

Shallow Slow Earthquake Episodes Near the Trench Axis Off Costa Rica

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Key Points:

- Shallow very low frequency earthquakes (VLFs) and tremors are detected off Costa Rica near the Middle America Trench
- Distribution of VLFs and tremors is spatially correlated with slow slip events
- Scaled energy of shallow slow earthquakes off Costa Rica is 10^{-9} – 10^{-8} , which is similar to those in Nankai

18 **Abstract**

19 Slow earthquakes are mainly distributed in regions surrounding seismogenic zones
20 along the plate boundaries of subduction zones. In the Central American subduction zone, large
21 regular interplate earthquakes with magnitudes of 7–8 occur repeatedly around the Nicoya
22 Peninsula, in Costa Rica, and a tsunami earthquake occurred off Nicaragua, just north of Costa
23 Rica, in 1992. To clarify the spatial distribution of various slip behaviors at the plate boundary, we
24 detected and located very low frequency earthquakes (VLFs) around the Nicoya Peninsula using
25 a grid-search matched-filter technique with synthetic templates based on a regional three-
26 dimensional model. VLFs were active in September 2004 and August 2005, mainly near the
27 trench axis, updip of the seismogenic zone. The distribution of VLFs overlapped with large slip
28 areas of slow slip events. Low frequency tremor signals were also found in high-frequency
29 seismogram envelopes within the same time windows as detected VLFs; thus, we also
30 investigated the energy rates of tremors accompanied by VLFs. The range of scaled energy,
31 which is the ratio of the seismic energy rate of a tremor to the seismic moment rate of
32 accompanying VLF and related to the rupture process of seismic phenomena, was 10^{-9} – 10^{-8} . The
33 along-dip separation of shallow slow and large earthquakes and the range of the scaled energy off
34 Costa Rica are similar to those in shallow slow earthquakes in Nankai, which shares a similar
35 thermal structure along the shallow plate boundary.

36 **Plain language summary**

37 Slow earthquakes generally occur on the plate boundaries of subduction zones. We
38 detected and located very low frequency earthquakes (VLFs), which are a type of slow
39 earthquake, off Costa Rica. The VLFs occurred at a depth range of 6–10 km, and their spatial
40 distribution is correlated with slow slip events, another type of slow earthquakes. The spatial
41 separation of slow and large regular earthquakes is common to the Nankai subduction zone. Low
42 frequency tremor signals, which are also classified as slow earthquakes, were also found in
43 seismograms at higher frequencies within the same time windows of detected VLFs. We also
44 estimated the ratio of energy rates of tremors to moment rates of VLFs, which relates to the
45 rupture process of seismic phenomena. The ratio is 10^{-9} – 10^{-8} off Costa Rica, similar to that in
46 shallow slow earthquakes in the Nankai subduction zone.

47 **1. Introduction**

48 Slow earthquakes are mainly observed in regions surrounding seismogenic zones, which
49 are the areas that rupture in large regular earthquakes, along the plate boundaries of subduction
50 zones (e.g., Obara & Kato, 2016) or strike-slip faults (e.g., Nadeau & Dolenc, 2005; Wang &
51 Barbot, 2020). Various types of slow earthquakes, such as low frequency tremors (tectonic
52 tremors; e.g., Obara, 2002), low frequency earthquakes (LFs; e.g., Shelly et al., 2006), very low
53 frequency earthquakes (VLFs; e.g., Obara & Ito, 2005), and slow slip events (SSEs; e.g., Dragert
54 et al., 2001) have been observed in many subduction zones. Although there are areas where some
55 types of slow earthquakes are not spatiotemporally correspondent (Hutchison, 2020; Hutchison &
56 Ghosh, 2016, 2019), they often correlate spatiotemporally, which is termed episodic tremor and
57 slip (ETS). ETSs were observed in deep Cascadia (e.g., Ghosh et al., 2015; Rogers & Dragert,
58 2003) and deep Nankai (e.g., Ito et al., 2007; Obara, 2011), for example. Recently, in the Nankai
59 subduction zone, pore fluid pressure changes have been observed during tremor and VLF
60 activities and are considered to reflect shallow SSEs by offshore borehole observations (Araki et

61 al., 2017; Nakano et al., 2018). The hypocenters and focal mechanisms of slow earthquakes are
62 generally consistent with shear slip on the plate boundaries. VLFE episodes and SSEs occur in
63 almost identical source regions and their temporal changes of moment release are similar during
64 an ETS, therefore VLFE episodes are considered as proxies for SSEs (Hutchison & Ghosh, 2019;
65 Ito et al., 2007; Nakano et al., 2018; Yokota & Ishikawa, 2020). In summary, the distribution of
66 slow earthquakes is related to large earthquake slip areas, interplate coupling, or fluid distribution
67 (e.g., Baba et al., 2020b; Ghosh et al., 2015; Obara & Kato, 2016).

68 In the Central American subduction zone, the Cocos plate subducts beneath the Caribbean
69 plate at the Middle America Trench at a rate of approximately 80 mm/year (Figure 1b; referred
70 from NUVEL1A; DeMets et al., 1994). In this subduction zone, large thrust-type earthquakes with
71 a moment magnitude (M_w) of 7–8 occur with a recurrence interval of tens of years around the
72 Nicoya Peninsula, in Costa Rica (light blue areas in Figure 1a; Protti, 1995; Yue et al., 2013). The
73 coseismic slip areas of these large earthquakes are distributed at a depth range of 10–35 km beneath
74 the peninsula and off the coast. The latest large earthquake with M_w of 7.6 occurred on 5
75 September, 2012 (green contour lines in Figure 1a; Yue et al., 2013). In the vicinity, a tsunami
76 earthquake with M_w of 7.6 also occurred off Nicaragua, just north of Costa Rica, on 2 September,
77 1992 (dark blue area in Figure 1a; Satake, 1994).

78 In addition to large regular and tsunami earthquakes, slow earthquakes also occur around
79 the Nicoya Peninsula. The Global Navigation Satellite System data revealed that SSEs with M_w
80 of 6.6–7.2 occur at intervals of 21.7 ± 2.6 months (Jiang et al., 2012; Xie et al., 2020). The large
81 slip area of the SSE in 2007 was separated into downdip and updip areas by the seismogenic slip
82 area (Jiang et al., 2012, 2017; Outerbridge et al., 2010). The spatiotemporal change in relation to
83 the 2012 M_w 7.6 earthquake was investigated by previous studies (Dixon et al., 2014; Voss et al.,
84 2017), and an SSE preceded the 2012 M_w 7.6 earthquake (Voss et al., 2018) in the almost same
85 area of the 2007 SSE, similar to both the slow slip before the 2011 Tohoku earthquake in Japan
86 (Ito et al., 2013; Kato et al., 2012) and the slow slip before the 2014 Iquique earthquake in Chile
87 (Kato & Nakagawa, 2014; Ruiz et al., 2017).

88 By using high-frequency (>1 Hz) seismograms, Brown et al. (2009) and Outerbridge et al.
89 (2010) located LFEs and tremors in 2007, respectively (Figure 1a). The tremors and LFEs were
90 located in almost the same area, downdip of the seismogenic zone. Although tremors and LFEs
91 were temporally correlated with the SSE, the location of tremors and LFEs were separated from
92 the large slip area of the 2007 SSE. On the other hand, Walter et al. (2011) located many tremors
93 in the offshore region from 2007 to 2009. Walter et al. (2013) also found that VLFs appeared in
94 seismograms in a frequency range of 0.02–0.05 Hz and were temporally correlated with tremors
95 in the time period of the 2008 SSE. Based on beamforming analysis, they estimated the propagation
96 direction and the propagation speed of VLFE signals and suggested that VLFs also occurred in
97 offshore areas. Due to the limitations of a conventional analysis, however, epicenters of VLFs in
98 offshore areas were not located. Therefore, the detailed spatial distribution of VLFs off Costa
99 Rica is still not well understood.

100 The spatial variation of slow and large regular earthquakes can reflect the spatial
101 heterogeneity of the frictional conditions on the plate boundary (e.g., Baba et al., 2020b). To clarify
102 the spatial relationship between slow and large regular earthquake distribution around the Nicoya
103 Peninsula, an accurate spatial distribution of VLFs is needed. Thus, we detected VLFs around
104 the Nicoya Peninsula using a temporary broadband seismic network from August 2004 to January
105 2006 because signals of VLFs are less attenuated than those of tremors and propagate longer

106 distances. The method is based on the matched-filter technique. Template waveforms from
107 possible VLFE locations were evaluated by numerical simulations of seismic wave propagation
108 using a regional three-dimensional (3D) velocity structure model. In addition, scaled energy is an
109 informative parameter for the rupture process of seismic phenomena (Kanamori & Rivera, 2006).
110 Although scaled energies of slow earthquakes around Japan were well investigated by previous
111 studies (e.g., Ide & Yabe, 2014; Yabe et al., 2019; 2021), those in Costa Rica was not estimated.
112 Therefore, we also estimated the seismic energy rate functions of tremors accompanied by VLFES
113 by using high frequency (2–8 Hz) seismograms to evaluate the scaled energy of slow earthquakes
114 around the Nicoya Peninsula.

115 **2. VLFE analysis**

116 **2.1. Data and method**

117 **2.1.1. Data**

118 We used waveforms of a temporary seismic network, Tomography Under Costa Rica and
119 Nicaragua (TUCAN; Abers & Fischer, 2003), recorded from August 2004 to January 2006. There
120 were 49 broadband seismic stations in four lines (Figure 1b). For the VLFE analysis, we used 14
121 stations near the Nicoya Peninsula in Costa Rica (shown in Figure 1a), because signals of VLFES
122 are relatively clear in these 14 stations and using all stations causes higher computational cost for
123 synthetic calculations. After removing instrumental responses, the seismograms for VLFE
124 detection were resampled at one sample per second. We applied a bandpass filter in the frequency
125 range of 0.02–0.05 Hz (e.g., Ghosh et al., 2015; Ito et al., 2009; Takemura et al., 2019), because
126 this frequency band is less affected by microseismic noises (e.g., Hasselmann, 1963; Kaneko et al.,
127 2018). We verified that the large amplitude surface waves are generally matched well between
128 observed and synthetic waveforms in a higher frequency range (Figure S1; 0.02-0.06 Hz).

129 **2.1.2. Matched-filter technique**

130 The detection procedure used for VLFES is similar to that used in our previous study (Baba
131 et al., 2020a). The horizontal-component seismograms of many stations were noisy; therefore, it
132 is difficult to use horizontal-component seismograms for the location of VLFES (Figure S2). Thus,
133 we used only the vertical-component seismograms for the VLFE analysis although it is usual to
134 analyze VLFES by using three-component seismograms. We placed 175 virtual source grids on
135 the Cocos Plate boundary at a uniform interval of 0.1° (Figure 2a) and computed synthetic
136 waveforms from these source grids to the stations in Costa Rica using an open-source seismic
137 wave propagation code (OpenSWPC; Maeda et al., 2017). We used a three-dimensional velocity
138 structure model constructed by combining CRUST 1.0 (Laske et al., 2013), Slab2 (Hayes et al.,
139 2018), and ETOPO1 (Amante & Eakins, 2009), setting the minimum *S*-wave velocity in the solid
140 columns to 1.0 km/s. We adopted the values of a mean oceanic slab structure (Christensen &
141 Salisbury, 1975) for the physical parameters of the subducting slab (Table S1). For the physical
142 parameters of the other layers except for the slab, we used the values of CRUST 1.0, and the default
143 parameter set of OpenSWPC. The cross-section of the structure model is shown in Figure S3. The
144 model covered the region enclosed by the red line (Figure 1b), which was discretized by a uniform
145 grid interval of 0.2 km. The assumed VLFE moment rate function was a Küpper wavelet with a
146 source duration of 15 s and an M_w of 4.0 (Figure 4 of Maeda et al., 2017). Since focal mechanisms
147 of VLFES are shown to be consistent with shear slip on the plate boundaries in previous studies
148 (Cascadia: Ghosh et al., 2015; Nankai: Ito et al., 2009; Nakano et al., 2018; Sugioka et al., 2012;
149 Takemura et al., 2019), the focal mechanism at each source grid was assumed to be consistent with

150 the geometry of the plate boundary of Slab2 and the plate motion model, NUVEL-1A (DeMets et
 151 al., 1994). The time window of each template was set to 150 s from the event origin time. Hereafter,
 152 we simply refer to these synthetic waveforms as template waveforms. Examples of template
 153 waveforms at updip and downdip source grids are shown in Figures 2b and 2c, respectively. The
 154 signal first arrives at MANS and the variation of amplitudes is small for the updip source, whereas
 155 signals first arriving at FINA exhibit amplitudes in or near the Nicoya Peninsula that are much
 156 larger than in other areas for the downdip source.

157 We then calculated cross-correlation coefficients (CCs) between the filtered template
 158 waveforms and observed seismograms every 1 s. We selected events with station-averaged
 159 coefficients larger than a threshold defined as 9.5 times the median absolute deviation (MAD) of
 160 the distributions. In order to decrease false detections by non-VLFE signals on the condition that
 161 only the vertical-component seismograms can be used and the station coverage along the azimuth
 162 direction is poor, we adopted a strict detection threshold compared to previous studies (e.g., $8 \times$
 163 MAD in Shelly et al., 2007, and Baba et al., 2018 and $9 \times$ MAD in Baba et al., 2020a). The changes
 164 of CCs when focal mechanisms or depths of assumed source models are different from the
 165 geometry of the plate boundary are shown in Figure S4.

166 2.1.3. VLFE location and discarding false detections

167 Although a strict detection threshold was employed, there were false detections that are
 168 caused by other signals, such as local or regional regular earthquakes or teleseismic events. To
 169 exclude local or regional earthquakes, we compared the origin time of detected events with a
 170 catalog of local and regional regular earthquakes constructed by El Observatorio Vulcanológico y
 171 Sismológico de Costa Rica, Universidad Nacional (Catálogo de Temblores de Costa Rica, 2004-
 172 2006; Protti, personal comm.). We discarded events whose epicentral distances were less than 150
 173 km and origin times were within ± 50 s from the local or regional earthquakes listed in this
 174 earthquake catalog. To discard false detections by teleseismic events, we removed the events
 175 detected between the P -wave arrivals and 600 s after S -wave arrivals of teleseismic events ($M_w \geq$
 176 5) in the catalog of the United States Geological Survey. The event amplitudes and CCs are
 177 positively correlated in general, but events with high amplitudes and low average CCs occasionally
 178 appeared. These events can be considered to be false detections due to teleseismic events absent
 179 in the catalogs. Therefore, we did not count events with average CCs below 0.56 and relative
 180 amplitudes to templates higher than 0.4 (Baba et al., 2018; 2020a). If the amplitude relative to the
 181 template with M_w of 4.0 was smaller than 0.05, we did not count the event because the signal was
 182 too small to judge whether the event is truly existed or not.

183 For the remaining events, we calculated the variance reduction (VR) between the template
 184 and observed waveforms. We estimated VRs using only the vertical-component seismograms of
 185 relatively quiet stations in and around the Nicoya Peninsula (MANS, CABA, FINA, CRUP, and
 186 PALM), because amplitude differences between updip and downdip events were large in these
 187 stations:

$$188 \quad VR = \left[1 - \frac{\sum_i \int \{f_i(t) - cg_i(t)\}^2 dt}{\sum_i \int \{f_i(t)\}^2 dt} \right] \times 100\% , \quad (1)$$

189 where $f_i(t)$ and $g_i(t)$ are the observed and template waveforms at the i -th station, respectively,
 190 and c is the relative amplitude of the observed waveform to the template. We selected events whose
 191 VRs were larger than 30%. A discarded example based on the VR is shown in Figure S5. This
 192 threshold was set by trial and error based on visual identifications of VLFEs in the observed data.

193 After the above procedures, falsely detected events still remained because we only used the
194 vertical-component seismograms, and the array configuration was cross shaped. To discard the
195 remaining false detections, we estimated the normalized-and-stacked amplitude, azimuth, and
196 velocity of signal propagation by applying delay-and-sum beamforming (Section 3.1 of Rost &
197 Thomas, 2002; Walter et al., 2013) to vertical-component seismograms. After normalizing the
198 waveform of each station by its maximum amplitude in the 150 s time window, we searched for
199 the azimuth and velocity that maximized the stacked amplitude by performing a grid search for
200 the azimuth between 135–315° with 1° intervals and the velocity between 2–5 km/s with 0.1 km/s
201 intervals. We first used the along-strike stations in both Costa Rica and Nicaragua (brown inverted
202 triangles in Figure 1b) to discard teleseismic events. The amplitudes of Costa Rican VLFs at the
203 Nicaraguan stations were generally very small compared with those in the Costa Rican stations
204 due to geometrical spreading, but amplitudes for teleseismic events are similar. Therefore, we
205 selected events whose stacked normalized amplitude normalized by the number of stations was
206 smaller than 0.6 because events with large stacked signals were suspected to be teleseismic
207 earthquakes (Figure S6). We then conducted another beamforming analysis for the remaining
208 events using the same stations as the matched-filter analysis, and selected events whose azimuth
209 was 200–230°. Finally, to avoid duplicate detection, only one event was counted every 60 s from
210 the remaining VLFE candidates. We only counted the event whose averaged CC was the highest
211 spatiotemporally.

212 **2.1.4. Estimation of the moments of events**

213 We estimated the source durations of detected VLFs by comparing template waveforms
214 with source durations of 10–50 s with observed waveforms (e.g., Yabe et al., 2021). The M_w of
215 the templates was set to be 4.0. The source duration that resulted in the highest values of CC
216 between the observed and template waveforms was adopted.

217 We also calculated the amplitude of an event relative to the template waveforms using the
218 same method as Baba et al. (2020b). The relative amplitude was used to calculate the seismic
219 moment of each VLFE. The seismic moment rate of a VLFE was calculated by dividing its seismic
220 moment by its source duration. To evaluate the estimation error of moment rates of VLFs, we
221 calculated moment rates by assuming the various source durations whose CCs between synthetic
222 and observed waveforms were more than 90% of the maximum CC. Although there are errors in
223 the order of 0.2, we verified that the order of moment rates did not change (Figure S7).

224 **2.2. Results**

225 We detected 68 VLFs during the analysis period. Example traces of a VLFE located at
226 85.8°W and 9.4°N are shown in Figure 3. The signal of this VLFE first arrives at MANS and
227 propagates to inland stations (top panel of Figure 3). This feature was successfully modeled for
228 the updip templates (Fig. 2b). There is a tremor signal in the frequency range of 2–8 Hz in the
229 same time window (middle and bottom panels of Figure 3). The cumulative number of VLFs
230 showed significant increases in September 2004 and August 2005 (Figure 4a). In August 2005, an
231 SSE was reported by Jiang et al. (2012); therefore, SSE and VLFE activities were temporally
232 correlated. The M_w and source duration of VLFs in Costa Rica were mainly distributed in 3.4–
233 4.2 and 10–30 s, respectively (Figures 5a, b).

234 Most of the detected VLFs (62 events) are distributed where the plate boundary is at a
235 depth range of 6–10 km below the sea level, near the trench axis off the Nicoya Peninsula (Figure
236 4b), at the updip of the seismogenic zone. The distribution of these VLFs is consistent with the

237 VLFs in 2008 suggested by Walter et al. (2013). For the verifications of current results based on
238 only vertical components, we selected several events with relatively high signal-to-noise (SN)
239 ratios in horizontal components and located them using three-components seismograms. The
240 resultant high CC areas overlap and the epicenters were also located near the trench axis, although
241 there are differences of $0.1\text{--}0.2^\circ$ (Figure S2). The area also overlaps with the shallower part of the
242 large slip area of the 2007 SSE (Jiang et al., 2017) or summed SSE slip in 2007–2012 (Dixon et
243 al., 2014). Although the slip distribution of the 2005 SSE was not estimated in previous studies,
244 our results suggest that the 2005 SSE can also have a large slip area near the trench axis, similar
245 to the 2007 SSE. The distribution of VLFs lies within the gap between large slip areas of thrust-
246 type large interplate earthquakes with an M_w of 7–8 around the Nicoya Peninsula and the 1992
247 tsunami earthquake with an M_w of 7.6. The distribution of VLFs also separated from the afterslip
248 area of the 2012 M_w 7.6 earthquake (Malservisi et al., 2015).

249 The distribution of the CC shows the resolution of the location of VLFs. By the
250 distribution of CC, it is confirmed that most of the VLFs were located near the trench axis. CCs
251 for more than half of the events exceeded the threshold only for updip templates (Figure 6a). For
252 several events, CCs exceeded the threshold both updip and downdip of the seismogenic zone with
253 a larger CC in the updip region. The area where CCs are more than 90% of the maximum CC is
254 concentrated only in the updip area (Figure 6b). On the other hand, 6 VLFs were located at a
255 depth of ~ 40 km at the downdip of large earthquakes (Figure 4b). Although focal mechanisms may
256 not be thrust-type and the areas where CCs are larger than the threshold are widely distributed, we
257 verified that regular earthquakes listed in the earthquake catalog by El Observatorio Vulcanológico
258 y Sismológico de Costa Rica in the updip and downdip areas are located in the updip and downdip
259 areas respectively by this method (Figure S8). However, we cannot exclude the possibility that
260 such VLFs occur in the updip region in real because, in such cases, bimodal CC distributions
261 tend to appear both in the updip and downdip (Figure 6c). Of course, there is a possibility that such
262 VLFs really occur in the downdip region because the locations of such VLFs were near the
263 locations of previously reported LFs (Brown et al. 2009) and tremors (Outerbridge et al. 2010).
264 In this study, the SN ratios of VLFs detected in the downdip region were very low; hence, it is
265 difficult to judge whether such VLFs occur in downdip or updip, because it is hard to judge which
266 station the signal of the VLFE arrival first due to the similar arrival times at updip stations. The
267 reason for the small number and the low SN ratio of downdip events may be that slow earthquakes
268 in the downdip region were inactive during 1.5 years of the temporary array. To investigate
269 whether deep VLFs really exist, an analysis with a longer dataset is needed in future work.

270 **3. Estimations of seismic energy rates for tremors accompanied by VLFs**

271 **3.1. Data and method**

272 Tremor signals were also found in the frequency range of 2–8 Hz within the time windows
273 of detected VLFs (middle panel of Figure 3; Figure S9). It is difficult to locate tremors in the
274 offshore region by using an onshore network because sources of tremors are distant from the
275 network and signals of tremors attenuate strongly compared to VLFE (0.02–0.05 Hz) signals.
276 Based on the spatiotemporal correlation between VLFs and tremors reported in other regions
277 (e.g., Ghosh et al., 2015; Maeda & Obara, 2009; Tamaribuchi et al., 2019) and the interpretation
278 that VLFs and tremors are components of broadband slow earthquake phenomena (Gomberg et
279 al., 2016; Hawthorne & Bartlow, 2018; Ide & Maury, 2018), we estimated the energy rate functions
280 of tremors accompanied by VLFs by assuming that a tremor occurs at the same location as the
281 VLFE, i.e., the VLFE source grid with the highest CC as written in Section 2.1.3 (e.g., Yabe et al.,

282 2021). We simulated the waveforms at the location of a VLFE using the same model which is
 283 described in Section 2.1.2 but discretized by a finer grid interval (0.04 km). The simulated
 284 envelope shapes are different from observed ones due to a simple pulse source time function
 285 (details in the caption of Figure S10), but the arrival times of maximum *S*-wave amplitudes in the
 286 frequency range of 2–8 Hz are consistent with observed tremor waveforms (Figure S10). The
 287 interval of source grids for the VLFE detection was set as 0.1°, therefore, we supposed that a VLFE
 288 and the corresponding tremor occurred at the same location in the order of 10 km.

289 We also used waveforms of the TUCAN network similarly to the VLFE detection. After
 290 applying a bandpass filter of 2–8 Hz, the envelope waveforms were calculated by taking the root-
 291 mean-square of sums of three-component squared seismograms and a smoothing time window of
 292 3 s (bottom panel of Figure 3). The envelope waveforms were resampled at one sample per second.

293 3.1.1. Quality factor of the apparent *S*-wave attenuation

294 To estimate the energy rate functions of tremors accurately, we estimated the quality factor
 295 of the apparent *S*-wave attenuation (Q_{app}), based on the coda-normalization method (e.g., Aki,
 296 1980; Yoshimoto et al., 1993). First, we selected some isolated regular earthquakes (Figure S11).
 297 To eliminate the effect of differences in source size and site amplification, observed maximum *S*-
 298 wave amplitudes were normalized by averaged coda amplitudes within a lapse time of 80-90 s.
 299 The coda-normalized maximum *S*-wave amplitude of the *i*-th earthquake at the *j*-th station (A_{ij})
 300 and the distance between the hypocenter of the *i*-th earthquake and *j*-th station (L_{ij}) have the
 301 following relationship (Takemura et al., 2017):

$$302 \ln(L_{ij}A_{ij}) = -\frac{\pi f_c Q_{app}^{-1}}{v_s} L_{ij} + C', \quad (2)$$

303 where V_s is the *S*-wave velocity (assuming 3.5 km/s in this study; Maeda & Obara, 2009; Yabe et
 304 al., 2019; 2021), f_c is the central frequency (assuming 5 Hz in this study), and C' is a constant. By
 305 solving Equation (2) by the least-squares method, we estimated Q_{app}^{-1} as $10^{-2.42}$ (Figure 7a).

306 3.1.2. Site amplification factor

307 We estimated the site amplification factor at 2–8 Hz using relative coda amplitudes (e.g.,
 308 Maeda and Obara, 2009). Coda amplitudes at a certain time window generally depend on the
 309 source size and site amplification (e.g., Chapters 2 and 3 of Sato et al., 2012). Therefore, the ratio
 310 of the coda wave amplitude at a station to that at a reference station for the same event depends
 311 only on the site amplification factor relative to a reference station.

312 We calculated the ratios of the coda amplitudes for each station to those of MANS
 313 (reference station) for each regular earthquake used in Section 3.1. The time window for evaluating
 314 relative coda amplitudes is the same as that in coda-normalization in Section 3.1. Then we
 315 calculated the average of the coda amplitude ratios of all earthquakes for each station. The
 316 estimated relative site amplification factors at each station used in the estimations of the energy
 317 rate functions of tremors are shown in Figure 7b. We compared coda amplitudes of regular
 318 earthquakes at MANS with those at the JTS, a permanent station of the Global Seismograph
 319 Network by Incorporated Research Institutions for Seismology and International Deployment of
 320 Accelerometers (Scripps Institution of Oceanography, 1986). The average ratio of coda amplitudes
 321 at MANS to those at JTS is 1.14, suggesting that the condition of MANS site is very similar to that
 322 of the JTS.

323 3.1.3. Seismic energy rate of tremors

324 By using apparent attenuation (Q_{app}^{-1}) and site amplification in the previous subsections,
 325 we estimated the energy rate functions of tremors. The source energy rate function of a tremor
 326 ($E_j(t)$) using the amplitude of the j -th station is calculated by the following formula (Maeda &
 327 Obara, 2009):

$$328 \quad E_j(t) = 2\pi V_s r_j^2 \rho A_j'^2(t + t_j) \exp(2\pi f_c Q_{app}^{-1} t_j), \quad (3)$$

329 where $A_j'(t)$ is the site-corrected amplitude of the envelope waveform of the j -th station, r_j is the
 330 hypocentral distance from the accompanying VLFE, t_j is the travel time from the VLFE source,
 331 and ρ is the density (assuming 2,700 kg/m³). For calculating $E_j(t)$, we used a 180 s time window
 332 that started 60 s before the origin time of VLFES. We calculated the CCs of all station pairs in
 333 Figure 7b. The range of CCs of each pair is 0.5–0.85 for the event of Figure 3 (Figure S12). To
 334 estimate the source energy rate function of the tremor, we only used stations whose CCs with at
 335 least one other station exceeded 0.6.

336 The seismic energy rate W_j using the amplitude of the j -th station is given by the integration
 337 of the source energy rate function $E_j(t)$ in time:

$$338 \quad W_j = \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} E_j(t) dt, \quad (4)$$

339 where t_1 and t_2 are the start and end of the integration range, respectively. The integration range
 340 was defined as the period in which the values of $E_j(t)$ exceeded 20% of the maximum value of
 341 $E_j(t)$ (Figure 8). The seismic energy rate of a tremor (W_0) was obtained by calculating the average
 342 W_j of all stations. The error of W_0 was obtained by calculating the standard deviation of W_j .

343 **3.2. Results**

344 For 13 of 68 VLFES, there were no station pairs whose CCs were larger than 0.6 when
 345 estimating the energy rates of accompanying tremors, because such tremors may not be detected
 346 by technical limitations or tremors and VLFES may be distinct phenomena. We, therefore,
 347 estimated energy rates of 55 tremors. The energy rates of tremors were mainly distributed in 10^3 –
 348 $10^{5.5}$ J/s (Figure 9). There is a positive correlation between the energy rates of tremors and the
 349 moment rates of the corresponding VLFES. We estimated the scaled energy by calculating the ratio
 350 between the seismic energy rate of a tremor and the seismic moment rate of the corresponding
 351 VLFE. The scaled energy of slow earthquakes off Costa Rica is mainly distributed in the range of
 352 10^{-9} – 10^{-8} (dotted lines in Figure 9).

353 **4. Discussion**

354 **4.1. Shallow ETS off Costa Rica**

355 As shown in Figure 3 and Figure S9, VLFES and tremors often were temporally correlated.
 356 The activation of VLFES and tremors in August 2005 temporally correlates with the 2005 SSE
 357 reported by Jiang et al. (2012). VLFES and tremors occurred mainly in the updip area in August
 358 2005; hence, the slip area of the 2005 SSE can be distributed in the updip area near the trench axis,
 359 similar to the 2007 SSE. In areas where shallow VLFES occurred, subseafloor hydrological
 360 observatories recorded pore fluid pressure transients in 2000 (Brown et al., 2005), 2003–2004
 361 (Solomon et al., 2009), and 2007–2013 (Davis et al., 2011; 2015). They interpreted that pore fluid
 362 pressure transients were caused by SSEs. Spatial correspondence of pore fluid change in the
 363 periods of previous studies and VLFE activity in 2005 near the trench off Costa Rica suggests the

364 occurrence of a shallow ETS, as with the Nankai subduction zone (Araki et al., 2017; Nakano et
365 al., 2018).

366 **4.2. Potential inferences of the frictional property on the plate boundary**

367 To discuss the heterogeneity of the potential frictional property on the plate boundary, we
368 compare the differences of potential stress drops and interplate coupling between the VLFE area
369 and the seismogenic zone in the Central American subduction zone. The variability in the stress
370 drop reflects the variability of earthquake sources, which presumably represents a heterogeneity
371 in conditions at the sources (Abercrombie, 2021). In this study, we showed that most of VLFEs
372 were located at a depth range of 6–10 km on the plate boundary, which is updip of the seismogenic
373 zone. The stress drop of VLFEs in the Nankai subduction zone was estimated to be 0.1–10 kPa
374 (Ito & Obara, 2006), therefore we expect that the potential stress drop of VLFEs in Costa Rica is
375 similar. This is much smaller than the stress drop of earthquakes in the tsunami earthquake rupture
376 area (1.2 MPa; Bilek et al., 2016). In addition, the interplate coupling was estimated to be weak at
377 a depth range of 6–10 km (Feng et al., 2012), and strong in the seismogenic zone at a deeper depth
378 than 10 km (Protti et al., 2014).

379 The spatial variation of potential stress drops and interplate coupling at the plate boundary
380 may result from the heterogeneous distribution of potential frictional properties on the plate
381 boundary in the Central American subduction zone. In addition, a low stress drop suggests a high
382 pore pressure generated by the existence of fluids (Yao & Yang, 2020). Therefore, the potential
383 frictional strength of the slow earthquake area at a depth range of 6–10 km may be quite weak
384 owing to the rich fluid compared to that in the regions with regular and tsunami earthquakes.

385 In Costa Rica, repeating earthquakes occurred around the large coseismic slip area of the
386 2012 M_w 7.6 earthquake on the Nicoya Peninsula (Chaves et al., 2020). In this study, VLFEs were
387 mainly located near the trench axis, which is spatially separated from the locations of repeating
388 earthquakes that occur near the Nicoya Peninsula. Such spatial separation of slow and repeating
389 earthquakes on the plate boundary is also found in the Nankai (e.g., Takemura et al., 2020) and the
390 Tohoku subduction zone (e.g., Nishikawa et al., 2019).

391 **4.3. Comparison with other subduction zones**

392 The M_w and source duration of VLFEs have a positive correlation (Figure 5c) like shallow
393 VLFEs in Nankai, Japan (Sugioka et al., 2012; Takemura et al., 2019). Ide et al. (2007) suggested
394 that the relationship between durations and magnitudes of slow earthquakes is explained by 1st
395 power scaling law, whereas Dal Zilio et al. (2020) and Michel et al. (2019) inferred that the
396 relationship between moments and durations of SSEs is cubic. Although the number of cases is
397 small, it seems that durations and magnitudes of SSEs in Costa Rica (Voss et al., 2017) can be
398 explained by both 1st order and cubic scaling laws (Figure 5c). Jolivet & Frank (2020) suggested
399 that the difference between two scaling laws was caused by the ability to detect the beginnings and
400 ends of events. The relationship between moments and durations between both VLFEs and SSEs
401 is closer to the 1st power scaling law than the cubic scaling law.

402 Our study revealed that shallow VLFEs and tremors occurred near the trench axis off Costa
403 Rica, in the updip of coseismic slip areas of thrust-type large earthquakes with an M_w of 7–8. In
404 the updip area, SSEs also occurred in 2007–2012 (Dixon et al., 2017; Jiang et al., 2012). The depth
405 range and the separate distribution between shallow slow earthquakes and large earthquakes off
406 Costa Rica are similar to shallow slow earthquakes in the Nankai subduction zone, where slow

407 earthquakes are spatially separated from high slip-deficit zones (e.g., Takemura et al., 2020). On
408 the other hand, before the 2011 Tohoku earthquake, shallow slow slip events propagated to the
409 initial rupture point of the great earthquake (Kato et al., 2012). Therefore, the characteristics of
410 distribution of slow and large earthquakes differ between Tohoku and Costa Rica.

411 There are other common features in shallow slow earthquakes between Costa Rica and
412 Nankai. Although the lower limit of M_w is large (~ 3.4) due to a strict threshold, the ranges of
413 magnitudes and source durations of shallow VLFES off Costa Rica are similar to those of shallow
414 VLFES in the Nankai subduction zones (e.g., Takemura et al., 2019). The recurrence intervals of
415 activation of slow earthquakes are one to several years in Costa Rica (Jiang et al., 2012), which is
416 similar to shallow slow earthquakes in the Nankai subduction zone, but different from the shorter
417 intervals of deep slow earthquakes in Nankai (e.g., Baba et al., 2020b). Although the tremor
418 analysis is limited due to the missing of small events by the strict threshold of VLFES, the range
419 of energy rates of tremors was 10^3 – $10^{5.5}$ J/s. The upper limit of the energy rate range of tremors is
420 similar to that observed for shallow tremors in Nankai (Yabe et al., 2019). The estimated scaled
421 energy of slow earthquakes off Costa Rica is also similar to that of shallow slow earthquakes in
422 the Nankai subduction zone (Yabe et al., 2019). The scaled energy is related to the rupture process
423 of seismic phenomena (Kanamori & Rivera, 2006); therefore, the frictional properties within the
424 shallow slow earthquake areas may be similar in both Costa Rica and Nankai. On the other hand,
425 the scaled energy range in both regions is 0.5–1 orders of magnitude larger than that of shallow
426 slow earthquakes in the Tohoku subduction zone (Yabe et al., 2021), and approximately 1 order
427 of magnitude larger than that of deep slow earthquakes in Nankai (Ide et al., 2008; Ide & Yabe,
428 2014; Ide, 2016; Ide & Maury, 2018; Maeda & Obara, 2009) (Figure 9). We note that scaled
429 energies of shallow slow earthquakes were estimated for individual events, whereas those of deep
430 slow earthquakes estimated by Ide & Yabe (2014), Ide (2016), and Ide & Maury (2018) were
431 estimated for stacked events.

432 The range of scaled energy and distribution of shallow slow earthquakes off Costa Rica are
433 more similar to those in shallow Nankai than shallow Tohoku. According to Syracuse et al. (2010),
434 the age and thermal parameters of Costa Rica are 15.8 Ma and 1,010 km, respectively, which are
435 closer to those of Nankai (20.0 Ma and 450 km, respectively) than Tohoku (115.2–130.5 Ma and
436 5,720–6,040 km, respectively). The thermal parameter, which is product of the incoming plate age,
437 the convergence rate, and the sine of the slab dip angle, is used to predict the slab surface
438 temperature at a given depth (e.g., Kirby et al., 1991; Syracuse et al., 2010). In addition, the
439 temperatures of shallower parts of plate interfaces of these subduction zones where shallow slow
440 earthquakes are not so different (Nankai: ~ 100 °C in the depth range of 0–5 km from the seafloor;
441 Tohoku: 65–110 °C in the depth range of 6–12 km; and Costa Rica: 12–60°C in the depth range of
442 0–10 km; modeled temperature in Saffer & Wallace, 2015). On the other hand, the Central
443 American subduction zone is subduction of fast convergence rate (~ 8 cm/year; DeMets et al.,
444 1994), high dip angle, and erosional type (e.g., Bangs et al., 2016), which are more similar to
445 Tohoku than Nankai. Although the characteristics of slow earthquake activity can be related to
446 various factors, the thermal parameter and incoming plate age of Costa Rica is more similar to
447 Nankai than Tohoku. The temperature structure of the shallow plate interface is probably most
448 sensitive to incoming plate age (Maunder et al., 2019) and secondarily to thermal parameter
449 (Syracuse et al., 2010). Hence, similar temperature conditions on the interface may explain the
450 common features of shallow slow earthquakes off Costa Rica and in Nankai.

451 In previous studies, the large slip area of the SSE in 2007 was separated into deeper and
452 shallower parts (Jiang et al., 2017), and deep LFEs and tremors were detected downdip of the
453 seismogenic zone (Brown et al., 2009; Outerbridge et al., 2010). And, several VLFs were located
454 in the downdip area, in the similar area reported in previous studies of tremors and LFEs. If these
455 deep VLFs, LFEs and tremors occur in the downdip area, slow earthquakes might occur at
456 separate depths along both shallower and deeper extensions of rupture zones of large earthquakes
457 (Figure 10). This characteristic might also be the same as that of the Nankai subduction zone
458 (Obara & Kato, 2016). This suggests that the tectonic property may be similar in the wide depth
459 range in Costa Rica and Nankai. On the other hand, slow earthquakes are distributed only in the
460 deeper part in the Cascadia subduction zone and only in the shallower part in the Tohoku
461 subduction zone. The variation of the distribution of slow earthquakes may be attributed to the
462 difference in tectonics or detection capability. The elucidation of the reason for the difference in
463 the distribution in slow earthquakes is future work.

464 **5. Conclusions**

465 Based on the grid-search matched-filter technique using synthetic templates in the regional
466 3D model, we detected and located VLFs around the Nicoya Peninsula. Many VLFs occurred
467 in September 2004 and August 2005, and more than 90% of the VLFs were located near the
468 trench axis, where the plate boundary is at a depth range of 6–10 km, updip of the seismogenic
469 zone, whereas several VLFs were located in the downdip area at a depth of ~40 km. In this area,
470 the occurrence of shallow SSEs is suggested by VLFE episodes. The region with VLFE activity
471 overlaps with the shallower part of the large slip area of the 2007 SSE; therefore, the occurrences
472 of shallow SSEs are suggested in September 2004 and August 2005 to occur in the same area as
473 the shallower part of the 2007 SSE. The distribution of VLFs lies in the gap surrounding
474 coseismic slip areas of tsunami and large regular earthquakes. This separation reflects the spatial
475 distribution of the frictional strength of the plate boundary in the Central American subduction
476 zone. By using high-frequency seismogram envelopes, we also estimated the energy rates of
477 tremors accompanying VLFs. The ranges of magnitude and source duration of VLFs, energy
478 rate of tremors, and scaled energy off Costa Rica are similar to those in shallow slow earthquakes
479 in the Nankai subduction zone.

480 **Data Availability**

481 We used seismograms of the TUCAN network (Abers & Fischer, 2003;
482 https://doi.org/10.7914/SN/YO_2003) and Global Seismograph Network (Scripps Institution of
483 Oceanography, 1986; <https://doi.org/10.7914/SN/II>). We used the earthquake catalog of the U.S.
484 Geological Survey (<https://earthquake.usgs.gov/earthquakes/search/>). We used OpenSWPC code
485 Version 5.0.2 (Maeda et al., 2017; <https://doi.org/10.5281/zenodo.3712650>) for the numerical
486 simulations. Numerical simulations were conducted using the Fujitsu PRIMERGY
487 CX600M1/CX1640M1 (Oakforest-PACS) at the Information Technology Center, the University
488 of Tokyo. We used generic mapping tools (Wessel et al., 2013) and Seismic Analysis Code
489 (Helfrich et al., 2013) to prepare the figures and process seismograms, respectively. The VLFE
490 and tremor catalog constructed by this study is provided in an open access repository, zenodo (doi:
491 [10.5281/zenodo.4435232](https://doi.org/10.5281/zenodo.4435232)).

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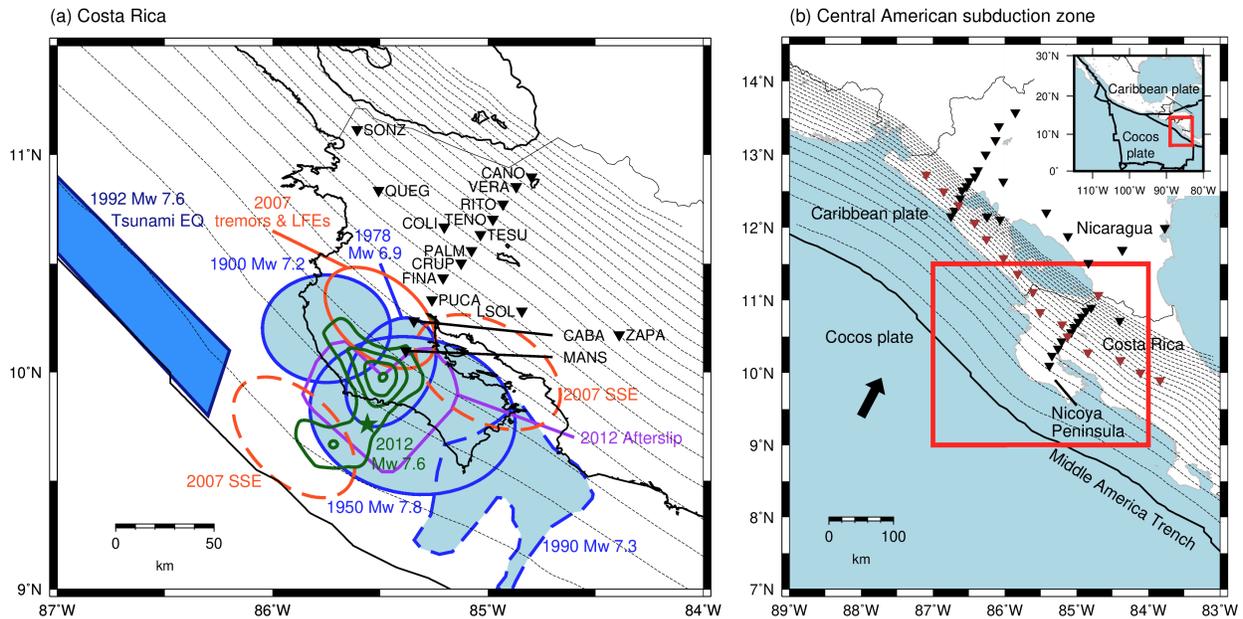
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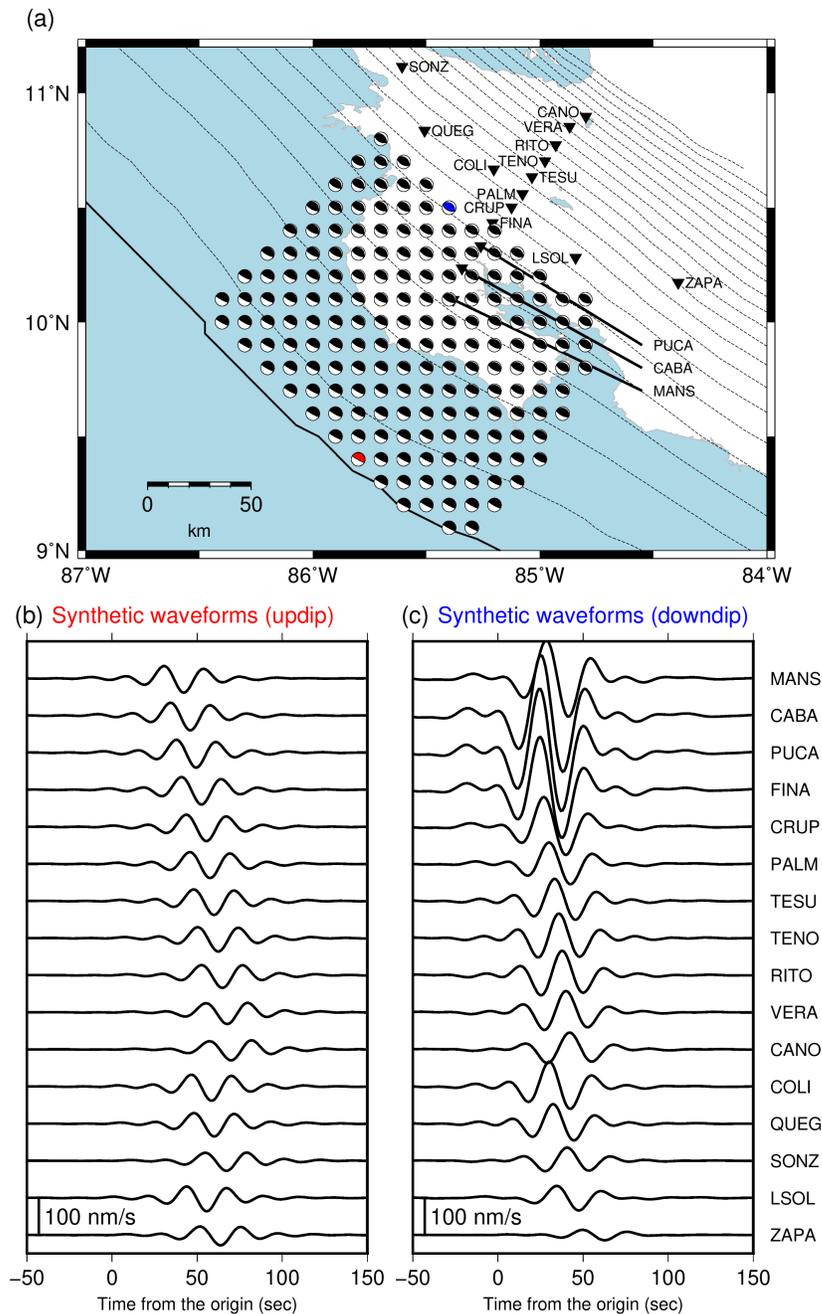
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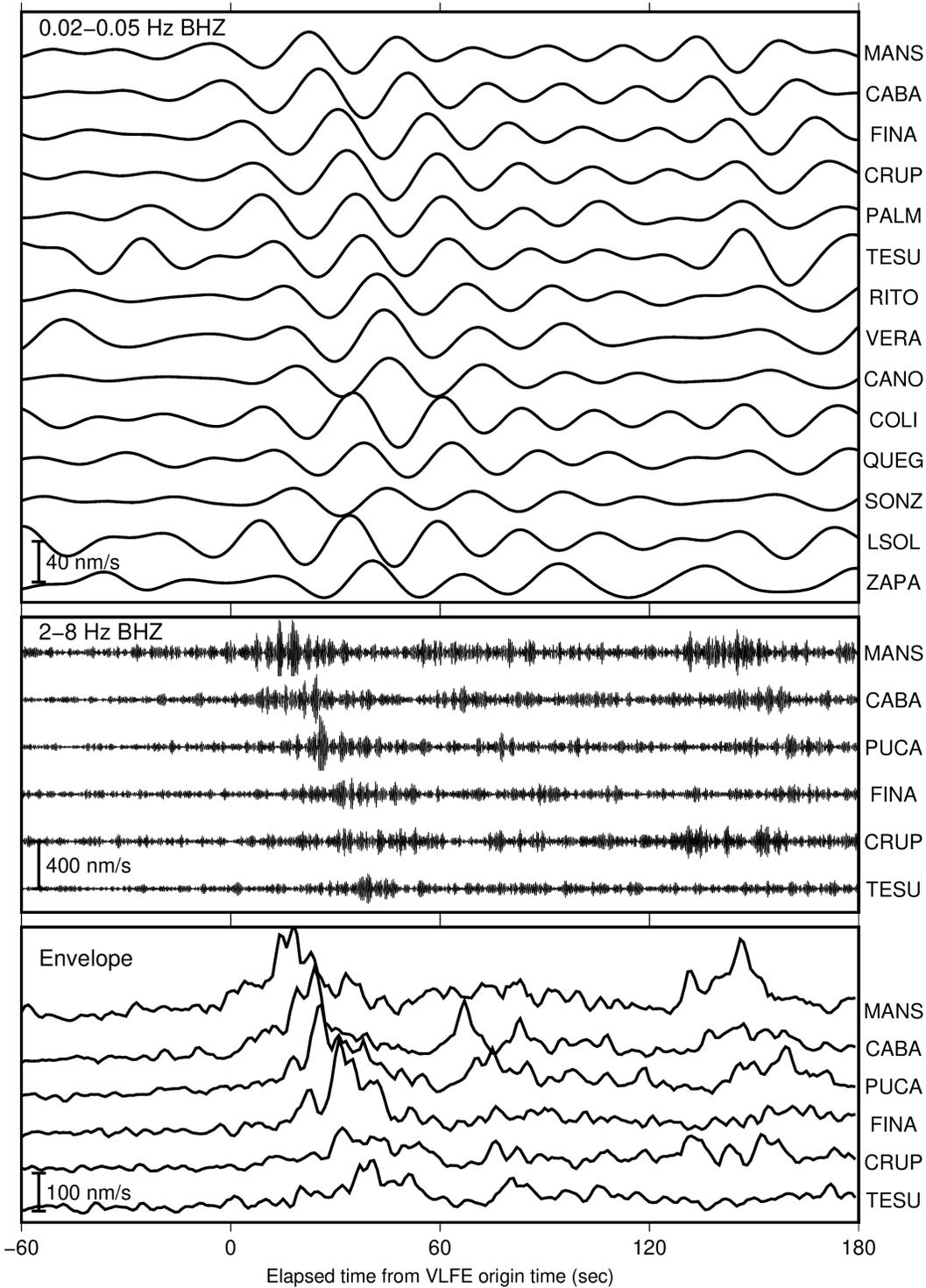
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790 **Figure 1.** (a) Large regular and slow earthquake areas based on previous studies around the Nicoya
 791 Peninsula, in Costa Rica. Green contours show the coseismic slip distribution of the 2012 M_w 7.6
 792 earthquake with a 1-m interval (Yue et al., 2013). Blue areas show the slip areas of large regular
 793 earthquakes (1990 M_w 7.3: Protti et al., 1995 (surrounded by dashed blue line); others: Yue et al.,
 794 2013 (surrounded by solid blue lines)). Dark blue area surrounded by solid dark blue line indicate
 795 the slip area of the 1992 tsunami earthquake (Satake, 1994). Orange ellipses with dashed lines
 796 show large slip areas of the 2007 SSE, which were separated in updip and downdip areas (Jiang et
 797 al., 2017). The orange ellipse with a solid line shows the distributions of LFEs (Brown et al., 2009)
 798 and tremors (Outerbridge et al., 2010). The purple polygon shows the area whose afterslip of the
 799 2012 M_w 7.6 earthquake is more than 150 mm (Malvervisi et al., 2015). Black inverted triangles
 800 show the station locations of the TUCAN network used in VLFE detection (Section 2.2). Dashed
 801 contours indicate the isodepths of the top of the Cocos Plate with 10 km intervals (Slab2; Hayes
 802 et al., 2018). (b) Map of the Central American subduction zone. Solid line represents the Middle
 803 America Trench (Slab2; Hayes et al., 2018). Dashed contours are the same as (a). Black arrow
 804 indicates the convergence direction of the Cocos Plate, which subducts below the Caribbean plate
 805 from the Middle America Trench (NUVEL-1A; DeMets et al., 1994). Inverted triangles show the
 806 locations of stations of the TUCAN network. Brown triangles are stations which were used in
 807 beamforming (Section 2.3). The black lines in the inset show plate boundaries.



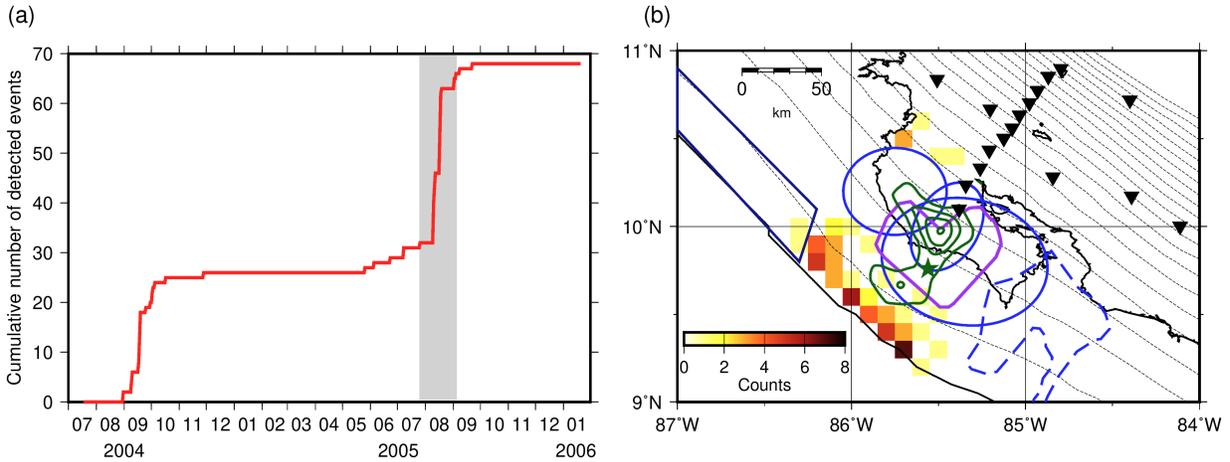
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809 **Figure 2.** (a) Virtual source grids assumed in this study. Beach balls show the locations and focal
 810 mechanisms of the virtual sources. Inverted triangles and the black line are the same as in Figure
 811 1. Dashed contours indicate the isodepths of the top of the Cocos Plate with 10 km intervals (Slab2;
 812 Hayes et al., 2018). Examples of waveforms of virtual sources with Mw 4 in the (b) updip and (c)
 813 downdip areas. Sources of Figures 1b and 1c are shown by the red and blue beachballs in Figure
 814 2a, respectively. Amplitudes of the updip source are small due to the long distance between the
 815 source and stations, whereas amplitudes of the downdip source in the stations near the Nicoya
 816 Peninsula are large due to the short distance between the source and stations.



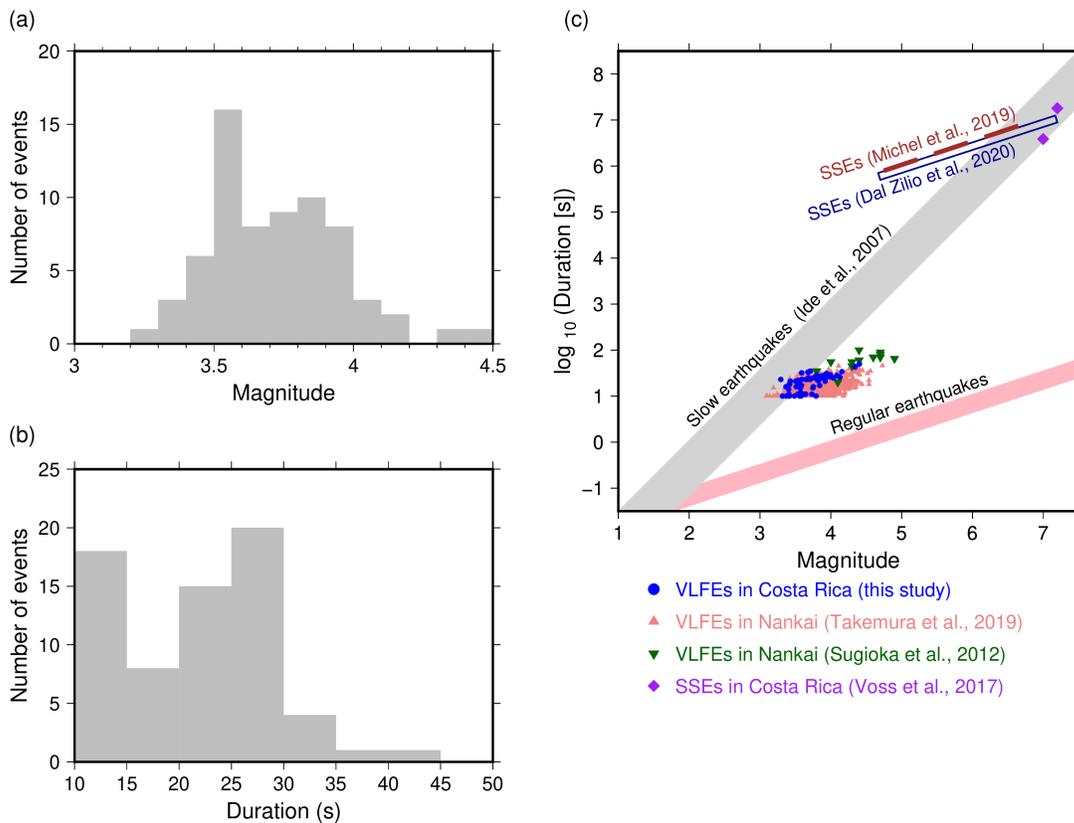
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818 **Figure 3.** Example of waveforms of a VLFE and the corresponding tremor located at 85.8°W and
 819 9.4°N (shown by a red beachball in Figure 2a) in the frequency range of 0.02–0.05 Hz and 2–8 Hz,
 820 and smoothed root-mean-square envelope in the frequency range of 2–8 Hz. Seismograms are
 821 shown from the origin time of the VLFE, 03:53:47 (UTC), August 10, 2005.



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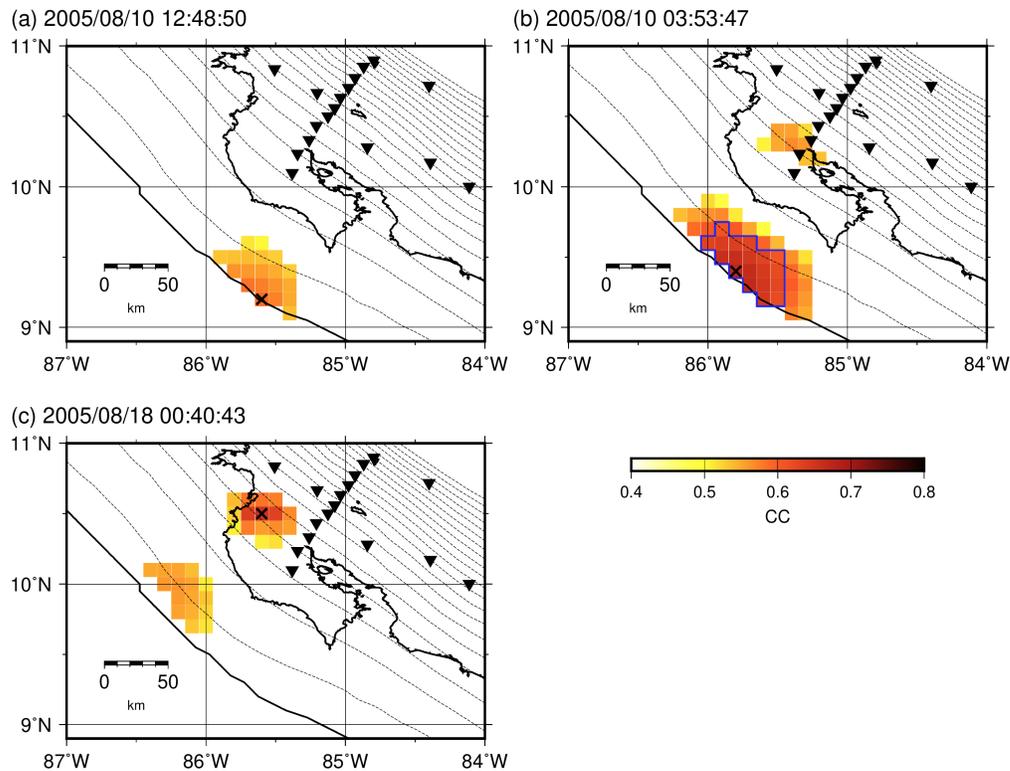
823 **Figure 4.** (a) Cumulative number of the VLFs from July 2004 to January 2006. Gray shading
 824 shows the period of the 2005 SSE (Jiang et al., 2012). (b) Distribution of the number of detected
 825 events at each virtual source. Blue ellipses and polygons, dark blue quadrangle, inverted triangles,
 826 blue line, the purple polygon, and dashed contours are the same as in Figure 1.



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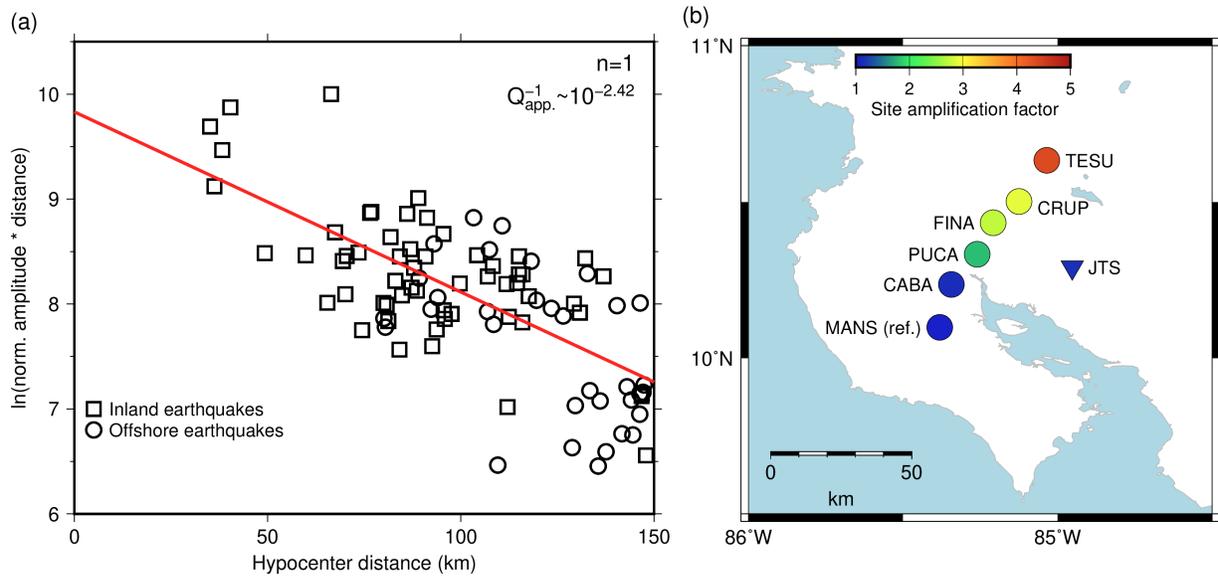
828 **Figure 5.** Distribution of (a) magnitudes and (b) source durations of VLFs. (c) Relationship
 829 between durations and magnitudes of slow earthquakes. Gray and pink shadings show the ranges
 830 of the scaling law for slow and regular earthquakes by Ide et al. (2007), respectively. Brown dashed

831 line and dark blue rectangle show the range of the scaling law for SSEs suggested by Michel et al.
 832 (2019) and Dal Zilio et al. (2020), respectively. Blue dots indicate the relationship between source
 833 durations and magnitudes of VLFEs located in this study. Green inverted triangles and pink
 834 triangles indicate the relationship between source durations and magnitudes of VLFEs estimated
 835 by Sugioka et al. (2012) and Takemura et al. (2019), respectively. Purple diamonds represent the
 836 relationship between durations and magnitudes of SSEs in Costa Rica (Voss et al., 2017).



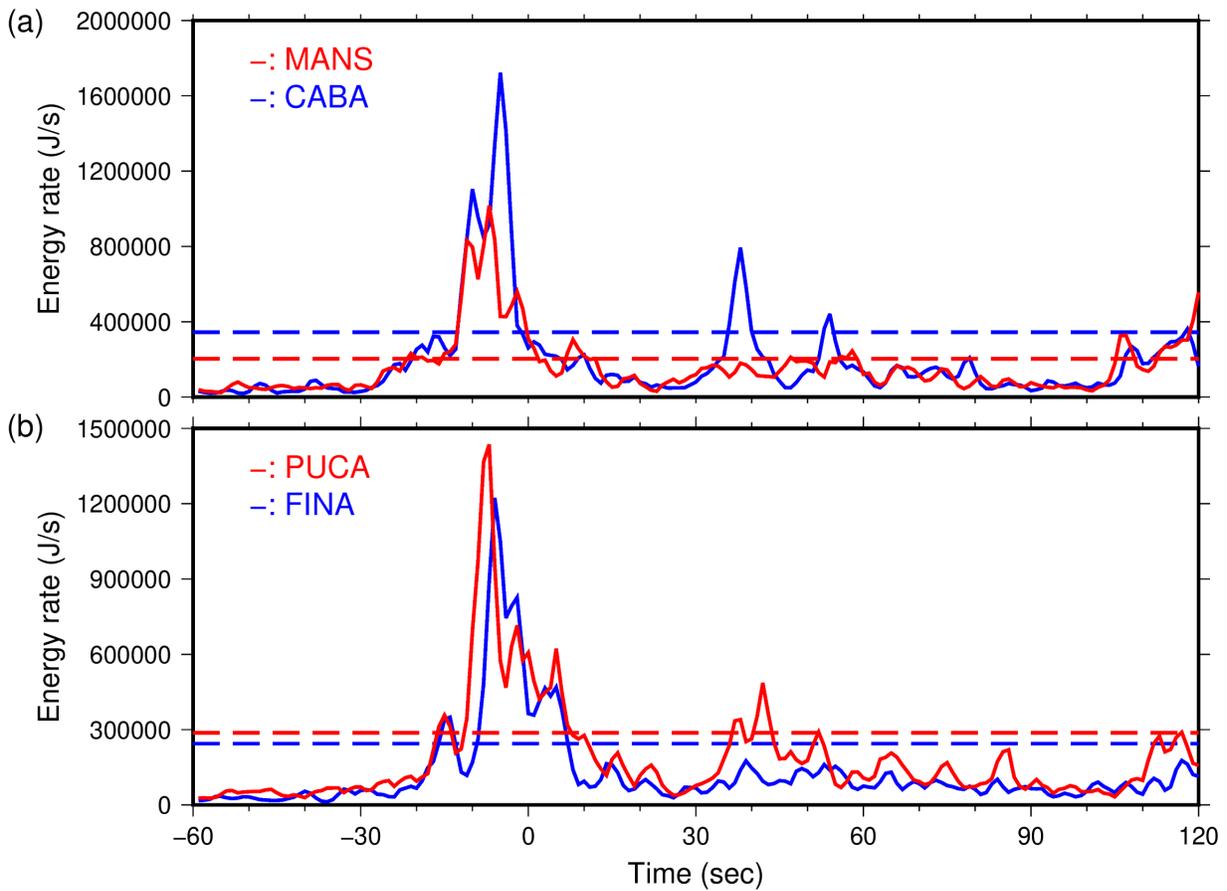
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838 **Figure 6.** Examples of CC distributions of (a) an event which has large CCs only in updip grids,
 839 (b) an event which has large CCs both in updip and downdip grids but is located in an updip grid,
 840 and (c) an event which has large CCs both in updip and downdip grids but is located in a downdip
 841 grid. Cross mark in each map indicates the epicenter of the VLF. Inverted triangles, black line,
 842 and dashed contours are the same as in Figure 1. The blue polygon in (b) indicates the grids whose
 843 CC are more than 0.9 times of the maximum CC.



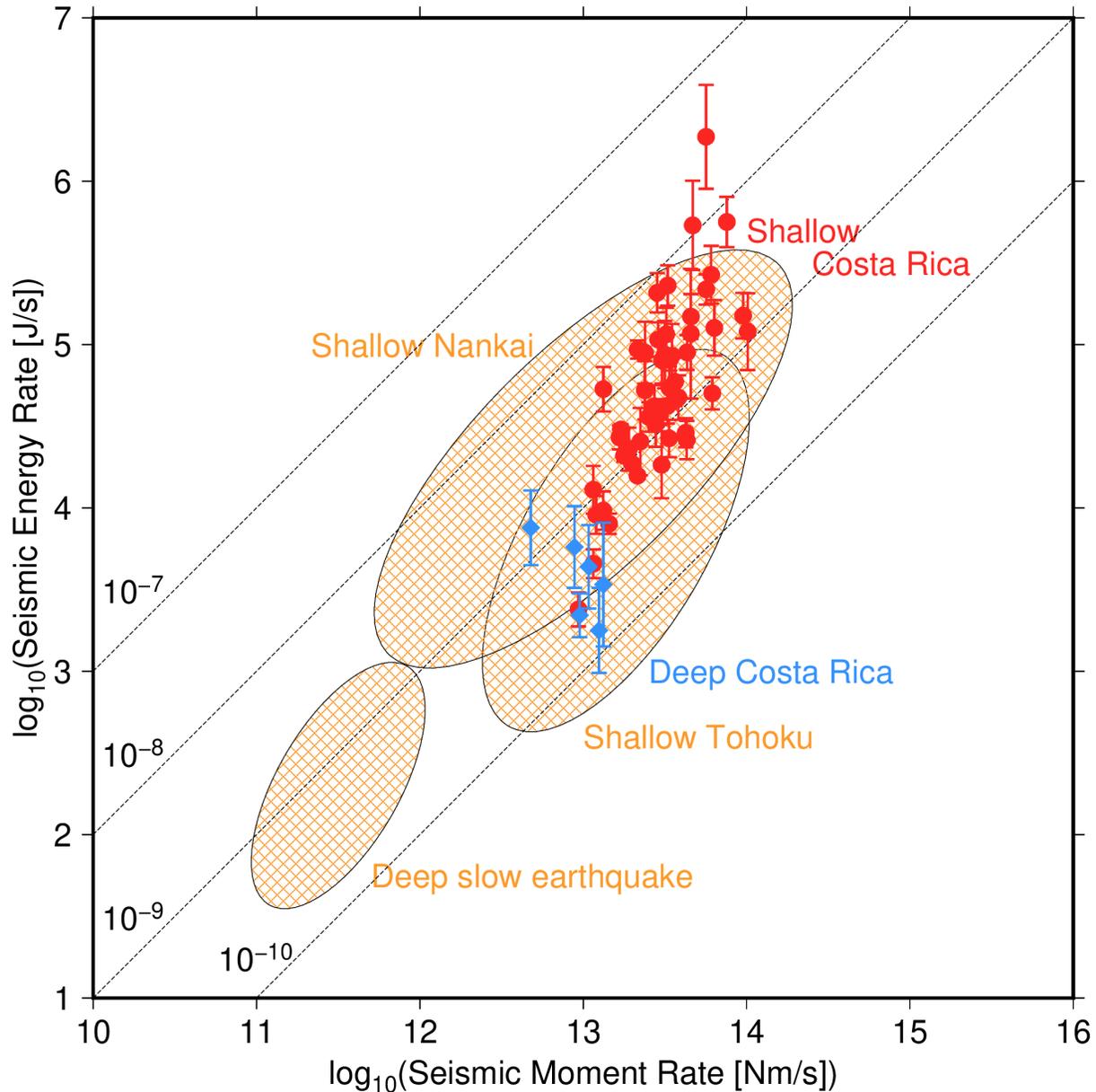
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845 **Figure 7.** (a) Relationship between logarithm of coda-normalized maximum *S*-wave amplitudes
 846 and hypocentral distances. To eliminate effects of geometrical spreading of *S*-wave, coda-
 847 nomadized *S*-wave amplitudes were multiplied by their hypocentral distance. Red line shows the
 848 regression line using Equation (2). (b) Site amplification factors relative to MANS based on
 849 relative coda amplitude measurements.



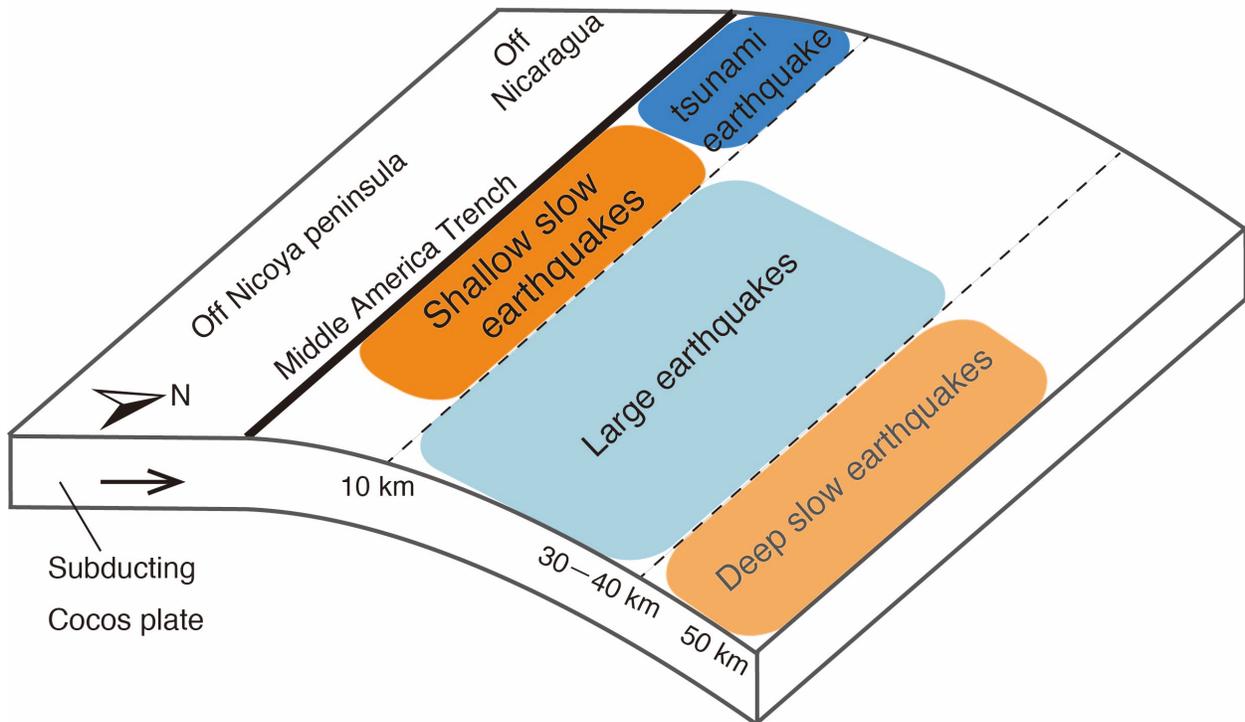
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851 **Figure 8.** Temporal changes of energy rate functions of a tremor in (a) MANS and CABA and (b)
 852 PUCA and FINA. The corresponding VLFE occurs on 03:53:47 (UTC), August 10, 2012. Dashed
 853 lines indicate the threshold, which is set as 20% of the maximum value of the energy rate functions.



854

855 **Figure 9.** Relationship between seismic moment rates of VLFs and seismic energy rates of
 856 tremors estimated in this study. Red circles and blue diamonds show the events of updip and
 857 downdip regions, respectively. Dashed lines show scaled energies of 10^{-7} , 10^{-8} , 10^{-9} , and 10^{-10} .
 858 Orange shadings show the relationships between seismic moment rates of VLFs and seismic
 859 moment rates of tremors of shallow slow earthquakes in the Nankai (Yabe et al., 2019) and Tohoku
 860 subduction zones (Yabe et al., 2021), and deep slow earthquakes in southwest Japan (Ide & Yabe,
 861 2014), Cascadia (Ide, 2016), and Mexico (Ide & Maury, 2018). We note that scaled energies of
 862 shallow slow earthquakes were estimated for individual events, whereas those of deep slow
 863 earthquakes were estimated for stacked events.



864

865 **Figure 10.** A schematic illustration showing the interpretation of distributions of slow, tsunami,
866 and large regular earthquakes in the Central American subduction zone. The areas of large
867 earthquakes, the 1992 tsunami earthquake, and deep slow earthquakes are referred from Yue et al.
868 (2013), Satake (1994), and Outerbridge et al. (2010), respectively.
869