionospheric *F* layers, around 200–400-km geodetic altitude (e.g., Rishbeth, 1962; Feld-

stein et al., 1975). Since ionization is strongly driven by solar illumination, plasma density exhibits solar cycle variations as well as strong seasonal and diurnal variations (e.g., Appleton, 1939). Typical plasma densities are of order  $10^5$ – $10^6$   $\text{cm}^{-3}$  in the sunlit ionosphere, but can be less by an order of magnitude or two in darkness.

In the polar regions the variation of plasma density with season is strongest, followed by diurnal variation and variation with solar cycle (e.g., Feldstein et al., 1975). The seasonal variation can largely be understood on the basis of solar illumination; under summer conditions, the polar cap is fully illuminated. Conversely, under winter conditions major portions of the polar cap are in complete darkness. The Sun-Earth distance plays a lesser, though non-negligible, role for variations in solar illumination (e.g., Dang et al., 2017). From the standpoint of plasma density variation, one would expect solar illumination, ionization and plasma production around equinox to be very similar in the Northern and Southern Hemisphere.

In contrast to ionization and production of ionospheric plasma, which are primarily due to solar EUV radiation, transport of ionospheric plasma is driven mostly by electromagnetic forces and is organized with respect to the geomagnetic rather than the geographic poles. Horizontal transport is mainly driven by large scale magnetospheric convection set up by reconnection at the dayside magnetopause (e.g., Dungey, 1963), and thermospheric neutral winds (e.g., Förster et al., 2008). Vertical transport—upflow and outflow—is due to a combination of various forces. Theoretical descriptions of ion outflow at the polar caps were developed in the 1960s (e.g. Dessler & Michel, 1966; Nishida, 1966; Axford, 1968; Banks & Holzer, 1968) and collectively comprise the classical polar wind paradigm. In this view, light ion species in the ionosphere gain upward mobility via plasma and neutral pressure gradients as well as ambipolar electric fields formed and sustained by requiring charge balance between electrons and ions in the ionosphere. Due to the mirror force, any additional transverse acceleration at the exobase (500–1000 km) and above effectively acts as upward acceleration (e.g., Klumpar, 1979). At altitudes of a few  $R_E$ , centrifugal forces (Cladis, 1986; Horwitz et al., 1994; C. Liu et al., 1994; Nilsson et al., 2008, 2010) become dominant.

Thus, the significant difference in magnetic topology of the Northern and Southern Hemisphere polar regions (e.g., Cnossen & Förster, 2016; Laundal et al., 2017) is a likely factor in reported hemispheric asymmetries in ionospheric outflow around equinox

112 (e.g., Maes et al., 2016; Haaland et al., 2017; Li et al., 2020). These differences do play  
113 a role, for example, in the seasonal variation of thermospheric and ionospheric winds (Aruliah,  
114 Farmer, Fuller-Rowell, et al., 1996; Aruliah, Farmer, Rees, & Brändström, 1996; Mikhailov  
115 & Schlegel, 2001).

116 Estimation of the total loss of geogenic plasma due to ion outflow is subject to ad-  
117 ditional complications that arise because the source regions (primarily the open polar  
118 cap, but also cusp and auroral zone) vary greatly in size and shape in response to so-  
119 lar wind driving (Sotirelis et al., 1998; Milan et al., 2008; Milan, 2009; Li et al., 2012).

120 In this study, we follow up on previous studies (Haaland et al., 2012; André et al.,  
121 2015; Haaland et al., 2017) indicating or otherwise suggesting that available ionospheric  
122 plasma rather than transport is the limiting factor for cold ion outflow from the polar  
123 cap. Using a large database of ionospheric plasma density measurements made by the  
124 Swarm and CHAMP satellites in both hemispheres, we seek to determine under which  
125 seasons hemispheric asymmetries in cold plasma outflow might be expected on the ba-  
126 sis of available ionospheric plasma.

127 This study is organized as follows. In section 2 we describe the Swarm and CHAMP  
128 combined polar cap plasma density database. In section 3 we identify and describe a num-  
129 ber of seasonal and hemispheric asymmetries in polar cap plasma density. In section 4  
130 we discuss results from the preceding section and describe some implications for cold ion  
131 outflow. In section 5 we summarize the results of this study and conclude.

## 132 **2 Swarm and CHAMP Plasma Density Measurements**

133 We use plasma density measurements made by two separate missions, the original  
134 three-satellite Swarm constellation (Friis-Christensen et al., 2008) and the Challenging  
135 Mini-Satellite Payload (CHAMP) satellite (Reigber et al., 2006).

136 The original three Swarm satellites complete approximately 15 orbits per day in  
137 a near-polar orbit, over the six-year period extending from launch on 22 November 2013  
138 to the present. The two lower satellites, Swarm Alpha (Swarm A) and Swarm Charlie  
139 (Swarm C), cover the range of geodetic altitudes between 445 km and 500 km (up to 527  
140 km during commissioning phase); Swarm Bravo (Swarm B) covers the range of geode-  
141 tic altitudes between 510–545 km (down to 500 km during commissioning phase). The  
142 Electric Field Instrument (EFI) (Knudsen et al., 2017) aboard the three original Swarm

143 satellites includes two dedicated low-gain and high-gain Langmuir Probes (LPs). The  
 144 two LPs measure plasma density and electron temperature at 2 Hz. The most complete  
 145 in-flight calibrations and validations of the Swarm LP plasma density and electron tem-  
 146 perature measurements, based on comparisons with plasma density measurements mea-  
 147 sured by other satellites and ground-based instruments, have been performed by Lomidze  
 148 et al. (2018).

149 The CHAMP satellite also completed approximately 15 orbits per day in a near-  
 150 polar orbit over a  $\sim 10$ -year period extending from 15 July 2000 to 19 September 2010.  
 151 The nominal range of geodetic altitudes covered by CHAMP extended over  $\sim 300$ – $455$   
 152 km. The Planar Langmuir Probe (PLP) instrument (Rother et al., 2005) aboard CHAMP  
 153 made measurements of plasma density at a 15-s cadence. In-flight calibration of the PLP  
 154 instrument has been performed by McNamara et al. (2007).

155 In this study we use all Swarm Level 1B LP plasma density measurements down-  
 156 sampled to 15-s cadence, from the period between 10 Dec 2013 and 5 Feb 2020 ([https://  
 157 swarm-diss.eo.esa.int/](https://swarm-diss.eo.esa.int/)). Downsampling is achieved by selecting every 30th measure-  
 158 ment. We also use all CHAMP Level 2 PLP plasma density measurements from the pe-  
 159 riod between 19 Feb 2002 and 21 Dec 2009 (<ftp://isdctp.gfz-potsdam.de>) made at  
 160  $\geq 350$ -km geodetic altitude. We impose this altitude restriction on CHAMP density mea-  
 161 surements to ensure that all plasma density measurements are made above the altitude  
 162 at which the  $F2$ -layer plasma density peak  $hmF2$  is located (e.g., Shim et al., 2011; Burns  
 163 et al., 2012; Bjoland et al., 2016). To Swarm plasma density measurements we apply the  
 164 Lomidze et al. (2018) in-flight calibrations (see Appendix A).

165 Since ion outflow and ionosphere-magnetosphere coupling are organized by the ge-  
 166 omagnetic field we are here concerned with the geomagnetic polar cap, which we define  
 167 (Table 1) as the region at and above  $80^\circ$  magnetic latitude (MLat) in the Modified Apex  
 168 coordinate system at a reference geodetic altitude of 110 km (i.e.,  $MA_{110}$  coordinates)  
 169 (Richmond, 1995; Laundal & Richmond, 2016). We perform the conversion of geocen-  
 170 tric coordinates of each satellite to  $MA_{110}$  coordinates via the `apexpy` Python package  
 171 (Emmert et al., 2010; van der Meeren et al., 2018). Table 1 summarizes some proper-  
 172 ties of the polar caps in each coordinate system.

173 The total numbers of plasma density ( $N_e$ ) measurements in the Northern Hemi-  
 174 sphere (NH) and Southern Hemisphere (SH) geomagnetic polar caps are respectively 2,410,423

**Table 1.** Definitions and properties of the geomagnetic and geocentric polar caps.

Hemisphere	Polar cap	Area <sup>a</sup> (km <sup>2</sup> )	Circumference <sup>a</sup> (km)
<i>Geomagnetic (<math>MA_{110}</math>) coordinates</i>			
North	$\geq 80^\circ$ MLat <sup>b</sup>	$3.98 \times 10^6$	$7.11 \times 10^3$
South	$\leq -80^\circ$ MLat	$3.65 \times 10^6$	$6.76 \times 10^3$
<i>Geocentric coordinates</i>			
North	$\geq 80^\circ$ Lat <sup>c</sup>	$3.91 \times 10^6$	$6.98 \times 10^3$
South	$\leq -80^\circ$ Lat	$3.91 \times 10^6$	$6.98 \times 10^3$

<sup>a</sup>Area and perimeter at 0-km altitude.

<sup>b</sup>MLat  $\equiv$  Magnetic latitude in  $MA_{110}$  coordinates (see text).

<sup>c</sup>Lat  $\equiv$  Latitude in geocentric coordinates.

175 and 1,045,654. There are two primary reasons that the statistical coverage of the NH ge-  
 176 omagnetic polar cap is greater. First, as a result of the greater displacement of the SH  
 177 geomagnetic pole relative to the geographic pole than the displacement in the NH, the  
 178 Swarm and CHAMP satellites pass less frequently through the SH geomagnetic polar  
 179 cap. Second, the SH geomagnetic polar cap area is approximately 9% smaller than the  
 180 NH geomagnetic polar cap area (Table 1 and Figure S1 in Supporting Information). The  
 181 difference in geomagnetic polar cap area arises because the Earth's magnetic field is stronger  
 182 in the vicinity of the SH magnetic pole than in the vicinity of the NH magnetic pole (Laundal  
 183 et al., 2017). The measurement coverage is approximately the same in both hemispheres  
 184 (2.64 and 2.68 million measurements in the NH and SH geocentric polar caps, respec-  
 185 tively) if one instead considers the polar caps defined in a geocentric coordinate system.

186 In the remainder of the manuscript all references to  $N_e$  and statistics refer only to  
 187 measurements made in the geomagnetic polar caps, unless specified otherwise.

188 We seek to investigate seasonal and hemispheric asymmetries via statistical com-  
 189 parison of plasma density measurements in the geomagnetic polar cap made by differ-  
 190 ent satellites. Such an investigation is complicated by a number of factors, including:

- 191 1. Differences in the altitudes of each satellite, which vary on time scales of days and  
 192 years due to satellite drag and operational maneuvers, and which are systemat-  
 193 ically different in the two hemispheres due to both the shape of each satellite's or-

194 bit and the oblateness of the Earth (Text S2 and Figures S2–S3 of the Support-  
 195 ing Information). These differences correspond to sampling of different heights in  
 196 the ionosphere.

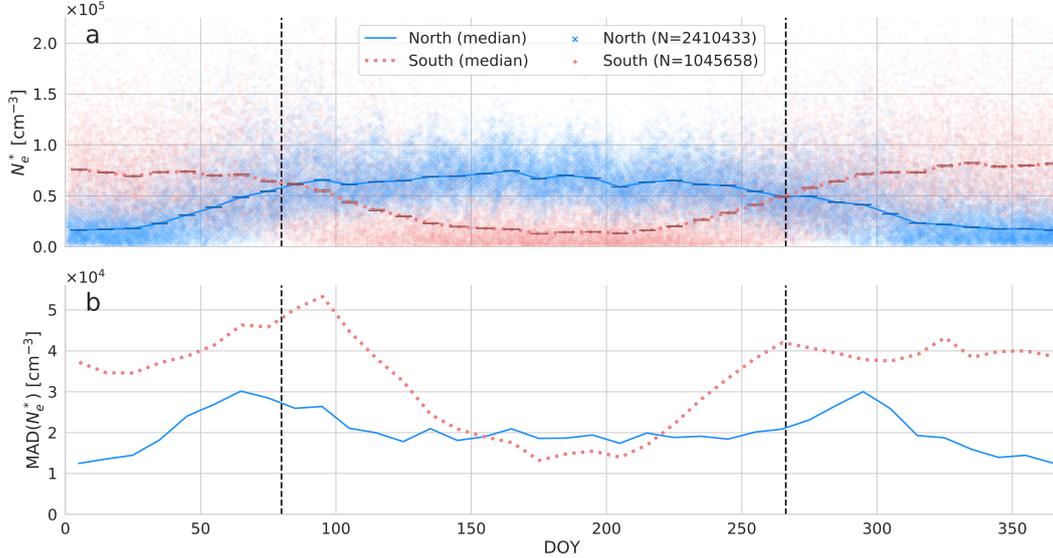
197 2. Variations in solar and geomagnetic activity, which lead to differences in ionospheric  
 198 conditions.

199 We partially account for these factors via (i) application of an empirically derived scale  
 200 height to  $N_e$  measurements that “maps”  $N_e$  to a common geodetic altitude of 500 km,  
 201 and (ii) application of an empirically derived correction factor that accounts for the vari-  
 202 ation of  $N_e$  measurements with 10.7-cm wavelength solar radio flux (otherwise known  
 203 as the  $F10.7$  index). The latter correction scales  $N_e$  to a nominal solar activity (normal-  
 204 ized solar radio flux index) of  $\langle F10.7 \rangle_{27} = 80$ , where  $\langle F10.7 \rangle_{27}$  is a rolling average of  
 205 the preceding 27 days of the  $F10.7$  index. Throughout this manuscript we use the no-  
 206 tation  $N_e^*$  to refer to these final adjusted densities. More details about the derivation  
 207 of the relevant scaling factors are located in Appendix A and in the Supporting Infor-  
 208 mation. This database of adjusted geomagnetic polar cap density measurements ( $N_e^*$ )  
 209 is publically available (Hatch et al., 2020).

### 210 **3 Hemispheric and Seasonal $N_e^*$ Variations**

211 Figure 1a shows  $N_e^*$  in the NH (blue) and SH (red) geomagnetic polar caps as a  
 212 function of day of year. The solid blue and dashed red lines respectively indicate the me-  
 213 dian NH and SH  $N_e^*$  values within 10-day bins.

214 One of the apparent differences between the median  $N_e^*$  values in the NH and SH  
 215 geomagnetic polar cap is that  $N_e^*$  takes on more extreme values in the SH than in the  
 216 NH. This difference may be related to the “ionospheric annual asymmetry,” which has  
 217 to do with NmF2, the ionospheric F2-layer peak plasma density, being about 30% greater  
 218 globally around December solstice than around June solstice (Rishbeth & Müller-Wodarg,  
 219 2006). The ionospheric annual asymmetry and related phenomena are well documented  
 220 (e.g. Mendillo et al., 2005; Torr et al., 1980; Rishbeth & Müller-Wodarg, 2006; Lei et al.,  
 221 2016; Dang et al., 2017; Xiong et al., 2018; Chartier et al., 2019; Sai Gowtam & Tulasi  
 222 Ram, 2017); the asymmetry is the result of a combination of effects related to solar ir-  
 223 radiance, atmospheric chemistry, neutral winds, and the global geomagnetic field con-



**Figure 1.** Geomagnetic polar cap plasma density  $N_e^*$  statistics versus day of year in the Northern Hemisphere and Southern Hemisphere. Here  $N_e^*$  denotes plasma density measurements that are scaled to a common geodetic altitude of 500 km and to a nominal solar activity of  $\langle F_{10.7} \rangle_{27} = 80$ , as described in Appendix A. (a)  $N_e^*$  measurements and binned medians. The transparent “x” and “+” markers respectively indicate 50,000 randomly selected individual measurements made in the NH and SH geomagnetic polar cap for each hemisphere. (Most readers will need to view the plot at full resolution or zoom in to see the distinction between these symbols.) Median  $N_e^*$  values within each 10-day bin are respectively indicated by the solid blue (North) and dashed red (South) line. Error bars indicate the 95% confidence interval of the bin median, calculated as described in Text S3 of the Supporting Information. (b)  $\text{MAD}(N_e^*)$  in the NH (solid blue line) and SH (dashed red line) geomagnetic polar caps, in 10-day bins. In both panels the dotted black lines at DOY  $\approx 79.9$  and DOY  $\approx 266.3$  respectively indicate the average DOY on which March and September equinoxes occur during the years 2000–2020; the time and date of each equinox is calculated as described in section 3.  $\text{MAD} \equiv$  median absolute deviation.

224 figuration. The precise role of the global geomagnetic field configuration, in particular,  
 225 apparently remains to be determined (Dang et al., 2017).

226 Central tendency and variation of a statistical quantity are often indicated by the  
 227 mean and standard deviation, respectively. However,  $N_e^*$  distributions in each bin in Fig-  
 228 ure 1a are heavy-tailed, and the mean is not a robust indicator of central tendency. In  
 229 Figure 1a we therefore show median  $N_e^*$  statistics in each bin. Likewise, in Figure 1b we  
 230 show the median absolute deviation

$$231 \quad \text{MAD}(N_e^*) \equiv \text{median} |N_e^* - \text{median}(N_e^*)|$$

232 instead of standard deviation to indicate the variation of  $N_e^*$  in each 10-day bin. Fig-  
 233 ure 1b shows  $\text{MAD}(N_e^*)$  in the Northern and Southern Hemisphere as solid blue and dashed  
 234 red lines, respectively.

235 Two salient aspects of  $\text{MAD}(N_e^*)$  curves in Figure 1b are (i) the SH  $\text{MAD}(N_e^*)$  is  
 236 typically greater than NH  $\text{MAD}(N_e^*)$ ; (ii)  $\text{MAD}(N_e^*)$  in the NH geomagnetic polar cap  
 237 evinces two distinct peaks, before March equinox and after September equinox, while  $\text{MAD}(N_e^*)$   
 238 in the SH geomagnetic polar cap evinces one primary peak after March equinox, a  $\text{MAD}(N_e^*)$   
 239 “plateau” that extends from September to the end of December, and a global minimum  
 240 near June solstice.

### 241 **3.1 Asymmetries in seasonal variation**

242 We now compare variations in  $N_e^*$  as a function of season. We wish to (i) avoid the  
 243 systematic bias that would be introduced by performing a comparison based on day of  
 244 year in the Gregorian calendar, which is inherently asymmetric from year to year with  
 245 respect to the day of year on which equinoxes and solstices occur; (ii) consistently ac-  
 246 count for variation in the length of the seasons themselves, which differ on the order of  
 247 days. To accomplish this, we scale the precise time period between each equinox and sol-  
 248 stice for each year such that the period between each equinox and solstice has a dura-  
 249 tion of 1, and the total duration of all four seasons (i.e., one year) is 4. We thus define  
 250 the “global season parameter”  $\phi_s \in [0, 4)$ , with March and September equinoxes respec-  
 251 tively corresponding to  $\phi_s = 0$  and  $\phi_s = 2$ . June and December solstices respectively  
 252 correspond to  $\phi_s = 1$  and  $\phi_s = 3$ . The timestamps of all  $N_e^*$  measurements are then  
 253 scaled to values between 0 and 4. The dates and times of occurrence of each equinox and  
 254 solstice for all relevant years between 2002 and 2020 are calculated to second precision

255 via the `skyfield` Python package (Rhodes, 2019). We also define the “local season pa-  
 256 rameter”

$$257 \quad \phi_l = \begin{cases} \phi_s & ; \text{NH}; \\ (\phi_s + 2) \pmod{4} & ; \text{SH}; \end{cases} \quad (1)$$

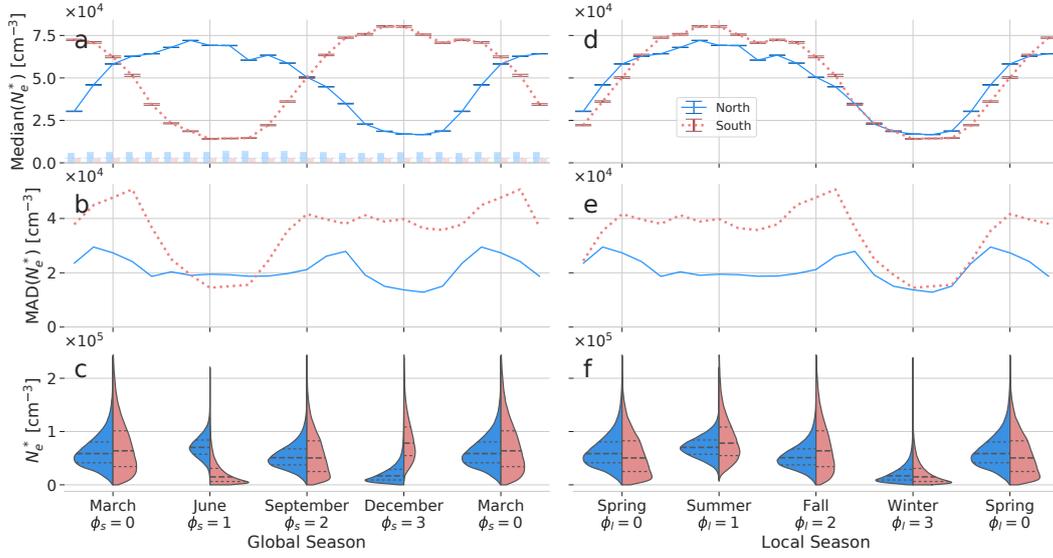
258 to compare  $N_e^*$  for the same local season in each hemisphere. For example  $\phi_l = 0$ , or  
 259 local spring equinox, corresponds to March equinox in the NH and September equinox  
 260 in the SH.

261 Figure 2a displays median  $N_e^*$  values in the NH (solid blue line) and SH (dotted  
 262 red line) geomagnetic polar caps as a function of  $\phi_s$  for bins of 0.2. At March equinox  
 263 the median value of SH  $N_e^*$  is  $7 \pm 1\%$  greater than the value of NH  $N_e^*$ , while there is  
 264 apparently no such asymmetry ( $0.4 \pm 1\%$ ) around September equinox.

265 Figure 2b displays  $\text{MAD}(N_e^*)$  in each hemisphere as a function of  $\phi_s$ . In addition  
 266 to the general trends in  $\text{MAD}(N_e^*)$  described at the beginning of this section, here it is  
 267 also apparent that the combined hemispheric  $\text{MAD}(N_e^*)$  at December solstice are greater  
 268 than the combined hemispheric  $\text{MAD}(N_e^*)$  around June solstice. The globally greater  
 269 variability of  $F$ -region  $N_e^*$  around December solstice has been shown (Chartier et al., 2019)  
 270 to result from a combination of the ionospheric annual asymmetry and  $\text{O}^+$  plasma life-  
 271 times that are longer during December solstice than during June solstice.

272 Figure 2c displays distributions of  $N_e^*$  in each hemisphere for March and Septem-  
 273 ber equinox and for June and December solstice. These distributions represent all  $N_e^*$   
 274 measurements within  $\pm 15$  days around the relevant equinox or solstice, and indicate mul-  
 275 tiple aspects of polar cap  $N_e^*$  that are not represented by either median or MAD statis-  
 276 tics. We discuss these differences in terms of the two other common measures of central  
 277 tendency, the mean and mode, and in terms of standard deviation. Estimation of the  
 278 mode of  $N_e^*$ , which is a continuous variable, is non-trivial. We estimate the mode via the  
 279 procedure described by Bickel and Frühwirth (2006); this methodology yields mode es-  
 280 timates that are very similar (typically differing by less than 0.1%) to mode estimates  
 281 obtained by identifying the peak of the  $N_e^*$  distributions that are shown in Figure 2c.

282 Table 2 shows that the SH  $N_e^*$  distribution mode is greater than the NH  $N_e^*$  dis-  
 283 tribution mode only during December solstice, which is local summer in the SH. On the  
 284 other hand the SH  $N_e^*$  mean is greater than the NH  $N_e^*$  mean for all seasons except June  
 285 solstice, and the SH  $N_e^*$  standard deviation is always greater than the NH  $N_e^*$  standard



**Figure 2.** Statistics of Swarm and CHAMP height- and solar flux-adjusted geomagnetic polar cap plasma density  $N_e^*$  as a function of global season parameter  $\phi_s$  (left panels; see section 3.1) and local season parameter  $\phi_l$  (right panels) in the Northern Hemisphere (solid blue line) and Southern Hemisphere (dotted red line). The tick marks in each panel precisely indicate the relevant equinox or solstice. Panels a and d (top row) show median  $N_e^*$  in each hemisphere. Each error bar indicates the 95% confidence interval of the median within the corresponding bin, calculated as described in Text S3 of the Supporting Information. Panels b and e (middle row) show median absolute deviation (MAD) of  $N_e^*$ . Panels c and f (bottom row) show the distributions of  $N_e^*$  in each hemisphere for each season, with statistics taken from  $\pm 15$  days around the corresponding equinox or solstice. For each distribution, the thick dashed line indicates the median and the two thin dashed lines indicate the first and third quartile. To facilitate comparison of the transition from December solstice to March equinox (panel c), and from local winter to local spring (panel f), the  $N_e^*$  distributions around March equinox and local spring equinox are repeated at far right in each of these panels. The transparent histograms at the bottom of Figure 2a indicate the number of  $N_e^*$  values used to calculate the median statistic in each bin. The average number of measurements in each bin is 120,000 in the NH and 52,500 in the SH; the dashed gray line indicates  $N = 54,000$ . The total number of SH measurements is about 60% less than the total number of NH measurements (see section 2).

**Table 2.** Northern and Southern Hemisphere  $N_e^*$  statistics during each equinox and solstice.<sup>a</sup>

Season	Mode	Median	Mean	Std. Dev	Skew	Kurtosis
Mar NH	4.95	5.86	6.35	3.10	0.987	1.74
Mar SH	3.59	6.43	7.37	5.10	1.11	1.71
Jun NH	6.70	7.02	7.13	2.03	0.327	0.301
Jun SH	0.31	1.49	2.23	2.26	2.00	5.77
Sep NH	4.66	5.10	5.42	2.40	0.888	1.55
Sep SH	1.49	5.06	5.80	4.16	1.24	4.05
Dec NH	0.83	1.69	2.20	1.89	2.35	9.99
Dec SH	6.26	7.85	8.63	4.29	1.24	2.74
Spring NH	4.95	5.86	6.35	3.10	0.987	1.74
Spring SH	1.49	5.06	5.80	4.16	1.24	4.05
Summer NH	6.70	7.02	7.13	2.03	0.327	0.301
Summer SH	6.26	7.85	8.63	4.29	1.24	2.74
Fall NH	4.66	5.10	5.42	2.40	0.888	1.55
Fall SH	3.59	6.43	7.37	5.10	1.11	1.71
Winter NH	0.83	1.69	2.20	1.89	2.35	9.99
Winter SH	0.31	1.49	2.23	2.26	2.00	5.77

<sup>a</sup>Statistics in columns 2–5 are given in  $10^4 \text{ cm}^{-3}$ . Statistics in columns 6–7 are unitless.

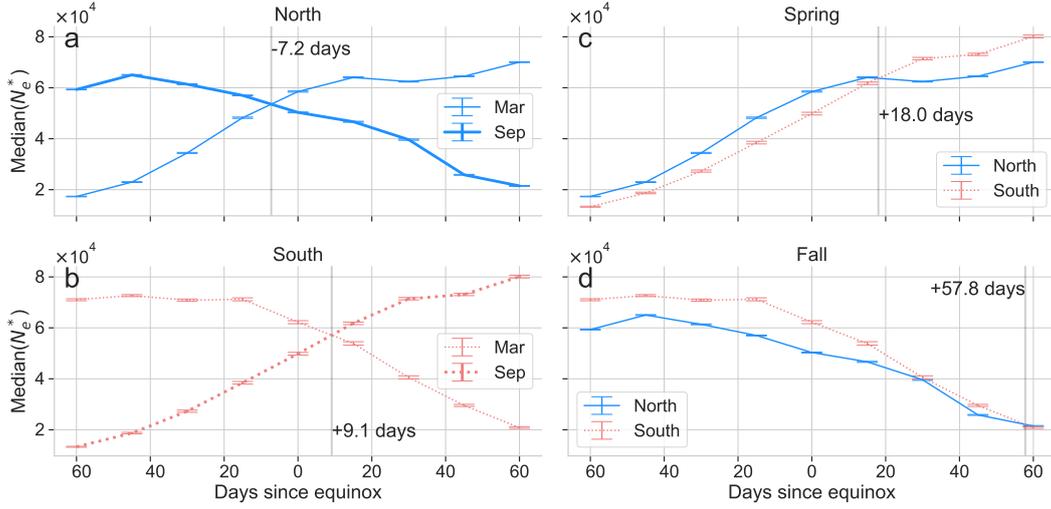
286 deviation. The NH and SH  $N_e^*$  distributions otherwise appear most similar during March  
 287 and September equinox (respectively  $\phi_s = 0$  and  $\phi_s = 2$ ) and most disparate during  
 288 June and December solstice (respectively  $\phi_s = 1$  and  $\phi_s = 3$ ), as expected. We further  
 289 discuss the relevance of these differences to cold ion outflow in section 4.

290 Figure 2d displays median  $N_e^*$  values in the NH (solid blue line) and SH (dotted  
 291 red line) geomagnetic polar caps as a function of  $\phi_l$ . From this figure it is immediately  
 292 apparent that (i) the range of median SH  $N_e^*$  values in the SH is overall larger than the  
 293 range of median NH  $N_e^*$  values, which is also visible in Figure 1a, and (ii) variation in  
 294 median SH  $N_e^*$  lags behind median NH  $N_e^*$  around local spring and fall equinoxes by sev-  
 295 eral days. We quantify this lag in the following subsection. These statistics also suggest  
 296 that the annual maximum in median NH  $N_e^*$  occurs before local summer solstice, while  
 297 the annual maximum in median SH  $N_e^*$  occurs at or perhaps slightly before local sum-  
 298 mer solstice. A secondary peak in median  $N_e^*$  between local summer solstice and local  
 299 fall equinox is also apparent in both hemispheres.

300 Figure 2e displays  $\text{MAD}(N_e^*)$  in each hemisphere as a function of  $\phi_l$ . The most im-  
 301 mediate observation is that SH  $\text{MAD}(N_e^*)$  (dotted red line) are almost always greater  
 302 than NH  $\text{MAD}(N_e^*)$  (solid blue line), except for the period between local winter and lo-  
 303 cal spring where the  $\text{MAD}(N_e^*)$  values in each hemisphere are similar. Beyond this ba-  
 304 sic difference, in both hemispheres  $\text{MAD}(N_e^*)$  peaks after local fall, reaches a global min-  
 305 imum near local winter, and either peaks (in the NH) or plateaus (in the SH) near lo-  
 306 cal spring.

307 Regarding the relative variability of  $N_e^*$ , the ratio  $\text{MAD}(N_e^*)/\text{median}(N_e^*)$  (not shown)  
 308 is larger during local winter compared to local summer, by a factor of 2 in the NH and  
 309 by a factor of 3 in the SH. The overall greater relative variability during local winter in  
 310 each hemisphere may be related to the overall higher occurrence rate of polar cap patches  
 311 during local winter that Spicher et al. (2017) and Coley and Heelis (1998) have reported.

312 Figure 2f shows  $N_e^*$  distributions in each hemisphere organized by local season. Ta-  
 313 ble 2 indicates that the SH  $N_e^*$  distribution mode is always less than the NH  $N_e^*$  distri-  
 314 bution mode, and the SH  $N_e^*$  standard deviation is always greater than the NH  $N_e^*$  stan-  
 315 dard deviation. On the other hand the SH  $N_e^*$  mean is less than the NH  $N_e^*$  mean only  
 316 during local spring solstice. The NH and SH  $N_e^*$  distributions otherwise appear most sim-  
 317 ilar during local winter solstice ( $\phi_l = 3$ ).



**Figure 3.** Median  $N_e^*$  statistics in 15-day bins relative to the number of days since equinox (Figures 3a–d). (a) Median NH  $N_e^*$  relative to March equinox (thin blue line) and September equinox (thick blue line). (b) Median SH  $N_e^*$  relative to March equinox (thin dotted red line) and September equinox (thick dotted red line). (c) Median NH  $N_e^*$  (solid blue line) and SH  $N_e^*$  (dotted red line) relative to local spring equinox. (d) Median NH  $N_e^*$  (solid blue line) and SH  $N_e^*$  (dotted red line) relative to local fall equinox. The 95% confidence intervals of the medians in 3a–d are calculated as described in Text S3 of the Supporting Information.

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### 3.2 Equinoctial Asymmetries

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We now consider the evolution of the median  $N_e^*$  in each hemisphere around equinox. Figure 3a shows median NH  $N_e^*$  values relative to March equinox (thin blue line) and September equinox (thick blue line) in 15-day bins. Crossover occurs at -7.2 days relative to equinox. Figure 3b shows median SH  $N_e^*$  values relative to March equinox (thin red dotted line) and September equinox (thick dotted red line). Crossover occurs at +9.1 days relative to equinox. Figure 3c shows NH and SH median  $N_e^*$  values relative to March and September equinox, respectively, and Figure 3d shows NH and SH median  $N_e^*$  values relative to September and March equinox, respectively. That is, Figure 3c and 3d show median  $N_e^*$  values in each hemisphere relative to local spring and fall, respectively.

Figure 3c shows that the local spring crossover between median NH  $N_e^*$  (solid blue line) and median SH  $N_e^*$  (dotted red line) occurs at +18 days relative to equinox. Figure 3d shows that the local fall crossover between median NH  $N_e^*$  (solid blue line) and median SH  $N_e^*$  (dotted red line) occurs at +58 days relative to equinox. However, it should

**Table 3.** Equinoctial asymmetries in median adjusted geomagnetic polar cap plasma density  $N_e^*$  identified in this study.

Asymmetry	(Fig)	$\Delta t$ (all sat.) days	$\Delta t$ (individ. sat.) <sup>a</sup> days
NH/SH Mar crossover delay	(1a)	4.0	[2.3, 0.4, 10.0, 6.0]
NH/SH Sep crossover <sup>b</sup>	(1a)	0.4	[1.0, -0.4, 0.4, -2.3]
NH spring/fall crossing	(3a)	-7.2	[-9.7, -7.6, -6.0, -7.3]
SH spring/fall crossing	(3b)	9.1	[8.3, 6.5, 14.2, 8.4]
NH/SH spring crossing	(3c)	18.0	[19.1, 16.7, 19.3, 17.4]
NH/SH fall crossing	(3d)	57.8 <sup>c</sup>	[26.2, 57.8, 60.0, 58.7]

<sup>a</sup>[CHAMP, Swarm A, Swarm B, Swarm C].

<sup>b</sup>Evidence for this asymmetry is weak, as  $\Delta t$  is small and exhibits spread around zero.

<sup>c</sup>As indicated in section 3.2, median  $N_e^*$  in the NH and SH are within a few percent of each other over days 30 to 60 after equinox.

332 be noted that these two lines also nearly cross at approximately +30 days. To calculate  
 333 the crossover point in each panel, we interpolate between each 15-day median with a res-  
 334 olution of 0.1 days and determine the relative day of year for which the two lines shown  
 335 in each panel are nearest each other.

## 336 4 Discussion

337 Results in the preceding section indicate the existence of several seasonal and hemi-  
 338 spheric asymmetries in the plasma density of the geomagnetic polar caps. Table 3 sum-  
 339 marizes the equinoctial asymmetries identified from Figures 1–3 on the basis of the com-  
 340 bined database of Swarm and CHAMP measurements.

341 A central purpose of this study is to determine whether the hemispheric asymme-  
 342 try in magnetospheric lobe cold plasma density reported by Haaland et al. (2017) could  
 343 be explained on the basis of plasma densities in the ionospheric polar caps. In specific,  
 344 they found that cold plasma densities in the NH lobe were overall greater than the cold  
 345 plasma densities in the SH lobe around September equinox, and speculated whether this  
 346 asymmetry was due to differences in outflow and plasma densities between NH and SH.

347 No such corresponding asymmetry in median geomagnetic polar cap  $N_e^*$  at September  
 348 equinox is apparent in Figures 1a and 2a. And while there are clear differences between  
 349 the distributions of  $N_e^*$  in each hemisphere at September equinox ( $\phi_s = 2$  in Figure 2c),  
 350 as we discuss in section 3.1, we find no evidence suggesting that NH  $N_e^*$  is systemati-  
 351 cally greater than SH  $N_e^*$  around September equinox.

352 In summary, on the basis of the Swarm and CHAMP  $N_e^*$  distributions that we have  
 353 presented, the hemispheric asymmetry in Cluster-observed cold plasma densities in the  
 354 magnetospheric lobes (Haaland et al., 2017) have no clear correspondence with plasma  
 355 densities in the geomagnetic polar caps. We believe that this is the most significant re-  
 356 sult of this study.

357 Among the possible causes of the hemispheric asymmetry in lobe cold plasma den-  
 358 sity are hemispherically asymmetric vertical transport, flux tube volume, or conductiv-  
 359 ities in the geomagnetic polar caps. Li et al. (2020) have shown, for instance, that the  
 360 strength of the Earth’s magnetic field is anti-correlated with ionospheric outflow. The  
 361 cause of this apparent discrepancy between Swarm, CHAMP, and Cluster observations  
 362 will be the subject of future work.

363 Another significant result of analysis in section 3.2 is displayed in Figure 3. In Fig-  
 364 ure 3a the crossover point of the two Northern Hemisphere (solid blue) lines occurs ap-  
 365 proximately 7 days before equinox, whereas in Figure 3b the crossover point of the two  
 366 Southern Hemisphere (dotted red) lines occurs approximately 9.1 days after equinox. Thus  
 367 the days on which the local hemisphere geomagnetic polar cap density  $N_e^*$  crossover near  
 368 local equinox occurs are hemispherically asymmetric. This asymmetry is also present when  
 369 the polar caps are defined in geocentric coordinates (not shown), and so is not the re-  
 370 sult of a particular choice of coordinate system.

371 Comparison of median  $N_e^*$  curves from each geomagnetic polar cap around local  
 372 spring (Figure 3c) and around local fall (Figure 3d) shows that the crossover points in  
 373 both hemispheres occur more than two weeks after equinox. This suggests the existence  
 374 of a seasonal “phase offset” between the two hemispheres in median  $N_e^*$  around local spring  
 375 and fall equinoxes, whereby median  $N_e^*$  in the SH geomagnetic polar cap lags median  
 376  $N_e^*$  in the NH geomagnetic polar cap by at least two weeks. The lag around local spring  
 377 equinox is even more pronounced, six weeks or more, when the polar caps are defined  
 378 in geocentric coordinates (not shown).

379 Thus the relative lag between SH and NH polar cap  $N_e^*$  around local spring equinox  
 380 is not the result of choosing a particular definition of the polar caps (i.e., geomagnetic  
 381 versus geocentric; see Table 3). On the other hand there is apparently no lag between  
 382 SH and NH geocentric polar cap median  $N_e^*$  around local fall equinox, which suggests  
 383 that the relative lag exhibited by median  $N_e^*$  in the geomagnetic polar caps is related  
 384 to the choice of coordinate system (i.e., geomagnetic instead of geocentric polar caps).

385 The different lags imply that there are at least two contributing factors to the de-  
 386 lay, which likely operate somewhat differently in the two sets of polar caps during local  
 387 spring and local fall. Here it is worth noting that the existence of a relative lag in ge-  
 388 omagnetic polar cap  $N_e^*$  around local fall equinox may be related to reported hemispheric  
 389 asymmetry in ion outflow processes and ionosphere-magnetosphere coupling that is or-  
 390 ganized by the geomagnetic field (Haaland et al., 2012; André et al., 2015; Haaland et  
 391 al., 2017).

392 To test the robustness of the asymmetries identified in Figures 1–3 and Table 1,  
 393 we have also performed the analysis separately for each of the four satellites used in this  
 394 study (not shown). The values obtained from each of these separate analyses are shown  
 395 in the rightmost column of Table 3. All of the asymmetries we have just discussed also  
 396 appear in the analyses based on measurements from individual satellites. More specif-  
 397 ically with the exception of the weak evidence for a NH/SH crossover delay at Septem-  
 398 ber equinox, the other delays are consistent between all four spacecraft albeit with slight  
 399 differences in the estimated  $\Delta t$  values.

400 We believe these separate analyses are important indicators of the robustness of  
 401 each asymmetry, since the Swarm and CHAMP satellites monitor polar cap plasma den-  
 402 sity at effectively three different altitude ranges over two different portions of a solar cy-  
 403 cle, with two different and independent types of Langmuir probe instruments and three  
 404 different orbits.

## 405 5 Summary

406 Using 15 years of plasma density measurements made by the original three Swarm  
 407 satellites and the CHAMP satellite, we have identified equinoctial asymmetries in  $F$ -region  
 408 ionospheric plasma density in the geomagnetic polar caps. In particular:

- 409 1. Haaland et al. (2017) have reported overall lower cold plasma densities in the SH  
 410 magnetospheric lobe relative to the NH magnetospheric lobe around September  
 411 equinox; they conjecture that the difference may be related to available ionospheric  
 412 plasma in the polar cap. We find no evidence supporting this conjecture.
- 413 2. We present evidence that SH polar cap plasma density lags behind NH polar cap  
 414 plasma density by at least two weeks around March and September equinox.
- 415 3. For every season the SH distribution of  $F$ -region polar cap plasma density is spread  
 416 over a wider range of values than the NH distribution. The mode of the SH dis-  
 417 tribution is also generally lower than the mode of the NH distribution.

## 418 **Appendix A Correction and Adjustment of $N_e$**

419 Here we provide some additional details on the procedure for obtaining the final  
 420 height- and solar flux-adjusted density measurements that are denoted  $N_e^*$  throughout  
 421 the manuscript. A detailed description of this procedure and relevant figures are located  
 422 in Text S2 and Figures S2–S3 of the Supporting Information.

423 After applying the Lomidze et al. (2018) in-flight calibrations to Swarm plasma den-  
 424 sity measurements, we additionally account for differences in altitude and solar activ-  
 425 ity via (i) application of an empirically derived scale height to  $N_e$  measurements that  
 426 “maps”  $N_e$  to a common geodetic altitude of 500 km, and (ii) application of an empir-  
 427 ically derived correction factor that accounts for the variation of  $N_e$  measurements with  
 428 10.7-cm solar radio flux (otherwise known as the  $F10.7$  index).

429 As pointed out in section 2 the CHAMP satellite and the three Swarm satellites  
 430 cover different altitude ranges, and thus different portions of the  $F$  region. The altitude  
 431 range covered by the CHAMP satellite (315–455 km) is the lowest of all four satellites,  
 432 while the altitude range covered by Swarm B (500–545 km) is mostly above those of the  
 433 other satellites.

434 From 380 conjunctions between Swarm B and either Swarm A or Swarm C for which  
 435 Swarm LP data is currently available (Dec 2013 through Feb 2020) we derive the Ver-  
 436 tical Scale Height  $VSH \equiv dh/(d \ln N_e)$  (e.g., Hu et al., 2019). We use “robust regres-  
 437 sion” (e.g., Huber (1973); Holland and Welsch (1977)) to estimate VSH from the ratio  
 438 of plasma density measurements during the 380 identified conjunctions (Figure S2c in  
 439 Supporting Information). From this regression we obtain VSH values of 205 km on the

440 dayside ( $6 \leq \text{MLT} < 18$ ) and 167 km on the nightside ( $\text{MLT} < 6$  and  $\text{MLT} \geq 18$ ).  
 441 These scale heights are within the range of typical estimates at geodetic altitudes of 350–  
 442 500 km (e.g., Figure 2 in Hu et al. (2019) and Figure 1B in Stankov and Jakowski (2006)).

443 To each  $N_e$  measurement we then apply a scaling factor

$$444 \quad N_{e,h_0} = N_e \exp[(h - h_0) / \text{VSH}], \quad (\text{A1})$$

445 where  $h$  is the altitude at which the measurement is made. We arbitrarily select a ref-  
 446 erence geodetic altitude  $h_0 = 500$  km. This scaling decreases the value of  $N_e$  for mea-  
 447 surements made below  $h_0$  and increases the value of  $N_e$  for measurements made above  
 448  $h_0$ .

449 In addition to variation with altitude polar cap  $N_e$  also varies approximately lin-  
 450 early with  $\langle F10.7 \rangle_{27}$ , an average of the  $F10.7$  index during the preceding 27 days. We  
 451 use  $\langle F10.7 \rangle_{27}$ , as a proxy for solar EUV intensity. Another common choice for averag-  
 452 ing the  $F10.7$  index is a centered 81-day window (e.g., L. Liu & Chen, 2009; Schunk &  
 453 Nagy, 2009). We have elected to use  $\langle F10.7 \rangle_{27}$  instead, since we find that the RMS er-  
 454 ror between this quantity and  $N_{e,h_0}$  is slightly ( $\sim 5\%$ ) lower than the RMS error between  
 455 an 81-day centered average of the  $F10.7$  index and  $N_{e,h_0}$ .

456 We use robust regression to fit  $N_{e,h_0}$  and  $\langle F10.7 \rangle_{27}$  values with a model of the form

$$457 \quad N_{e,h_0} = A \langle F10.7 \rangle_{27} - B = N (a \langle F10.7 \rangle_{27} - 1). \quad (\text{A2})$$

458 The resulting best-fit model parameters are  $a = 0.02564$  and  $N = 46,780 \text{ cm}^{-3}$ . We  
 459 apply the portion of the model in Equation (A2) that is dependent on  $\langle F10.7 \rangle_{27}$ , namely  
 460 the parameter  $a$ , to each  $N_{e,h_0}$  value to finally obtain the height- and solar flux-adjusted  
 461 density

$$462 \quad N_e^* = N_{e,h_0} \frac{80a - 1}{a \langle F10.7 \rangle_{27} - 1}. \quad (\text{A3})$$

463 The numerator in Equation (A3) scales the final adjusted density  $N_e$  to a nominal so-  
 464 lar flux level of  $\langle F10.7 \rangle_{27} = 80$ . (Final adjusted densities are shown in Figure S3b of  
 465 the Supporting Information.)

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470 The Level 2 CHAMP PLP dataset and Level 1B Swarm LP dataset are publically  
 471 accessible via <ftp://isdctftp.gfz-potsdam.de> and <https://swarm-diss.eo.esa.int/>,  
 472 respectively. The  $F_{10.7}$  index is available via the NASA OMNI database ([https://omniweb](https://omniweb.gsfc.nasa.gov/form/dx1.html)  
 473 [.gsfc.nasa.gov/form/dx1.html](https://omniweb.gsfc.nasa.gov/form/dx1.html)). The database of adjusted geomagnetic polar cap den-  
 474 sity measurements, denoted  $N_e^*$  in the manuscript, is also publically available (Hatch et  
 475 al., 2020) (<https://doi.org/10.5281/zenodo.3813145>).

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