

A Multivariate Conditional Probability Framework to Estimate Compound Sub-daily Rainfall Extremes Preconditioned by Humid Heatwaves

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Poulomi Ganguli¹, Bruno Merz²

¹Indian Institute of Technology Kharagpur, India

²GFZ German Research Centre for Geosciences, Potsdam, Germany

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WISER PG/47/2022-23/514



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Heatwaves are becoming near norm in Summer & Spring Seasons in India

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World ▾ Business ▾ Markets ▾ Sustainability ▾ Legal ▾ Breakingviews Technology ▾ Inves

India

India to get heat waves this year after hottest February on record

By Rajendra Jadhav

February 28, 2023 7:29 PM GMT+5:30 · Updated 8 months ago



[Reuters, 2023](#)

Summer heat stress impacts human health, energy production; extended warm spell leads to changes in precipitation.

Severe Summer heatwaves in May 1998 resulted in over 2500 fatalities ([GSDMA, 2023](#))

Winter heat stress impacts grain filling, causes early senescence, reducing crop yields ... especially for wheat

[IMD Statement on Climate, 2022](#)

Extreme humid heat in South Asia in April 2023, largely driven by climate change, detrimental to vulnerable and disadvantaged communities

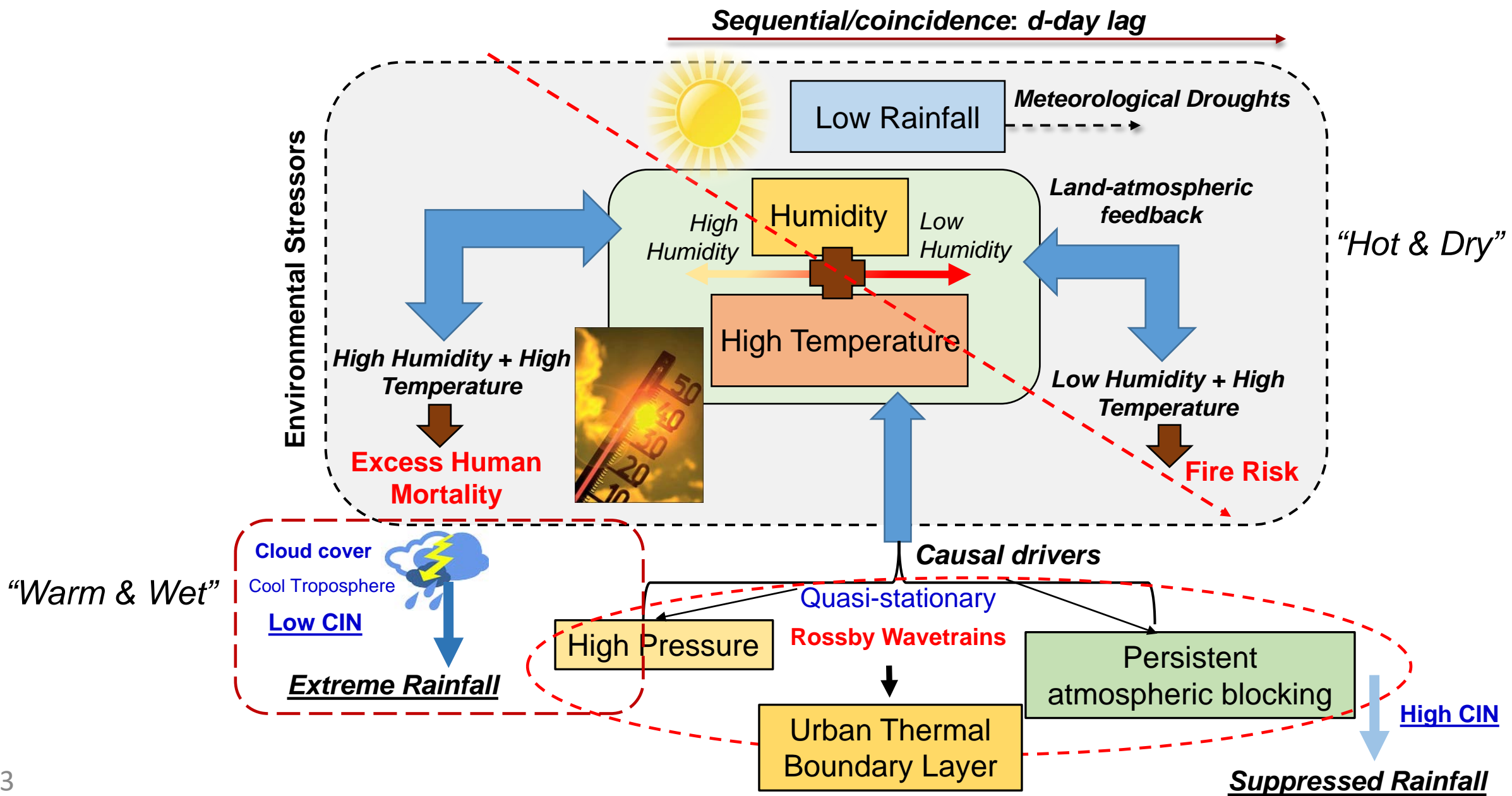
17 May, 2023

HEATWAVE
ASIA

For the last two weeks of April 2023, many parts of Bangladesh, India, Thailand and Lao PDR experienced record high temperatures.

In Bangladesh, Dhaka observed the highest maximum temperature recorded in decades of 40.6°C on 15th April. In India, several northern and eastern cities recorded maximum temperatures above 44°C on 18th of April. Thailand recorded its highest ever temperature of 45.4°C on 15th April in the city of Tak.

[World weather Attribution, 2023](#)

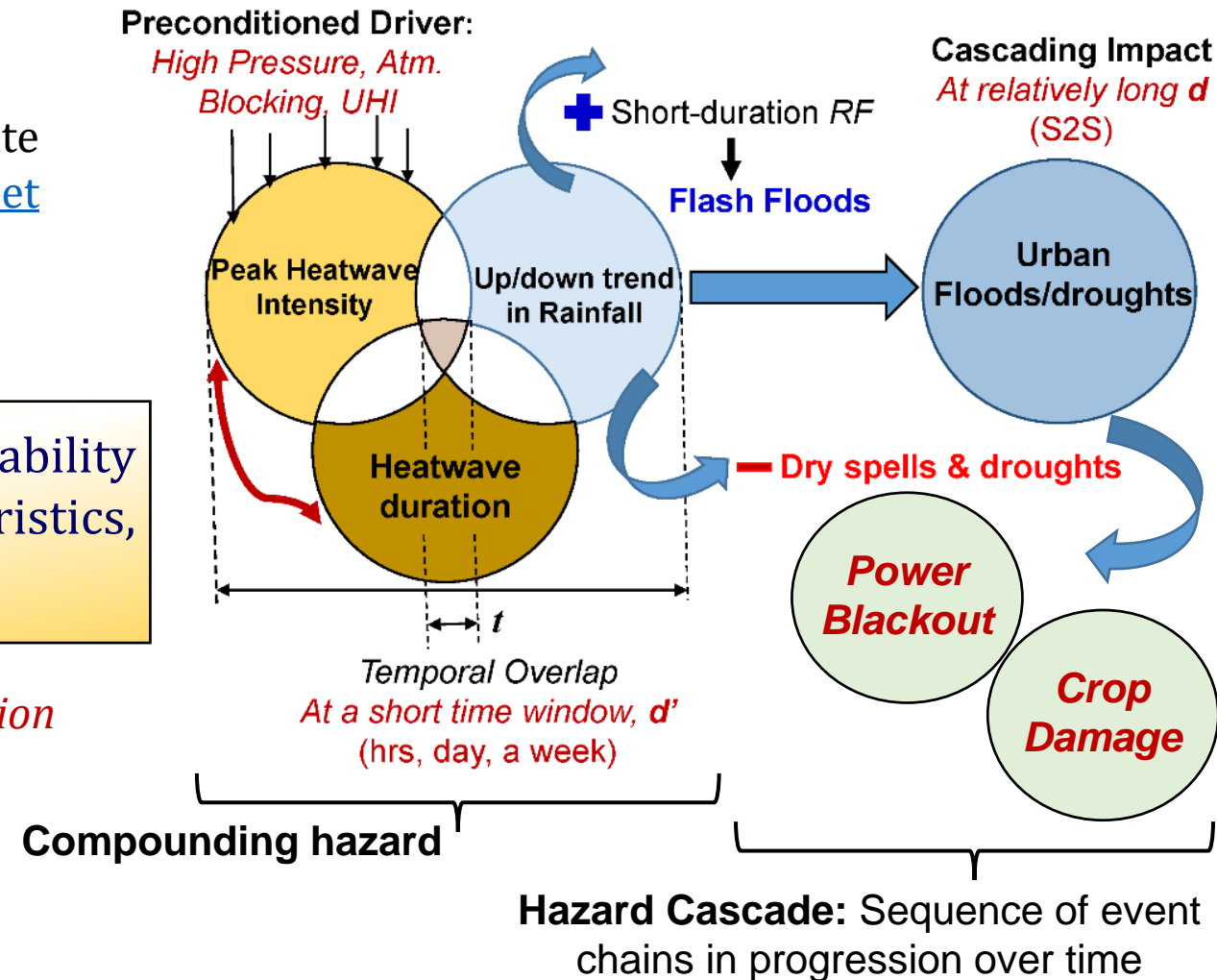


- Studies have implemented different definition of compound 'warm-wet/dry' events considering different datasets with varying spatiotemporal resolutions.
- Assessments have mostly focused on bivariate framework at global ([Gu et al. 2022](#)) & regional ([Chen et al. 2021](#); [Kumar et al. 2022](#)) domain.

✓ Any approach to quantify exceedance rainfall probability conditioned on preceding humid heatwave characteristics, duration and heatwave amplitude/peak intensity?

Lengthening of dry spells intensify heat stress → *duration* is a crucial metrics ([He et al., 2022](#))

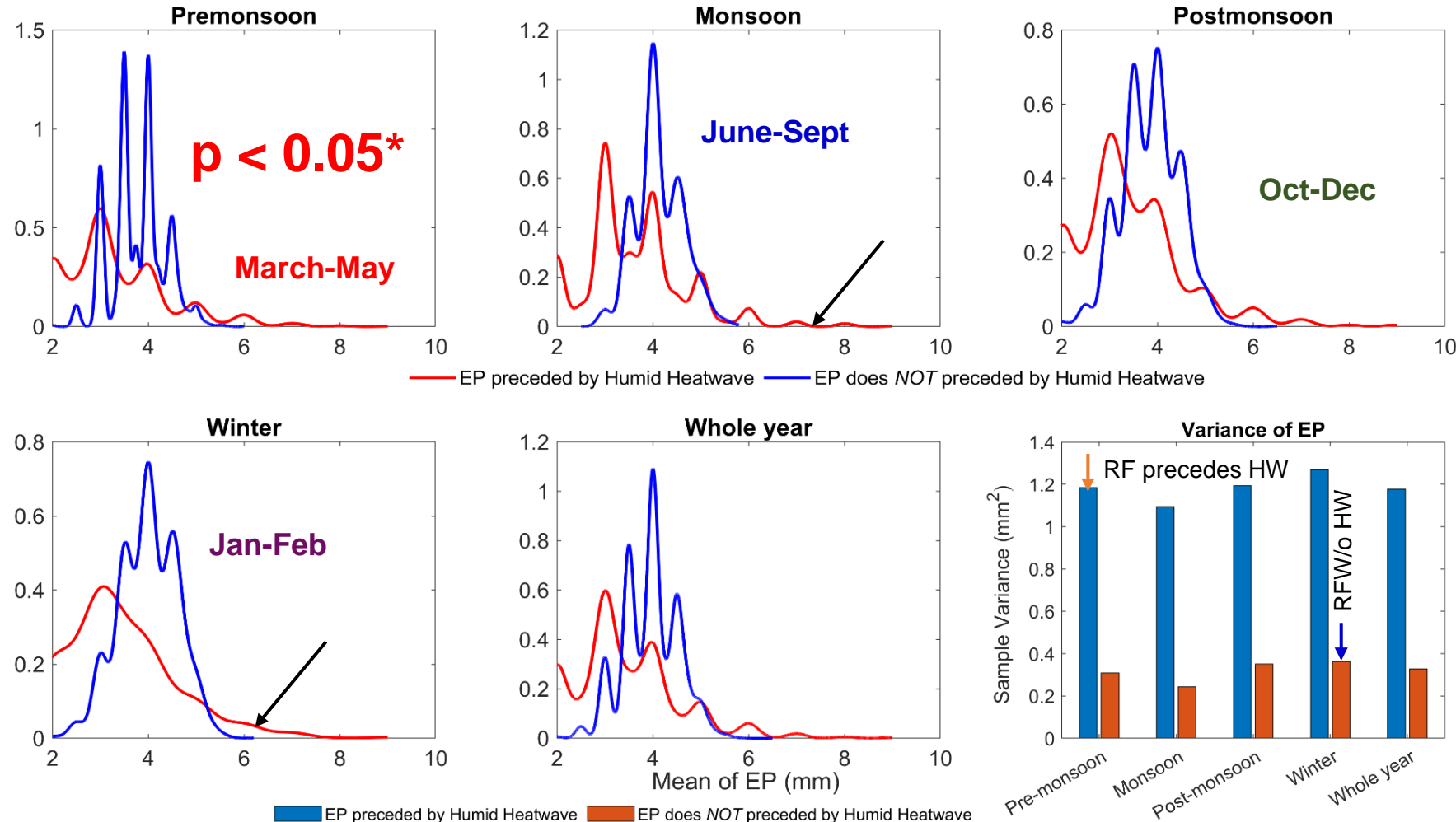
Compound & Cascade Hazards from Heatwave & Rainfall



- Rain events preceded by humid heatwave episodes show a heavier tail with multiple peaks for larger magnitudes.
 - The variability of rain preceded by heatwaves show larger variance.

▪ **Humid heatwave** is detected when daily maximum T_w (from 3-hourly observation) *exceeds temperature thre* ($> 90^{\text{th}}$ percentile) > 3 days or longer.

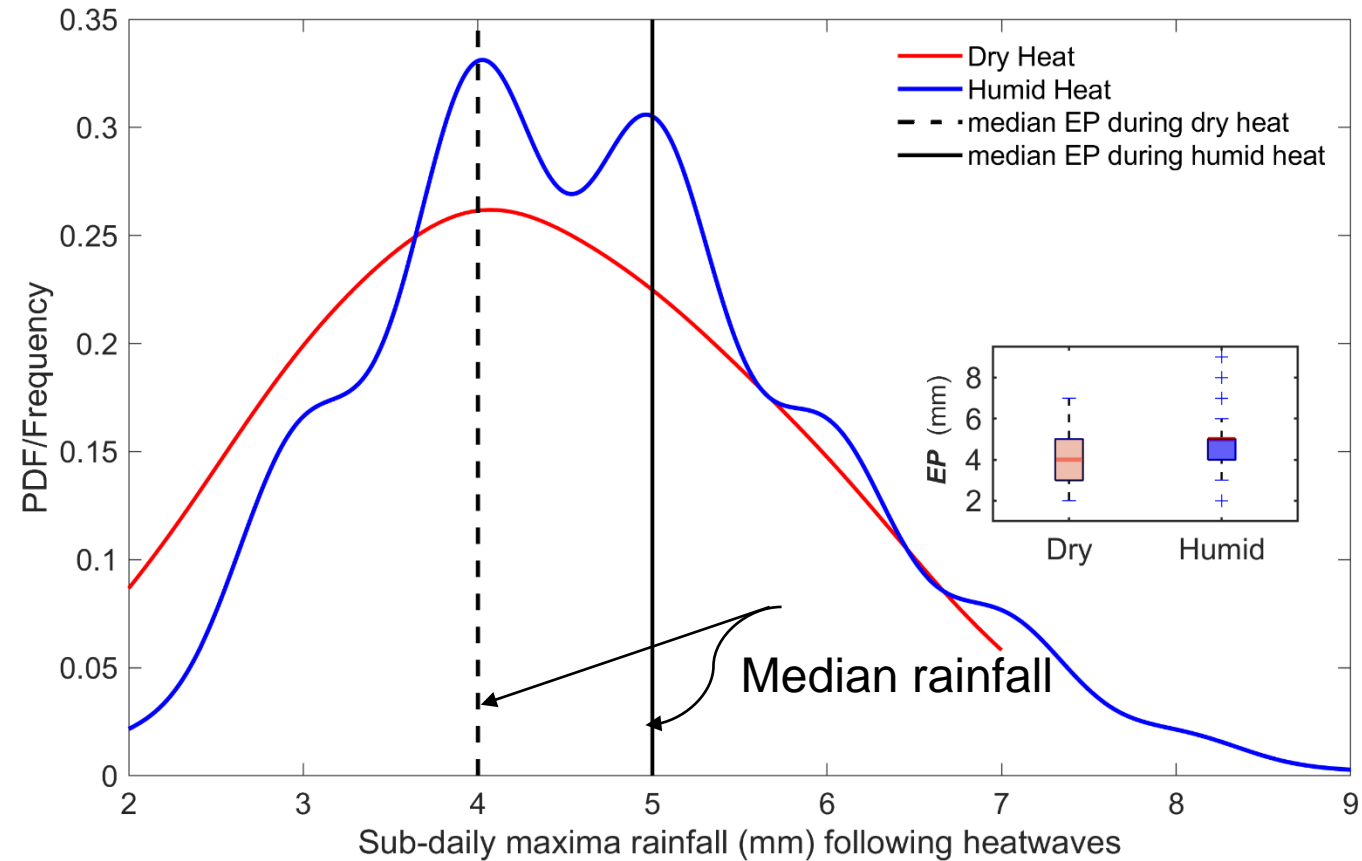
▪ EP is the sub-daily maximum rainfall, which is $> 50^{\text{th}}$ percentile of rainfall sampled at a 3-hourly scale.



***Two-sample KS Test**

Sub-daily Meteorological records:
[IMD Data Supply Portal](#) (3:00–12:00 hr UTC)

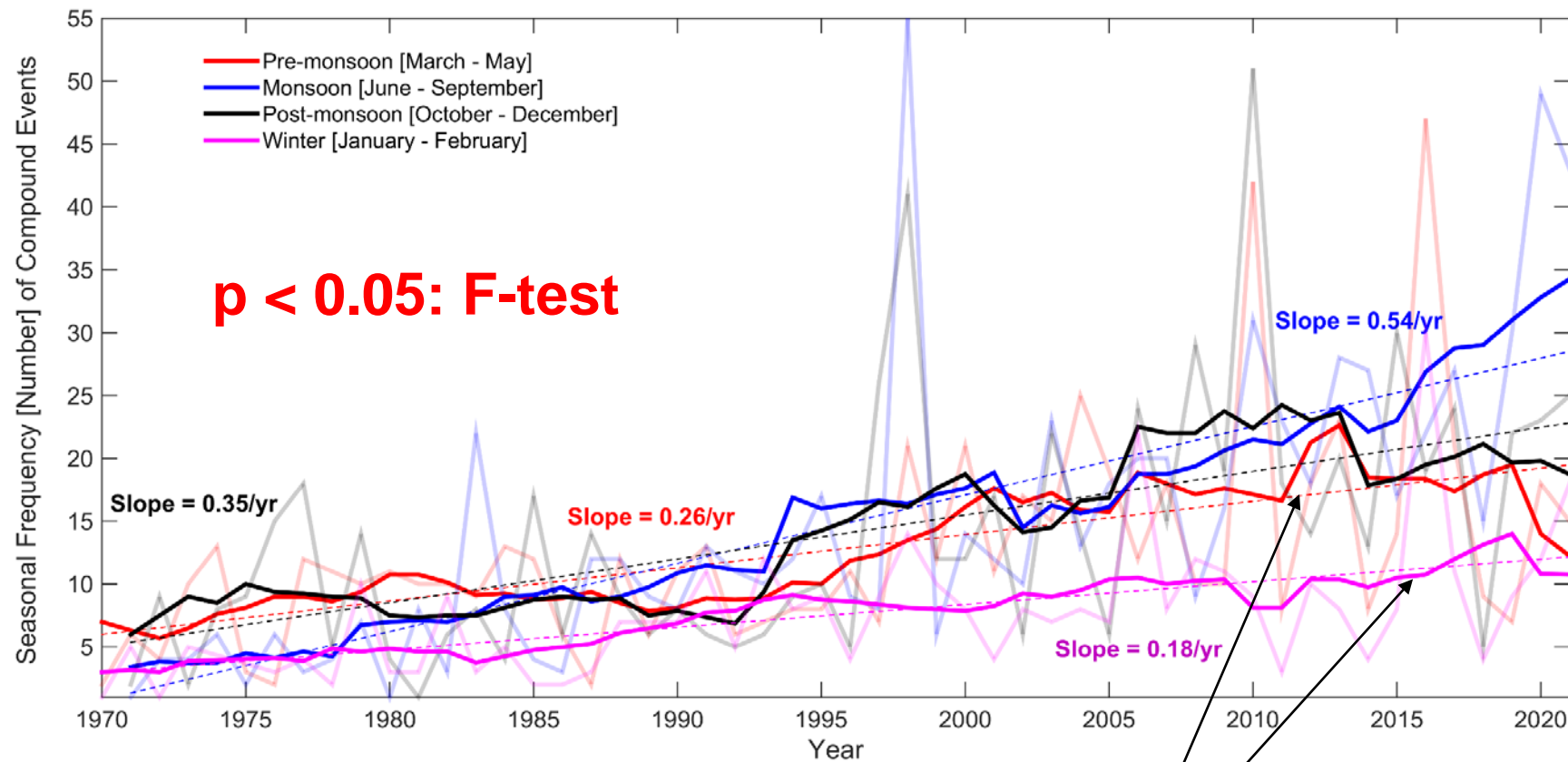
- Dry heat: $T_w < 33\%$ Rh
- Humid heat: $T_w > 67\%$ Rh



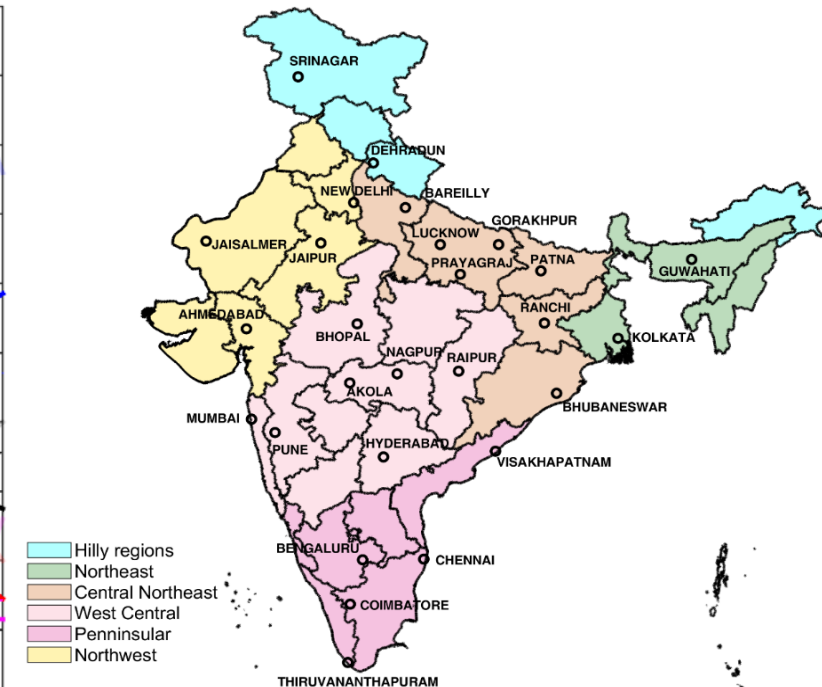
$p < 0.05$: Two-sample KS Test

Increasing Trends in Compound Warm-Wet Compound Extremes across Seasons

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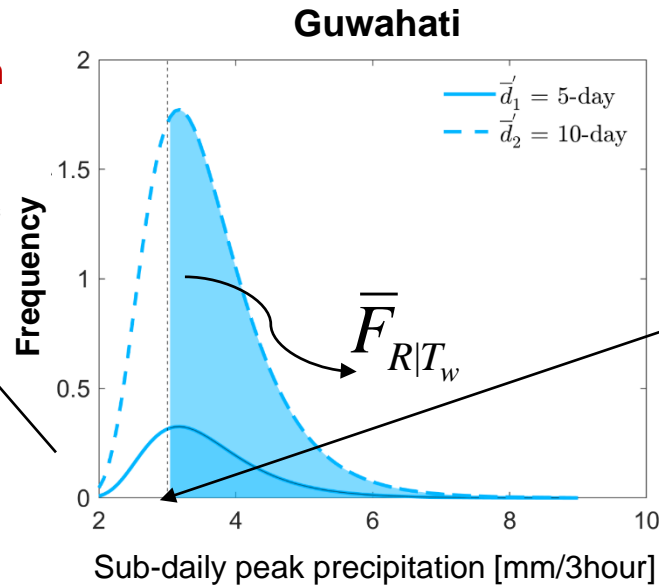
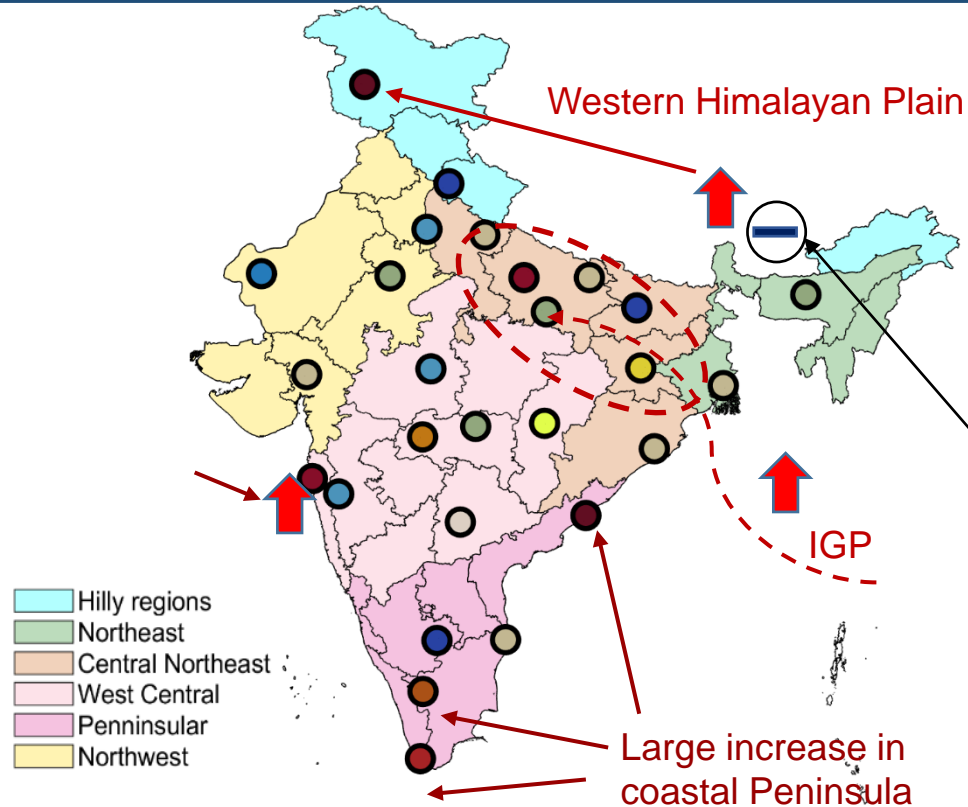


Smoothed using 8-year moving average



Compound “Warm-Wet” events are detected when humid heat stress precedes peak rainfall of a heavy rainfall event ($> 50^{\text{th}}$ percentile threshold) within $t \in [-1, 7]$ window.

More Land Areas Show Decline in Sub-daily Peak rainfall, while a Localized Increase is Apparent



$$\bar{F}_{R|T_w} (R > r | T_w = 10 - yr, d')$$

$$= 1 - F_{R|T_w} (R \leq r | T_w = 10 - yr)$$

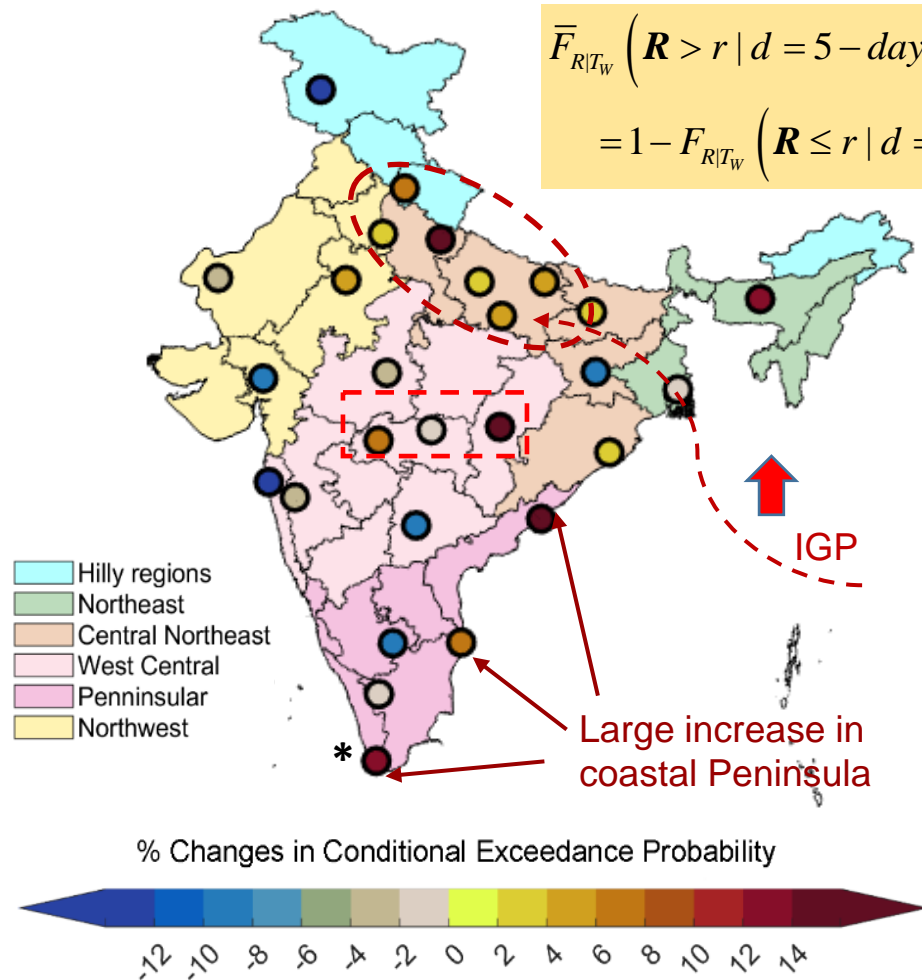
Trivariate copula-based framework

$$C(u_1, \dots, u_d; \mathcal{G}, \Sigma) = t_{\mathcal{G}, \Sigma}^d \left(t_{\mathcal{G}}^{-1}(u_1), \dots, t_{\mathcal{G}}^{-1}(u_d) \right), \quad \mathcal{G} \in (2, 10]$$

$$t_{\mathcal{G}, \Sigma}^d(x) = \int_{-\infty}^x \frac{\Gamma((\mathcal{G} + d)/2)}{\Gamma(\mathcal{G}/2)(\mathcal{G}\pi)^{d/2} \sqrt{|\Sigma|}} \left(1 + y^T \Sigma^{-1} y / \mathcal{G} \right)^{-(\mathcal{G} + d)/2} dy$$

With **increase** in durations from **5-day** to **10-day** & with $T_w = 10\text{-year peak heatwave amplitude}$, $\sim 67\%$ sites show **decline** in peak precipitation

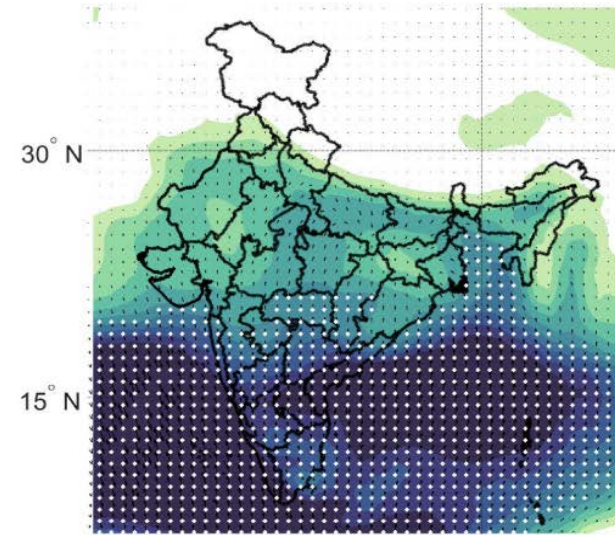
More Land Areas Show Increase in Sub-daily Peak Rainfall, with Increase in Peak Heatwave Intensity



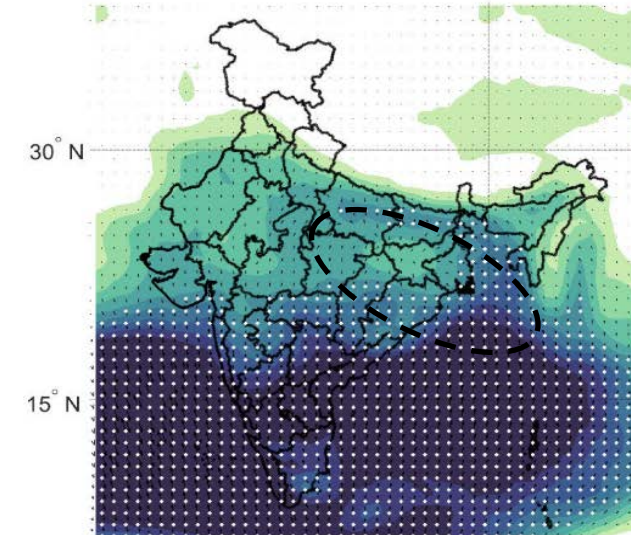
With increase in $T_w = 2$ -year to $T_w = 50$ -year peak heatwave amplitude for 5-day long events, > 50% sites show increase in peak precipitation

$$\bar{F}_{R|T_w} \left(R > r \mid d = 5 - \text{day}, T_w' \right) = 1 - F_{R|T_w} \left(R \leq r \mid d = 5 - \text{day}, T_w' \right)$$

Day of Peak Heatwave
Amplitude



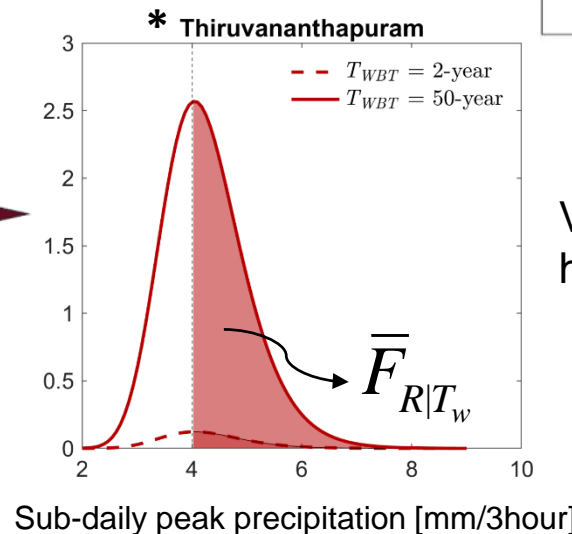
Day of Sub-daily Rainfall
Extremes



VIMT Changes (monsoon – All seasons) [in $\text{kg m}^{-1} \text{s}^{-1}$]



* $\geq 100 \text{ kg m}^{-1} \text{s}^{-1}$ with $p < 0.01$

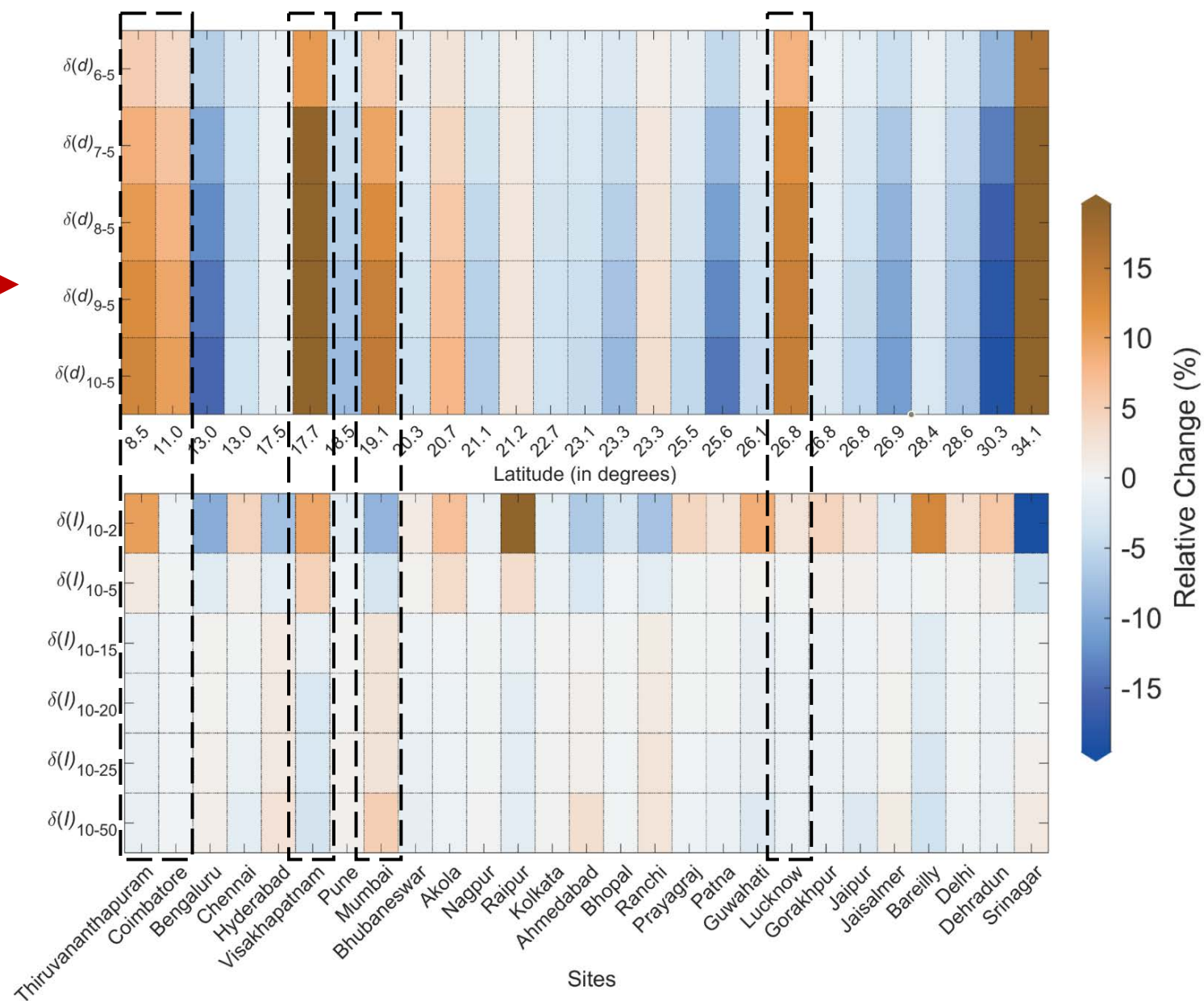


Vertical Integrated Moisture Transport (VIMT) during heatwave and following peak precipitation days

$$\frac{\bar{F}_{R>r|d',T_w=10-yr} - \bar{F}_{R>r|d,T_w=10-yr}}{\bar{F}_{R>r|d',T_w=10-yr}} \times 100$$



$$\frac{\bar{F}_{R>r|d=5-day,T'_w} - \bar{F}_{R>r|d=5-day,T_w}}{\bar{F}_{R>r|d=5-day,T'_w}} \times 100$$



- Robust **upward trend** in **frequency of warm-wet compound events** across [all seasons](#).
- Their Extremes show **Contrasting space-time trends**
 - ↓
 - Sub-daily rainfall maximum shows notable changes in exceedance probability in response to changing humid heatwave properties.
 - ↪
 - Rainfall extremes increase with an increase in preceding heatwave intensity over 50% of sites
 - Rainfall peaks decrease with increasing heatwave durations over 60% of sites.
- The decrease in rainfall peaks is possibly due to moisture limitations — **heat-induced suppression** of rainfall over *land* & **storm-induced temperature** variations over ocean ([Fowler et al., 2021](#); [Sun and Wang, 2022](#)).

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