

1 **Shallow Slow Earthquake Episodes Near the Trench Axis Off Costa Rica**

2

3 **Satoru Baba¹, Kazushige Obara¹, Shunsuke Takemura¹, Akiko Takeo¹, and Geoffrey A.**
4 **Abers²**

5 ¹Earthquake Research Institute, The University of Tokyo, Tokyo, Japan

6 ²Department of Earth and Atmospheric Sciences, Cornell University, Ithaca, New York, United
7 States of America

8

9 Corresponding author: Satoru Baba (babasatoru@eri.u-tokyo.ac.jp)

10

11 **Key Points:**

- 12 • Shallow very low frequency earthquakes (VLFEs) and tremors are detected off Costa
13 Rica near the Middle America Trench
- 14 • Distribution of VLFEs and tremors is spatially correlated with slow slip events
- 15 • Scaled energy of shallow slow earthquakes off Costa Rica is 10^{-9} – 10^{-8} , which is similar to
16 those in Nankai

17

18 **Abstract**

19 Slow earthquakes are mainly distributed in regions surrounding seismogenic zones
20 along the plate boundaries of subduction zones. In the Central American subduction zone, large
21 regular interplate earthquakes with magnitudes of 7–8 occur repeatedly around the Nicoya
22 Peninsula, in Costa Rica, and a tsunami earthquake occurred off Nicaragua, just north of Costa
23 Rica, in 1992. To clarify the spatial distribution of various slip behaviors at the plate boundary, we
24 detected and located very low frequency earthquakes (VLFs) around the Nicoya Peninsula using
25 a grid-search matched-filter technique with synthetic templates based on a regional three-
26 dimensional model. VLFs were active in September 2004 and August 2005, mainly near the
27 trench axis, updip of the seismogenic zone. The distribution of VLFs overlaps with large slip
28 areas of slow slip events. Low frequency tremor signals were also found in high-frequency
29 seismogram envelopes within the same time windows as detected VLFs; thus, we also
30 investigated the energy rates of tremors accompanied by VLFs. The range of scaled energy,
31 which is the ratio of the seismic energy rate of a tremor to the seismic moment rate of
32 accompanying VLF and related to the rupture process of seismic phenomena, was 10^{-9} – 10^{-8} . The
33 along-dip separation of shallow slow and large earthquakes and the range of the scaled energy off
34 Costa Rica are similar to those in shallow slow earthquakes in Nankai, which shares a similar
35 thermal structure along the shallow plate boundary.

36 **Plain language summary**

37 Slow earthquakes generally occur on the plate boundaries of subduction zones. We
38 detected and located very low frequency earthquakes (VLFs), which are a type of slow
39 earthquake, off Costa Rica. The VLFs occurred at a depth range of 6–10 km, and their spatial
40 distribution is correlated with slow slip events, another type of slow earthquakes. The spatial
41 separation of slow and large regular earthquakes is common to the Nankai subduction zone. Low
42 frequency tremor signals, which are also classified as slow earthquakes, are also found in
43 seismograms at higher frequencies within the same time windows of detected VLFs. We also
44 estimated the ratio of energy rates of tremors to moment rates of VLFs, which relates to the
45 rupture process of seismic phenomena. The ratio is 10^{-9} – 10^{-8} off Costa Rica, similar to that in
46 shallow slow earthquakes in the Nankai subduction zone.

47 **1. Introduction**

48 Slow earthquakes are mainly observed in regions surrounding seismogenic zones, which
49 are the areas that rupture in large regular earthquakes, along the plate boundaries of subduction
50 zones (e.g., Obara & Kato, 2016) or strike-slip faults (e.g., Nadeau & Dolenc, 2005; Wang &
51 Barbot, 2020). Various types of slow earthquakes, such as low frequency tremors (tectonic
52 tremors; e.g., Obara, 2002), low frequency earthquakes (LFs; e.g., Shelly et al., 2006), very low
53 frequency earthquakes (VLFs; e.g., Obara & Ito, 2005), and slow slip events (SSEs; e.g., Dragert
54 et al., 2001) have been observed in many subduction zones. Although there are areas where some
55 types of slow earthquakes are not spatiotemporally correspondent (Hutchison, 2020; Hutchison &
56 Ghosh, 2016, 2019), they often correlate spatiotemporally, which is termed episodic tremor and
57 slip (ETS). ETSs were observed in deep Cascadia (e.g., Ghosh et al., 2015; Rogers & Dragert,
58 2003) and deep Nankai (e.g., Ito et al., 2007; Obara, 2011), for example. Recently, in the Nankai
59 subduction zone, pore fluid pressure changes have been observed during tremor and VLF
60 activities and are considered to reflect shallow SSEs by offshore borehole observations (Araki et

61 al., 2017; Nakano et al., 2018). The hypocenters and focal mechanisms of slow earthquakes are
62 generally consistent with shear slip on the plate boundaries. VLFE episodes and SSEs occur in
63 almost identical source regions and their temporal changes of moment release are similar during
64 an ETS, therefore VLFE episodes are considered as proxies for SSEs (Hutchison & Ghosh, 2019;
65 Ito et al., 2007; Nakano et al., 2018; Yokota & Ishikawa, 2020). In summary, the distribution of
66 slow earthquakes is related to large earthquake slip areas, interplate coupling, or fluid distribution
67 (e.g., Baba et al., 2020b; Ghosh et al., 2015; Obara & Kato, 2016).

68 In the Central American subduction zone, the Cocos plate subducts beneath the Caribbean
69 plate at the Middle America Trench at a rate of approximately 80 mm/year (Figure 1b; referred
70 from NUVEL1A; DeMets et al., 1994). In this subduction zone, large thrust-type earthquakes with
71 a moment magnitude (M_w) of 7–8 occur with a recurrence interval of tens of years around the
72 Nicoya Peninsula, in Costa Rica (light blue areas in Figure 1a; Protti, 1995; Yue et al., 2013). The
73 coseismic slip areas of these large earthquakes are distributed at a depth range of 10–35 km beneath
74 the peninsula and off the coast. The latest large earthquake with M_w of 7.6 occurred on 5
75 September, 2012 (green contour lines in Figure 1a; Yue et al., 2013). In the vicinity, a tsunami
76 earthquake with M_w of 7.6 also occurred off Nicaragua, just north of Costa Rica, on 2 September,
77 1992 (dark blue area in Figure 1a; Satake, 1994).

78 In addition to large regular and tsunami earthquakes, slow earthquakes also occur around
79 the Nicoya Peninsula. The Global Navigation Satellite System data revealed that SSEs with M_w
80 of 6.6–7.2 occur at intervals of 21.7 ± 2.6 months (Jiang et al., 2012; Xie et al., 2020). The large
81 slip area of the SSE in 2007 was separated into downdip and updip areas by the seismogenic slip
82 area (Jiang et al., 2012, 2017; Outerbridge et al., 2010). The spatiotemporal change in relation to
83 the 2012 M_w 7.6 earthquake was investigated by previous studies (Dixon et al., 2014; Voss et al.,
84 2017), and an SSE preceded the 2012 M_w 7.6 earthquake (Voss et al., 2018) in the almost same
85 area of the 2007 SSE, similar to both the slow slip before the 2011 Tohoku earthquake in Japan
86 (Ito et al., 2013; Kato et al., 2012) and the slow slip before the 2014 Iquique earthquake in Chile
87 (Kato & Nakagawa, 2014; Ruiz et al., 2017).

88 By using high-frequency (>1 Hz) seismograms, Brown et al. (2009) and Outerbridge et al.
89 (2010) located LFEs and tremors in 2007, respectively (Figure 1a). The tremors and LFEs were
90 located in almost the same area, downdip of the seismogenic zone. Although tremors and LFEs
91 were temporally correlated with the SSE, the location of tremors and LFEs were separated from
92 the large slip area of the 2007 SSE. On the other hand, Walter et al. (2011) located many tremors
93 in the offshore region from 2007 to 2009. Walter et al. (2013) also found that VLFs appeared in
94 seismograms in a frequency range of 0.02–0.05 Hz and were temporally correlated with tremors
95 in the time period of the 2008 SSE. Based on beamforming analysis, they estimated the propagation
96 direction and the propagation speed of VLFE signals and suggested that VLFs also occurred in
97 offshore areas. Due to the limitations of a conventional analysis, however, epicenters of VLFs in
98 offshore areas were not located. Therefore, the detailed spatial distribution of VLFs off Costa
99 Rica is still not well understood.

100 The spatial variation of slow and large regular earthquakes can reflect the spatial
101 heterogeneity of the frictional conditions on the plate boundary (e.g., Baba et al., 2020b). To clarify
102 the spatial relationship between slow and large regular earthquake distribution around the Nicoya
103 Peninsula, an accurate spatial distribution of VLFs is needed. Thus, we detected VLFs around
104 the Nicoya Peninsula using a temporary broadband seismic network from August 2004 to January
105 2006 because signals of VLFs are less attenuated than those of tremors and propagate longer

106 distances. The method is based on the matched-filter technique. Template waveforms from
107 possible VLFE locations were evaluated by numerical simulations of seismic wave propagation
108 using a regional three-dimensional (3D) velocity structure model. In addition, scaled energy is an
109 informative parameter for the rupture process of seismic phenomena (Kanamori & Rivera, 2006).
110 Although scaled energies of slow earthquakes around Japan were well investigated by previous
111 studies (e.g., Ide & Yabe, 2014; Yabe et al., 2019; 2021), those in Costa Rica was not estimated.
112 Therefore, we also estimated the seismic energy rate functions of tremors accompanied by VLFES
113 by using high frequency (2–8 Hz) seismograms to evaluate the scaled energy of slow earthquakes
114 around the Nicoya Peninsula.

115 **2. VLFE analysis**

116 **2.1. Data and method**

117 **2.1.1. Data**

118 We used waveforms of a temporary seismic network, Tomography Under Costa Rica and
119 Nicaragua (TUCAN; Abers & Fischer, 2003), recorded from August 2004 to January 2006. There
120 were 49 broadband seismic stations in four lines (Figure 1b). For the VLFE analysis, we used 14
121 stations near the Nicoya Peninsula in Costa Rica (shown in Figure 1a), because signals of VLFES
122 are relatively clear in these 14 stations and using all stations causes higher computational cost for
123 synthetic calculations. After removing instrumental responses, the seismograms for VLFE
124 detection were resampled at one sample per second. We applied a bandpass filter in the frequency
125 range of 0.02–0.05 Hz (e.g., Ghosh et al., 2015; Ito et al., 2009; Takemura et al., 2019), because
126 this frequency band is less affected by microseismic noises (e.g., Hasselmann, 1963; Kaneko et al.,
127 2018). We verified that the large amplitude surface waves are generally matched well between
128 observed and synthetic waveforms in a higher frequency range (Figure S1; 0.02-0.06 Hz).

129 **2.1.2. Matched-filter technique**

130 The detection procedure used for VLFES is similar to that used in our previous study (Baba
131 et al., 2020a). The horizontal-component seismograms of many stations were noisy; therefore, it
132 is difficult to use horizontal-component seismograms for the location of VLFES (Figure S2). Thus,
133 we used only the vertical-component seismograms for the VLFE analysis although it is usual to
134 analyze VLFES by using three-component seismograms. We placed 175 virtual source grids on
135 the Cocos Plate boundary at a uniform interval of 0.1° (Figure 2a) and computed synthetic
136 waveforms from these source grids to the stations in Costa Rica using an open-source seismic
137 wave propagation code (OpenSWPC; Maeda et al., 2017). We used a three-dimensional velocity
138 structure model constructed by combining CRUST 1.0 (Laske et al., 2013), Slab2 (Hayes et al.,
139 2018), and ETOPO1 (Amante & Eakins, 2009), setting the minimum *S*-wave velocity in the solid
140 columns to 1.0 km/s. We adopted the values of a mean oceanic slab structure (Christensen &
141 Salisbury, 1975) for the physical parameters of the subducting slab (Table S1). For the physical
142 parameters of the other layers except for the slab, we used the values of CRUST 1.0, and the default
143 parameter set of OpenSWPC. The cross-section of the structure model is shown in Figure S3. The
144 model covered the region enclosed by the red line (Figure 1b), which was discretized by a uniform
145 grid interval of 0.2 km. The assumed VLFE moment rate function was a Küpper wavelet with a
146 source duration of 15 s and an M_w of 4.0 (Figure 4 of Maeda et al., 2017). Since focal mechanisms
147 of VLFES are consistent with shear slip on the plate boundaries in previous studies (Cascadia:
148 Ghosh et al., 2015; Nankai: Ito et al., 2009; Nakano et al., 2018; Sugioka et al., 2012; Takemura
149 et al., 2019), the focal mechanism at each source grid was assumed to be consistent with the

150 geometry of the plate boundary of Slab2 and the plate motion model, NUVEL-1A (DeMets et al.,
 151 1994). The time window of each template was set to 150 s from the event origin time. Hereafter,
 152 we simply refer to these synthetic waveforms as template waveforms. Examples of template
 153 waveforms at updip and downdip source grids are shown in Figures 2b and 2c, respectively. The
 154 signal first arrives at MANS and the variation of amplitudes is small for the updip source, whereas
 155 signals first arriving at FINA exhibit amplitudes in or near the Nicoya Peninsula that are much
 156 larger than in other areas for the downdip source.

157 We then calculated cross-correlation coefficients (CCs) between the filtered template
 158 waveforms and observed seismograms every 1 s. We selected events with station-averaged
 159 coefficients larger than a threshold defined as 9.5 times the median absolute deviation (MAD) of
 160 the distributions. In order to decrease false detections by non-VLFE signals on the condition that
 161 only the vertical-component seismograms can be used and the station coverage along the azimuth
 162 direction is poor, we adopted a strict detection threshold compared to previous studies (e.g., $8 \times$
 163 MAD in Shelly et al., 2007, and Baba et al., 2018 and $9 \times$ MAD in Baba et al., 2020a). The changes
 164 of CCs when focal mechanisms or depths of assumed source models are different from the
 165 geometry of the plate boundary are shown in Figure S4.

166 2.1.3. VLFE location and discarding false detections

167 Although a strict detection threshold was employed, there are false detections that are
 168 caused by other signals, such as local or regional regular earthquakes or teleseismic events. To
 169 exclude local or regional earthquakes, we compared the origin time of detected events with a
 170 catalog of local and regional regular earthquakes constructed by El Observatorio Vulcanológico y
 171 Sismológico de Costa Rica, Universidad Nacional (Catálogo de Temblores de Costa Rica, 2004-
 172 2006; Protti, personal comm.). We discarded events whose epicentral distances were less than 150
 173 km and origin times were within ± 50 s from the local or regional earthquakes listed in this
 174 earthquake catalog. To discard false detections by teleseismic events, we removed the events
 175 detected between the *P*-wave arrivals and 600 s after *S*-wave arrivals of teleseismic events ($M_w \geq$
 176 5) in the catalog of the United States Geological Survey. The event amplitudes and CCs are
 177 positively correlated in general, but events with high amplitudes and low average CCs occasionally
 178 appear. These events are considered to be false detections due to teleseismic events absent in the
 179 catalogs. Therefore, we did not count events with average CCs below 0.56 and relative amplitudes
 180 to templates higher than 0.4 (Baba et al., 2018; 2020a). If the amplitude relative to the template
 181 with M_w of 4.0 was smaller than 0.05, we did not count the event because the signal was too small
 182 to judge whether the event is truly existed or not.

183 For the remaining events, we calculated the variance reduction (VR) between the template
 184 and observed waveforms. We estimated VRs using only the vertical-component seismograms of
 185 relatively quiet stations in and around the Nicoya Peninsula (MANS, CABA, FINA, CRUP, and
 186 PALM), because amplitude differences between updip and downdip events are large in these
 187 stations:

$$188 \quad VR = \left[1 - \frac{\sum_i \int \{f_i(t) - cg_i(t)\}^2 dt}{\sum_i \int \{f_i(t)\}^2 dt} \right] \times 100\% , \quad (1)$$

189 where $f_i(t)$ and $g_i(t)$ are the observed and template waveforms at the i -th station, respectively,
 190 and c is the relative amplitude of the observed waveform to the template. We selected events whose
 191 VRs were larger than 30%. This threshold is set by trial and error based on visual identifications
 192 of VLFEs in the observed data.

193 After the above procedures, falsely detected events still remained because we only used the
194 vertical-component seismograms, and the array configuration was cross shaped. To discard the
195 remaining false detections, we estimated the normalized-and-stacked amplitude, azimuth, and
196 velocity of signal propagation by applying delay-and-sum beamforming (Section 3.1 of Rost &
197 Thomas, 2002; Walter et al., 2013) to vertical-component seismograms. After normalizing the
198 waveform of each station by its maximum amplitude in the 150 s time window, we searched for
199 the azimuth and velocity that maximized the stacked amplitude by performing a grid search for
200 the azimuth between 135–315° with 1° intervals and the velocity between 2–5 km/s with 0.1 km/s
201 intervals. We first used the along-strike stations in both Costa Rica and Nicaragua (brown inverted
202 triangles in Figure 1b) to discard teleseismic events. The amplitudes of Costa Rican VLFs at the
203 Nicaraguan stations are generally very small compared with those in the Costa Rican stations due
204 to geometrical spreading, but amplitudes for teleseismic events are similar. Therefore, we selected
205 events whose stacked normalized amplitude normalized by the number of stations was smaller
206 than 0.6 because events with large stacked signals are suspected to be teleseismic earthquakes
207 (Figure S5). We then conducted another beamforming analysis for the remaining events using the
208 same stations as the matched-filter analysis, and selected events whose azimuth was 200–230°.
209 Finally, to avoid duplicate detection, only one event was counted every 60 s from the remaining
210 VLFE candidates. We only counted the event whose averaged CC was the highest
211 spatiotemporally.

212 **2.1.4. Estimation of the moments of events**

213 We estimated the source durations of detected VLFs by comparing template waveforms
214 with source durations of 10–50 s with observed waveforms (e.g., Yabe et al., 2021). The M_w of
215 the templates was set to be 4.0. The source duration that resulted in the highest values of CC
216 between the observed and template waveforms was adopted.

217 We also calculated the amplitude of an event relative to the template waveforms using the
218 same method as Baba et al. (2020b). The relative amplitude can be used to calculate the seismic
219 moment of each VLFE. The seismic moment rate of a VLFE was calculated by dividing its seismic
220 moment by its source duration. To evaluate the estimation error of moment rates of VLFs, we
221 calculated moment rates by assuming the various source durations whose CCs between synthetic
222 and observed waveforms are more than 90% of the maximum CC. Although there are errors in the
223 order of 0.2, we verified that the order of moment rates does not change (Figure S6).

224 **2.2. Results**

225 We detected 68 VLFs during the analysis period. Example traces of a VLFE located at
226 85.8°W and 9.4°N are shown in Figure 3. The signal of this VLFE first arrives at MANS and
227 propagates to inland stations (top panel of Figure 3). This feature was successfully modeled for
228 the updip templates (Fig. 2b). There is a tremor signal in the frequency range of 2–8 Hz in the
229 same time window (middle and bottom panels of Figure 3). The cumulative number of VLFs
230 showed significant increases in September 2004 and August 2005 (Figure 4a). In August 2005, an
231 SSE was reported by Jiang et al. (2012); therefore, SSE and VLFE activities were temporally
232 correlated. The M_w and source duration of VLFs in Costa Rica were mainly distributed in 3.4–
233 4.2 and 10–30 s, respectively (Figures 5a, b). The M_w and source duration of VLFs have a
234 positive correlation (Figure 5c) like shallow VLFs in Nankai, Japan (Sugioka et al., 2012;
235 Takemura et al., 2019). The relationship between durations and magnitudes of VLFs and SSEs

236 (Jiang et al., 2012; Voss et al., 2017) in Costa Rica is closer to the range inferred from the scaling
237 law of slow earthquakes than that of regular earthquakes by Ide et al. (2007) (Figure 5c).

238 Most of the VLFs (62 events) are distributed where the plate boundary is at a depth range
239 of 6–10 km below the sea level, near the trench axis off the Nicoya Peninsula (Figure 4b), at the
240 updip of the seismogenic zone. The distribution of these VLFs is consistent with the VLFs in
241 2008 suggested by Walter et al. (2013). When locating some events using both vertical and
242 horizontal-component seismograms whose signal to noise (SN) ratios are relatively high for the
243 verification of the analysis by using vertical-component seismograms only, the high CC areas
244 overlap and the epicenters were also located near the trench axis, although there are differences of
245 0.1–0.2° (Figure S2). The area overlaps with the shallower part of the large slip area of the 2007
246 SSE (Jiang et al., 2017) or summed SSE slip in 2007–2012 (Dixon et al., 2014). Although the slip
247 distribution of the 2005 SSE was not estimated in previous studies, our results suggest that the
248 2005 SSE can also have a large slip area near the trench axis, similar to the 2007 SSE. The
249 distribution of VLFs lies within the gap between large slip areas of thrust-type large interplate
250 earthquakes with an M_w of 7–8 around the Nicoya Peninsula and the 1992 tsunami earthquake
251 with an M_w of 7.6. The distribution of VLFs also separated from the afterslip area of the 2012
252 M_w 7.6 earthquake (Malservisi et al., 2015).

253 The distribution of the CC shows the resolution of the location of VLFs. By the
254 distribution of CC, it is confirmed that most of the VLFs were located near the trench axis. CCs
255 for more than half of the events exceeded the threshold only for updip templates (Figure 6a). For
256 several events, CCs exceeded the threshold both updip and downdip of the seismogenic zone with
257 a larger CC in the updip region. The area where CCs are more than 90% of the maximum CC is
258 concentrated only in the updip area (Figure 6b). On the other hand, 6 VLFs were located at a
259 depth of ~40 km at the downdip of large earthquakes (Figure 4b). Although focal mechanisms may
260 not be thrust-type and the areas where CCs are larger than the threshold are widely distributed, we
261 verified that regular earthquakes listed in the earthquake catalog by El Observatorio Vulcanológico
262 y Sismológico de Costa Rica in the updip and downdip areas are located in the updip and downdip
263 areas respectively by this method (Figure S7). However, we cannot exclude the possibility that
264 such VLFs occur in the updip region in real because, in such cases, bimodal CC distributions
265 tend to appear both in the updip and downdip (Figure 6c). Of course, there is a possibility that such
266 VLFs really occur in the downdip region because the locations of such VLFs were near the
267 locations of previously reported LFs (Brown et al. 2009) and tremors (Outerbridge et al. 2010).
268 In this study, the SN ratios of VLFs detected in the downdip region are very low; hence, it is
269 difficult to judge whether such VLFs occur in downdip or updip, because it is hard to judge which
270 station the signal of the VLF arrival first due to the similar arrival times at updip stations. The
271 reason for the small number and the low SN ratio of downdip events may be that slow earthquakes
272 in the downdip region were inactive during 1.5 years of the temporary array. To investigate
273 whether deep VLFs really exist, an analysis with a longer dataset is needed in future work.

274 **3. Estimations of seismic energy rates for tremors accompanied by VLFs**

275 **3.1. Data and method**

276 Tremor signals were also found in the frequency range of 2–8 Hz within the time windows
277 of detected VLFs (middle panel of Figure 3; Figure S8). It is difficult to locate tremors in the
278 offshore region by using an onshore network because sources of tremors are distant from the
279 network and signals of tremors attenuate strongly compared to VLF (0.02–0.05 Hz) signals.

280 Based on the spatiotemporal correlation between VLFs and tremors reported in other regions
 281 (e.g., Ghosh et al., 2015; Maeda & Obara, 2009; Tamaribuchi et al., 2019) and the interpretation
 282 that VLFs and tremors are components of broadband slow earthquake phenomena (Gomberg et
 283 al., 2016; Hawthorne & Bartlow, 2018; Ide & Maury, 2018), we estimated the energy rate functions
 284 of tremors accompanied by VLFs by assuming that a tremor occurs at the same location as the
 285 VLFE, i.e., the VLFE source grid with the highest CC as written in Section 2.1.3 (e.g., Yabe et al.,
 286 2021). We simulated the waveforms at the location of a VLFE using the same model which is
 287 described in Section 2.1.2 but discretized by a finer grid interval (0.04 km). The simulated
 288 envelope shapes are different from observed ones due to a simple pulse source time function
 289 (details in the caption of Figure S9), but the arrival times of maximum *S*-wave amplitudes in the
 290 frequency range of 2–8 Hz are consistent with observed tremor waveforms (Figure S9). The
 291 interval of source grids for the VLFE detection was set as 0.1°, therefore, we supposed that a VLFE
 292 and the corresponding tremor occurred at the same location in the order of 10 km.

293 We also used waveforms of the TUCAN network similarly to the VLFE detection. After
 294 applying a bandpass filter of 2–8 Hz, the envelope waveforms were calculated by taking the root-
 295 mean-square of sums of three-component squared seismograms and a smoothing time window of
 296 3 s (bottom panel of Figure 3). The envelope waveforms were resampled at one sample per second.

297 3.1.1. Quality factor of the apparent *S*-wave attenuation

298 To estimate the energy rate functions of tremors accurately, we estimated the quality factor
 299 of the apparent *S*-wave attenuation (Q_{app}), based on the coda-normalization method (e.g., Aki,
 300 1980; Yoshimoto et al., 1993). First, we selected some isolated regular earthquakes (Figure S10).
 301 To eliminate the effect of differences in source size and site amplification, observed maximum *S*-
 302 wave amplitudes were normalized by averaged coda amplitudes within a lapse time of 80–90 s.
 303 The coda-normalized maximum *S*-wave amplitude of the *i*-th earthquake at the *j*-th station (A_{ij})
 304 and the distance between the hypocenter of the *i*-th earthquake and *j*-th station (L_{ij}) have the
 305 following relationship (Takemura et al., 2017):

$$306 \quad \ln(L_{ij}A_{ij}) = -\frac{\pi f_c Q_{app}^{-1}}{V_s} L_{ij} + C', \quad (2)$$

307 where V_s is the *S*-wave velocity (assuming 3.5 km/s in this study; Maeda & Obara, 2009; Yabe et
 308 al., 2019; 2021), f_c is the central frequency (assuming 5 Hz in this study), and C' is a constant. By
 309 solving Equation (2) by the least-squares method, we estimated Q_{app}^{-1} as $10^{-2.42}$ (Figure 7a).

310 3.1.2. Site amplification factor

311 We estimated the site amplification factor at 2–8 Hz using relative coda amplitudes (e.g.,
 312 Maeda and Obara, 2009). Coda amplitudes at a certain time window generally depend on the
 313 source size and site amplification (e.g., Chapters 2 and 3 of Sato et al., 2012). Therefore, the ratio
 314 of the coda wave amplitude at a station to that at a reference station for the same event depends
 315 only on the site amplification factor relative to a reference station.

316 We calculated the ratios of the coda amplitudes for each station to those of MANS
 317 (reference station) for each regular earthquake used in Section 3.1. The time window for evaluating
 318 relative coda amplitudes is the same as that in coda-normalization in Section 3.1. Then we
 319 calculated the average of the coda amplitude ratios of all earthquakes for each station. The
 320 estimated relative site amplification factors at each station used in the estimations of the energy
 321 rate functions of tremors are shown in Figure 7b. We compared coda amplitudes of regular

322 earthquakes at MANS with those at the JTS, a permanent station of the Global Seismograph
 323 Network by Incorporated Research Institutions for Seismology and International Deployment of
 324 Accelerometers (Scripps Institution of Oceanography, 1986). The average ratio of coda amplitudes
 325 at MANS to those at JTS is 1.14, suggesting that the condition of MANS site is very similar to that
 326 of the JTS.

327 3.1.3. Seismic energy rate of tremors

328 By using apparent attenuation (Q_{app}^{-1}) and site amplification in the previous subsections,
 329 we estimated the energy rate functions of tremors. The source energy rate function of a tremor
 330 ($E_j(t)$) using the amplitude of the j -th station is calculated by the following formula (Maeda &
 331 Obara, 2009):

$$332 E_j(t) = 2\pi V_S r_j^2 \rho A_j'^2(t + t_j) \exp(2\pi f_c Q_{app}^{-1} t_j), \quad (3)$$

333 where $A_j'(t)$ is the site-corrected amplitude of the envelope waveform of the j -th station, r_j is the
 334 hypocentral distance from the accompanying VLFE, t_j is the travel time from the VLFE source,
 335 and ρ is the density (assuming 2,700 kg/m³). For calculating $E_j(t)$, we used a 180 s time window
 336 that started 60 s before the origin time of VLFES. We calculated the CCs of all station pairs in
 337 Figure 7b. The range of CCs of each pair is 0.5–0.85 for the event of Figure 3 (Figure S11). To
 338 estimate the source energy rate function of the tremor, we only used stations whose CCs with at
 339 least one other station exceeded 0.6.

340 The seismic energy rate W_j using the amplitude of the j -th station is given by the integration
 341 of the source energy rate function $E_j(t)$ in time:

$$342 W_j = \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} E_j(t) dt, \quad (4)$$

343 where t_1 and t_2 are the start and end of the integration range, respectively. The integration range is
 344 defined as the period in which the values of $E_j(t)$ exceeded 20% of the maximum value of $E_j(t)$
 345 (Figure 8). The seismic energy rate of a tremor (W_0) was obtained by calculating the average W_j
 346 of all stations. The error of W_0 was obtained by calculating the standard deviation of W_j .

347 3.2. Results

348 For 13 of 68 VLFES, there were no station pairs whose CCs were larger than 0.6 when
 349 estimating the energy rates of accompanying tremors, because such tremors may not be detected
 350 by technical limitations or tremors and VLFES may be distinct phenomena. We, therefore,
 351 estimated energy rates of 55 tremors. The energy rates of tremors were mainly distributed in 10^3 –
 352 $10^{5.5}$ J/s (Figure 9). There is a positive correlation between the energy rates of tremors and the
 353 moment rates of the corresponding VLFES. We estimated the scaled energy by calculating the ratio
 354 between the seismic energy rate of a tremor and the seismic moment rate of the corresponding
 355 VLFE. The scaled energy of slow earthquakes off Costa Rica is mainly distributed in the range of
 356 10^{-9} – 10^{-8} (dotted lines in Figure 9).

357 4. Discussion

358 4.1. Shallow ETS off Costa Rica

359 As shown in Figure 3 and Figure S8, VLFES and tremors often were temporally correlated.
 360 The activation of VLFES and tremors in August 2005 temporally correlates with the 2005 SSE
 361 reported by Jiang et al. (2012). VLFES and tremors occurred mainly in the updip area in August

362 2005; hence, the slip area of the 2005 SSE can be distributed in the updip area near the trench axis,
363 similar to the 2007 SSE. In areas where shallow VLFs occurred, subseafloor hydrological
364 observatories recorded pore fluid pressure transients in 2000 (Brown et al., 2005), 2003–2004
365 (Solomon et al., 2009), and 2007–2013 (Davis et al., 2011; 2015). They interpreted that pore fluid
366 pressure transients were caused by SSEs. Spatial correspondence of pore fluid change in the
367 periods of previous studies and VLFE activity in 2005 near the trench off Costa Rica suggests the
368 occurrence of a shallow ETS, as with the Nankai subduction zone (Araki et al., 2017; Nakano et
369 al., 2018).

370 **4.2. Heterogeneity of the frictional property on the plate boundary**

371 To discuss the heterogeneity of the frictional property on the plate boundary, we compare
372 the differences of stress drops and interplate coupling between the VLFE area and the seismogenic
373 zone in the Central American subduction zone. In this study, we showed that most of VLFs were
374 located at a depth range of 6–10 km on the plate boundary, which is updip of the seismogenic zone.
375 The stress drop of VLFs in the Nankai subduction zone was estimated to be 0.1–10 kPa (Ito &
376 Obara, 2006), therefore we expect that the stress drop of VLFs in Costa Rica is similar. This is
377 much smaller than the stress drop of earthquakes in the tsunami earthquake rupture area (1.2 MPa;
378 Bilek et al., 2016). In addition, the interplate coupling was estimated to be weak at a depth range
379 of 6–10 km (Feng et al., 2012), and strong in the seismogenic zone at a deeper depth than 10 km
380 (Protti et al., 2014).

381 The spatial variation of stress drops and interplate coupling at the plate boundary results
382 from the heterogeneous distribution of frictional properties at the plate boundary in the Central
383 American subduction zone. In addition, a low stress drop suggests a high pore pressure generated
384 by the existence of fluids (Yao & Yang, 2020). Therefore, the frictional strength of the slow
385 earthquake area at a depth range of 6–10 km can be quite weak owing to the rich fluid compared
386 to that in the regions with regular and tsunami earthquakes.

387 In Costa Rica, repeating earthquakes occur around the large coseismic slip area of the 2012
388 M_w 7.6 earthquake on the Nicoya Peninsula (Chaves et al., 2020). In this study, VLFs were
389 mainly located near the trench axis, which is spatially separated from the locations of repeating
390 earthquakes that occur near the Nicoya Peninsula. Such spatial separation of slow and repeating
391 earthquakes on the plate boundary is also found in the Nankai (e.g., Takemura et al., 2020) and the
392 Tohoku subduction zone (e.g., Nishikawa et al., 2019).

393 **4.3. Comparison with other subduction zones**

394 Our study revealed that shallow VLFs and tremors occur near the trench axis off Costa
395 Rica, in the updip of coseismic slip areas of thrust-type large earthquakes with an M_w of 7–8. In
396 the updip area, SSEs also occurred in 2007–2012 (Dixon et al., 2017; Jiang et al., 2012). The depth
397 range and the separate distribution between shallow slow earthquakes and large earthquakes off
398 Costa Rica are similar to shallow slow earthquakes in the Nankai subduction zone, where slow
399 earthquakes are spatially separated from high slip-deficit zones (e.g., Takemura et al., 2020). On
400 the other hand, before the 2011 Tohoku earthquake, shallow slow slip events propagated to the
401 initial rupture point of the great earthquake (Kato et al., 2012). Therefore, the characteristics of
402 distribution of slow and large earthquakes differ between Tohoku and Costa Rica.

403 There are other common features in shallow slow earthquakes between Costa Rica and
404 Nankai. Although the lower limit of M_w is large (~ 3.4) due to a strict threshold, the ranges of

405 magnitudes and source durations of shallow VLFs off Costa Rica are similar to those of shallow
406 VLFs in the Nankai subduction zones (e.g., Takemura et al., 2019). The recurrence intervals of
407 activation of slow earthquakes are one to several years in Costa Rica (Jiang et al., 2012), which is
408 similar to shallow slow earthquakes in the Nankai subduction zone, but different from the shorter
409 intervals of deep slow earthquakes in Nankai (e.g., Baba et al., 2020b). Although the tremor
410 analysis is limited due to the missing of small events by the strict threshold of VLFs, the range
411 of energy rates of tremors was 10^3 – $10^{5.5}$ J/s. The upper limit of the energy rate range of tremors is
412 similar to that observed for shallow tremors in Nankai (Yabe et al., 2019). The estimated scaled
413 energy of slow earthquakes off Costa Rica is also similar to that of shallow slow earthquakes in
414 the Nankai subduction zone (Yabe et al., 2019). The scaled energy is related to the rupture process
415 of seismic phenomena (Kanamori & Rivera, 2006); therefore, these results suggest that the
416 frictional properties within the shallow slow earthquake areas are similar in both Costa Rica and
417 Nankai. On the other hand, the scaled energy range in both regions is 0.5–1 orders of magnitude
418 larger than that of shallow slow earthquakes in the Tohoku subduction zone (Yabe et al., 2021),
419 and approximately 1 order of magnitude larger than that of deep slow earthquakes in Nankai (Ide
420 et al., 2008; Ide & Yabe, 2014; Ide, 2016; Ide & Maury, 2018; Maeda & Obara, 2009) (Figure 9).
421 We note that scaled energies of shallow slow earthquakes were estimated for individual events,
422 whereas those of deep slow earthquakes estimated by Ide & Yabe (2014), Ide (2016), and Ide &
423 Maury (2018) were estimated for stacked events.

424 The range of scaled energy and distribution of shallow slow earthquakes off Costa Rica are
425 more similar to those in shallow Nankai than shallow Tohoku. According to Syracuse et al. (2010),
426 the age and thermal parameters of Costa Rica are 15.8 Ma and 1,010 km, respectively, which are
427 closer to those of Nankai (20.0 Ma and 450 km, respectively) than Tohoku (115.2–130.5 Ma and
428 5,720–6,040 km, respectively). The thermal parameter, which is product of the incoming plate age,
429 the convergence rate, and the sine of the slab dip angle, is used to predict the slab surface
430 temperature at a given depth (e.g., Kirby et al., 1991; Syracuse et al., 2010). In addition, the
431 temperatures of shallower parts of plate interfaces of these subduction zones where shallow slow
432 earthquakes are not so different (Nankai: ~ 100 °C in the depth range of 0–5 km from the seafloor;
433 Tohoku: 65–110 °C in the depth range of 6–12 km; and Costa Rica: 12–60°C in the depth range of
434 0–10 km; modeled temperature in Saffer & Wallace, 2015). On the other hand, the Central
435 American subduction zone is subduction of fast convergence rate (~ 8 cm/year; DeMets et al.,
436 1994), high dip angle, and erosional type (e.g., Bangs et al., 2016), which are more similar to
437 Tohoku than Nankai. Although the characteristics of slow earthquake activity can be related to
438 various factors, the thermal parameter and incoming plate age of Costa Rica is more similar to
439 Nankai than Tohoku. The temperature structure of the shallow plate interface is probably most
440 sensitive to incoming plate age (Maunder et al., 2019) and secondarily to thermal parameter
441 (Syracuse et al., 2010). Hence, similar temperature conditions on the interface may explain the
442 common features of shallow slow earthquakes off Costa Rica and in Nankai.

443 In previous studies, the large slip area of the SSE in 2007 was separated into deeper and
444 shallower parts (Jiang et al., 2017), and deep LFEs and tremors were detected downdip of the
445 seismogenic zone (Brown et al., 2009; Outerbridge et al., 2010). And, several VLFs were located
446 in the downdip area, in the similar area reported in previous studies of tremors and LFEs. If these
447 deep VLFs, LFEs and tremors occur in the downdip area, slow earthquakes might occur at
448 separate depths along both shallower and deeper extensions of rupture zones of large earthquakes
449 (Figure 10). This characteristic might also be the same as that of the Nankai subduction zone
450 (Obara & Kato, 2016). This suggests that the tectonic property may be similar in the wide depth

451 range in Costa Rica and Nankai. On the other hand, slow earthquakes are distributed only in the
452 deeper part in the Cascadia subduction zone and only in the shallower part in the Tohoku
453 subduction zone. The variation of the distribution of slow earthquakes may be attributed to the
454 difference in tectonics or detection capability. The elucidation of the reason for the difference of
455 the distribution in slow earthquake is future works.

456 **5. Conclusions**

457 Based on the grid-search matched-filter technique using synthetic templates in the regional
458 3D model, we detected and located VLFs around the Nicoya Peninsula. Many VLFs occurred
459 in September 2004 and August 2005, and more than 90% of the VLFs were located near the
460 trench axis, where the plate boundary is at a depth range of 6–10 km, updip of the seismogenic
461 zone, whereas several VLFs were located in the downdip area at a depth of ~40 km. In this area,
462 the occurrence of shallow SSEs is suggested by VLFE episodes. The region with VLFE activity
463 overlaps with the shallower part of the large slip area of the 2007 SSE; therefore, the occurrences
464 of shallow SSEs are suggested in September 2004 and August 2005 to occur in the same area as
465 the shallower part of the 2007 SSE. The distribution of VLFs lies in the gap surrounding
466 coseismic slip areas of tsunami and large regular earthquakes. This separation reflects the spatial
467 distribution of the frictional strength of the plate boundary in the Central American subduction
468 zone. By using high-frequency seismogram envelopes, we also estimated the energy rates of
469 tremors accompanying VLFs. The ranges of magnitude and source duration of VLFs, energy
470 rate of tremors, and scaled energy off Costa Rica are similar to those in shallow slow earthquakes
471 in the Nankai subduction zone.

472 **Data Availability**

473 We used seismograms of the TUCAN network (Abers & Fischer, 2003;
474 https://doi.org/10.7914/SN/YO_2003) and Global Seismograph Network (Scripps Institution of
475 Oceanography, 1986; <https://doi.org/10.7914/SN/II>). We used the earthquake catalog of the U.S.
476 Geological Survey (<https://earthquake.usgs.gov/earthquakes/search/>). We used OpenSWPC code
477 Version 5.0.2 (Maeda et al., 2017; <https://doi.org/10.5281/zenodo.3712650>) for the numerical
478 simulations. Numerical simulations were conducted using the Fujitsu PRIMERGY
479 CX600M1/CX1640M1 (Oakforest-PACS) at the Information Technology Center, the University
480 of Tokyo. We used generic mapping tools (Wessel et al., 2013) and Seismic Analysis Code
481 (Helfrich et al., 2013) to prepare the figures and process seismograms, respectively. The VLFE
482 and tremor catalog constructed by this study is provided in an open access repository, zenodo (doi:
483 [10.5281/zenodo.4435232](https://doi.org/10.5281/zenodo.4435232)).

484 **Acknowledgements**

485 We would like to thank the Editor Rachel Abercrombie, the Associate Editor Elisa Tinti,
486 Alexandra A. Hutchison and two anonymous reviewers for their valuable comments and
487 suggestions. We would like to thank Suguru Yabe for valuable discussions. We would also like to
488 thank Marino Protti for providing the earthquake catalog in Costa Rica and for discussions. We
489 thank Editage (www.editage.com) for English proofreading. This research was supported by JSPS
490 KAKENHI Grant in Science Research on Innovative Areas “Science of Slow Earthquakes”
491 (JP16H06473) and JSPS Research Fellowship DC1 (JP19J20760). This study was also supported
492 by the ERI-JURP 2020-S-04.

493 **References**

- 494 Abers, G. A., & Fischer, K. M. (2003). Tomography Under Costa Rica and Nicaragua.
 495 International Federation of Digital Seismograph Networks.
 496 https://doi.org/10.7914/SN/YO_2003
- 497 Aki, K. (1980). Attenuation of shear-waves in the lithosphere for frequencies from 0.05 to 25 Hz.
 498 *Physics of the Earth and Planetary Interiors*, 21(1), 50–60. [https://doi.org/10.1016/0031-](https://doi.org/10.1016/0031-9201(80)90019-9)
 499 [9201\(80\)90019-9](https://doi.org/10.1016/0031-9201(80)90019-9)
- 500 Amante, C., & Eakins, B.W. (2009). ETOPO1 1 Arc-Minute Global Relief Model: Procedures,
 501 Data Sources and Analysis. NOAA Technical Memorandum NESDIS NGDC-24.
 502 <https://doi.org/10.7289/V5C8276M>
- 503 Araki, E., Saffer, D. M., Kopf, A. J., Wallace, L. M., Kimura, T., Machida, Y., Ide, S., Davis, E.,
 504 & IODP Expedition 365 shipboard scientists (2017). Recurring and triggered slow-slip
 505 events near the trench at the Nankai Trough subduction megathrust. *Science*, 356(6343),
 506 1157–1160. <https://doi.org/10.1126/science.aan3120>
- 507 Baba, S., Takeo, A., Obara, K., Kato, A., Maeda, T., & Matsuzawa, T. (2018). Temporal
 508 Activity Modulation of Deep Very Low Frequency Earthquakes in Shikoku, Southwest
 509 Japan. *Geophysical Research Letters*, 45(2), 733–738.
 510 <https://doi.org/10.1002/2017GL076122>
- 511 Baba, S., Takeo, A., Obara, K., Matsuzawa, T., & Maeda, T. (2020a). Comprehensive Detection
 512 of Very Low Frequency Earthquakes Off the Hokkaido and Tohoku Pacific Coasts,
 513 Northeastern Japan. *Journal of Geophysical Research: Solid Earth*, 125(1), 1–13.
 514 <https://doi.org/10.1029/2019JB017988>
- 515 Baba, S., Takemura, S., Obara, K., & Noda, A. (2020b). Slow Earthquakes Illuminating
 516 Interplate Coupling Heterogeneities in Subduction Zones. *Geophysical Research Letters*,
 517 47(14), 4–5. <https://doi.org/10.1029/2020GL088089>
- 518 Bangs, N. L., McIntosh, K. D., Silver, E. A., Kluesner, J. W., & Ranero, C. R. (2016). A recent
 519 phase of accretion along the southern Costa Rican subduction zone. *Earth and Planetary*
 520 *Science Letters*, 443, 204–215. <https://doi.org/10.1016/j.epsl.2016.03.008>
- 521 Bilek, S. L., Rotman, H. M. M., & Phillips, W. S. (2016). Low stress drop earthquakes in the
 522 rupture zone of the 1992 Nicaragua tsunami earthquake. *Geophysical Research Letters*,
 523 43(19), 10,180–10,188. <https://doi.org/10.1002/2016GL070409>
- 524 Brown, J. R., Beroza, G. C., Ide, S., Ohta, K., Shelly, D. R., Schwartz, S. Y., et al. (2009). Deep
 525 low-frequency earthquakes in tremor localize to the plate interface in multiple subduction
 526 zones. *Geophysical Research Letters*, 36(19), 1–5. <https://doi.org/10.1029/2009GL040027>
- 527 Brown, K. M., Tryon, M. D., DeShon, H. R., Dorman, L. R. M., & Schwartz, S. Y. (2005).
 528 Correlated transient fluid pulsing and seismic tremor in the Costa Rica subduction zone.
 529 *Earth and Planetary Science Letters*, 238(1–2), 189–203.
 530 <https://doi.org/10.1016/j.epsl.2005.06.055>
- 531 Chaves, E. J., Schwartz, S. Y., & Abercrombie, R. E. (2020). Repeating earthquakes record fault
 532 weakening and healing in areas of megathrust postseismic slip. *Science Advances*, 6(32),
 533 eaaz9317. <https://doi.org/10.1126/sciadv.aaz9317>
- 534 Christensen, N. I., & Salisbury, M. H. (1975). Structure and constitution of the lower oceanic
 535 crust. *Reviews of Geophysics*, 13(1), 57–86. <https://doi.org/10.1029/RG013i001p00057>
- 536 Davis, E., Heesemann, M., & Wang, K. (2011). Evidence for episodic aseismic slip across the
 537 subduction seismogenic zone off Costa Rica: CORK borehole pressure observations at the

- 538 subduction prism toe. *Earth and Planetary Science Letters*, 306(3–4), 299–305.
539 <https://doi.org/10.1016/j.epsl.2011.04.017>
- 540 Davis, E. E., Villinger, H., & Sun, T. (2015). Slow and delayed deformation and uplift of the
541 outermost subduction prism following ETS and seismogenic slip events beneath Nicoya
542 Peninsula, Costa Rica. *Earth and Planetary Science Letters*, 410, 117–127.
543 <https://doi.org/10.1016/j.epsl.2014.11.015>
- 544 DeMets, C., Gordon, R. G., Argus, D. F., & Stein, S. (1994). Effect of recent revisions to the
545 geomagnetic reversal time scale on estimates of current plate motions. *Geophysical
546 Research Letters*, 21(20), 2191–2194. <https://doi.org/10.1029/94GL02118>
- 547 Dixon, T. H., Jiang, Y., Malservisi, R., McCaffrey, R., Voss, N., Protti, M., & Gonzalez, V.
548 (2014). Earthquake and tsunami forecasts: Relation of slow slip events to subsequent
549 earthquake rupture. *Proceedings of the National Academy of Sciences of the United States
550 of America*, 111(48), 17039–17044. <https://doi.org/10.1073/pnas.1412299111>
- 551 Dragert, H., Wang, K., James, T. S. (2001). A Silent Slip Event on the Deeper Cascadia
552 Subduction Interface. *Science*, 292(5521), 1525–1528.
553 <https://doi.org/10.1126/science.1060152>
- 554 Feng, L., Newman, A. V., Protti, M., Gonzalez, V., Jiang, Y., & Dixon, T. H. (2012). Active
555 deformation near the Nicoya Peninsula, northwestern Costa Rica, between 1996 and 2010:
556 Interseismic megathrust coupling. *Journal of Geophysical Research: Solid Earth*, 117(6),
557 1–23. <https://doi.org/10.1029/2012JB009230>
- 558 Ghosh, A., Huesca-Pérez, E., Brodsky, E., & Ito, Y. (2015). Very low frequency earthquakes in
559 Cascadia migrate with tremor. *Geophysical Research Letters*, 42(9), 3228–3232.
560 <https://doi.org/10.1002/2015GL063286>
- 561 Gombert, J., Wech, A., Creager, K., Obara, K., & Agnew, D. (2016). Reconsidering earthquake
562 scaling. *Geophysical Research Letters*, 43(12), 6243–6251.
563 <https://doi.org/10.1002/2016GL069967>
- 564 Hawthorne, J. C., & Bartlow, N. M. (2018). Observing and Modeling the Spectrum of a Slow
565 Slip Event. *Journal of Geophysical Research: Solid Earth*, 123(5), 4243–4265.
566 <https://doi.org/10.1029/2017JB015124>
- 567 Hasselmann, K. (1963). A statistical analysis of the generation of microseisms. *Reviews of
568 Geophysics*, 1, 177–209. <https://doi.org/10.1029/RG001i002p00177>
- 569 Hayes, G. P., Moore, G. L., Portner, D. E., Hearne, M., Flamme, H., Furtney, M., & Smoczyk,
570 G. M. (2018). Slab2, a Comprehensive Subduction Zone Geometry Model, *Science*,
571 61(October), 58–61. <https://doi.org/10.1126/science.aat4723>
- 572 Helffrich, G., Wookey, J., & Bastow, I. (2013). *The Seismic Analysis Code*. Cambridge:
573 Cambridge University Press. <https://doi.org/10.1017/CBO9781139547260>
- 574 Hutchison, A. A. (2020). Interepisodic Tremor and Slip Event Episodes of Quasi-
575 spatiotemporally Discrete Tremor and Very Low Frequency Earthquakes in Cascadia
576 Suggestive of a Connective Underlying, Heterogeneous Process. *Geophysical Research
577 Letters*, 47(3), 1–7. <https://doi.org/10.1029/2019GL086798>
- 578 Hutchison, A. A., & Ghosh, A. (2016). Very low frequency earthquakes spatiotemporally
579 asynchronous with strong tremor during the 2014 episodic tremor and slip event in
580 Cascadia. *Geophysical Research Letters*, 43(13), 6876–6882.
581 <https://doi.org/10.1002/2016GL069750>

- 582 Hutchison, A. A., & Ghosh, A. (2019). Repeating VLFs During ETS Events in Cascadia Track
583 Slow Slip and Continue Throughout Inter-ETS Period. *Journal of Geophysical Research:*
584 *Solid Earth*, 124(1), 554–565. <https://doi.org/10.1029/2018JB016138>
- 585 Ide, S. (2016). Characteristics of slow earthquakes in the very low frequency band: Application
586 to the Cascadia subduction zone. *Journal of Geophysical Research: Solid Earth*, 121(8),
587 5942–5952. <https://doi.org/10.1002/2016JB013085>
- 588 Ide, S., & Maury, J. (2018). Seismic Moment, Seismic Energy, and Source Duration of Slow
589 Earthquakes: Application of Brownian slow earthquake model to three major subduction
590 zones. *Geophysical Research Letters*, 45(7), 3059–3067.
591 <https://doi.org/10.1002/2018GL077461>
- 592 Ide, S., & Yabe, S. (2014). Universality of slow earthquakes in the very low frequency band.
593 *Geophysical Research Letters*, 41(8), 2786–2793. <https://doi.org/10.1002/2014GL059712>
- 594 Ide, S., Beroza, G. C., Shelly, D. R., & Uchide, T. (2007). A scaling law for slow earthquakes.
595 *Nature*, 447(7140), 76–79. <https://doi.org/10.1038/nature05780>
- 596 Ide, S., Imanishi, K., Yoshida, Y., Beroza, G. C., & Shelly, D. R. (2008). Bridging the gap
597 between seismically and geodetically detected slow earthquakes. *Geophysical Research*
598 *Letters*, 35(10), 2–7. <https://doi.org/10.1029/2008GL034014>
- 599 Ito, Y., Obara, K., Shiomi, K., Sekine, S., & Hirose, H. (2007). Slow Earthquakes Coincident
600 with Episodic Tremors and Slow Slip Events. *Science*, 315(5811), 503–506.
601 <https://doi.org/10.1126/science.1134454>
- 602 Ito, Y., & Obara, K. (2006). Very low frequency earthquakes within accretionary prisms are very
603 low stress-drop earthquakes. *Geophysical Research Letters*, 33(9), 1–4.
604 <https://doi.org/10.1029/2006GL025883>
- 605 Ito, Y., Obara, K., Matsuzawa, T., & Maeda, T. (2009). Very low frequency earthquakes related
606 to small asperities on the plate boundary interface at the locked to aseismic transition.
607 *Journal of Geophysical Research: Solid Earth*, 114(11), 1–16.
608 <https://doi.org/10.1029/2008JB006036>
- 609 Ito, Y., Hino, R., Kido, M., Fujimoto, H., Osada, Y., Inazu, D., et al. (2013). Episodic slow slip
610 events in the Japan subduction zone before the 2011 Tohoku-Oki earthquake.
611 *Tectonophysics*, 600, 14–26. <https://doi.org/10.1016/j.tecto.2012.08.022>
- 612 Jiang, Y., Wdowinski, S., Dixon, T. H., Hackl, M., Protti, M., & Gonzalez, V. (2012). Slow slip
613 events in Costa Rica detected by continuous GPS observations, 2002–2011. *Geochemistry,*
614 *Geophysics, Geosystems*, 13(1), 1–18. <https://doi.org/10.1029/2012GC004058>
- 615 Jiang, Y., Liu, Z., Davis, E. E., Schwartz, S. Y., Dixon, T. H., Voss, N., et al. (2017). Strain
616 release at the trench during shallow slow slip: The example of Nicoya Peninsula, Costa
617 Rica. *Geophysical Research Letters*, 44(10), 4846–4854.
618 <https://doi.org/10.1002/2017GL072803>
- 619 Kanamori, H., & Rivera, L. (2006). Energy partitioning during an earthquake. *Geophysical*
620 *Monograph Series*, 170, 3–13. <https://doi.org/10.1029/170GM03>
- 621 Kaneko, L., Ide, S., & Nakano, M. (2018). Slow Earthquakes in the Microseism Frequency Band
622 (0.1–1.0 Hz) off Kii Peninsula, Japan. *Geophysical Research Letters*, 45(6), 2618–2624.
623 <https://doi.org/10.1002/2017GL076773>
- 624 Kato, A., & Nakagawa, S. (2014). Geophysical Research Letters. *Geophysical Research Letters*,
625 (April), 6413–6419. <https://doi.org/10.1002/2014GL061184>.Received

- 626 Kato, A., Obara, K., Igarashi, T., Tsuruoka, H., Nakagawa, S., & Hirata, N. (2012). Propagation
627 of Slow Slip Leading Up to the 2011 Mw 9.0 Tohoku-Oki Earthquake. *Science*, 335(6069),
628 705–708. <https://doi.org/10.1126/science.1215141>
- 629 Kirby, S. T., Durham, W. B., & Stern, L. A. (1991). Mantle Phase Changes and Deep-
630 Earthquake Faulting in Subducting Lithosphere. *Science*, 252(5003), 216-225.
631 <https://doi.org/10.1126/science.252.5003.216>
- 632 Laske, G., Masters, G., Ma, Z., & Pasyanos, M. (2013). Update on CRUST1.0 - A 1-degree
633 Global Model of Earth's Crust, Paper presented at EGU General Assembly, European
634 Geoscience Union, Vienna
- 635 Maeda, T., & Obara, K. (2009). Spatiotemporal distribution of seismic energy radiation from
636 low-frequency tremor in western Shikoku, Japan. *Journal of Geophysical Research: Solid*
637 *Earth*, 114(10). <https://doi.org/10.1029/2008JB006043>
- 638 Maeda, T., Takemura, S., & Furumura, T. (2017). OpenSWPC: An open-source integrated
639 parallel simulation code for modeling seismic wave propagation in 3D heterogeneous
640 viscoelastic media 4. *Seismology, Earth, Planets and Space*, 69(1).
641 <https://doi.org/10.1186/s40623-017-0687-2>
- 642 Malservisi, R., Schwartz, S.Y., Voss, N., Protti, M., Gonzalez, V., Dixon, T.H., Jian, Y.,
643 Newman, A.V., Walter, J.I., & Vayenko, D. (2015). Multiscale postseismic behavior on a
644 megathrust: The 2012 Nicoya earthquake, Costa Rica. *Geochemistry, Geophysics,*
645 *Geosystems*, 16, 1848–1864. <https://doi.org/10.1002/2015GC005794>.
- 646 Maunder, B., van Hunen, J., Bouilhol, P., & Magni, V. (2019). Modeling Slab Temperature: A
647 Reevaluation of the Thermal Parameter. *Geochemistry, Geophysics, Geosystems*, 20(2),
648 673–687. <https://doi.org/10.1029/2018GC007641>
- 649 Nadeau, R. M., & Dolenc, D. (2005). Nonvolcanic tremors deep beneath the San Andreas Fault.
650 *Science*, 307(5708), 389. <https://doi.org/10.1126/science.1107142>
- 651 Nakano, M., Hori, T., Araki, E., Kodaira, S., & Ide, S. (2018). Shallow very-low-frequency
652 earthquakes accompany slow slip events in the Nankai subduction zone /704/2151/210
653 /704/2151/508 article. *Nature Communications*, 9(1). [https://doi.org/10.1038/s41467-018-](https://doi.org/10.1038/s41467-018-03431-5)
654 03431-5
- 655 Nishikawa, T., Matsuzawa, T., Ohta, K., Uchida, N., Nishimura, T., & Ide, S. (2019). The slow
656 earthquake spectrum in the Japan Trench illuminated by the S-net seafloor observatories.
657 *Science (New York, N.Y.)*, 365(6455), 808–813. <https://doi.org/10.1126/science.aax5618>
- 658 Obara, K. (2002). Nonvolcanic Deep Tremor Associated with Subduction in Southwest Japan.
659 *Science*, 296(5573), 1679–1681. <https://doi.org/10.1126/science.1070378>
- 660 Obara, K. (2011). Characteristics and interactions between non-volcanic tremor and related slow
661 earthquakes in the Nankai subduction zone, southwest Japan. *Journal of Geodynamics*,
662 52(3–4), 229–248. <https://doi.org/10.1016/j.jog.2011.04.002>
- 663 Obara, K., & Ito, Y. (2005). Very low frequency earthquakes excited by the 2004 off Kii
664 peninsula earthquakes: A dynamic deformation process in the large accretionary prism.
665 *Earth, Planets and Space*, 57(4), 321–326. <https://doi.org/10.1186/BF03352570>
- 666 Obara, K., & Kato, A. (2016). Connecting slow earthquakes to huge earthquakes. *Science (New*
667 *York, N.Y.)*, 353(6296), 253–257. <https://doi.org/10.1126/science.aaf1512>
- 668 Outerbridge, K. C., Dixon, T. H., Schwartz, S. Y., Walter, J. I., Protti, M., Gonzalez, V., et al.
669 (2010). A tremor and slip event on the Cocos-Caribbean subduction zone as measured by a
670 global positioning system (GPS) and seismic network on the Nicoya Peninsula, Costa Rica.

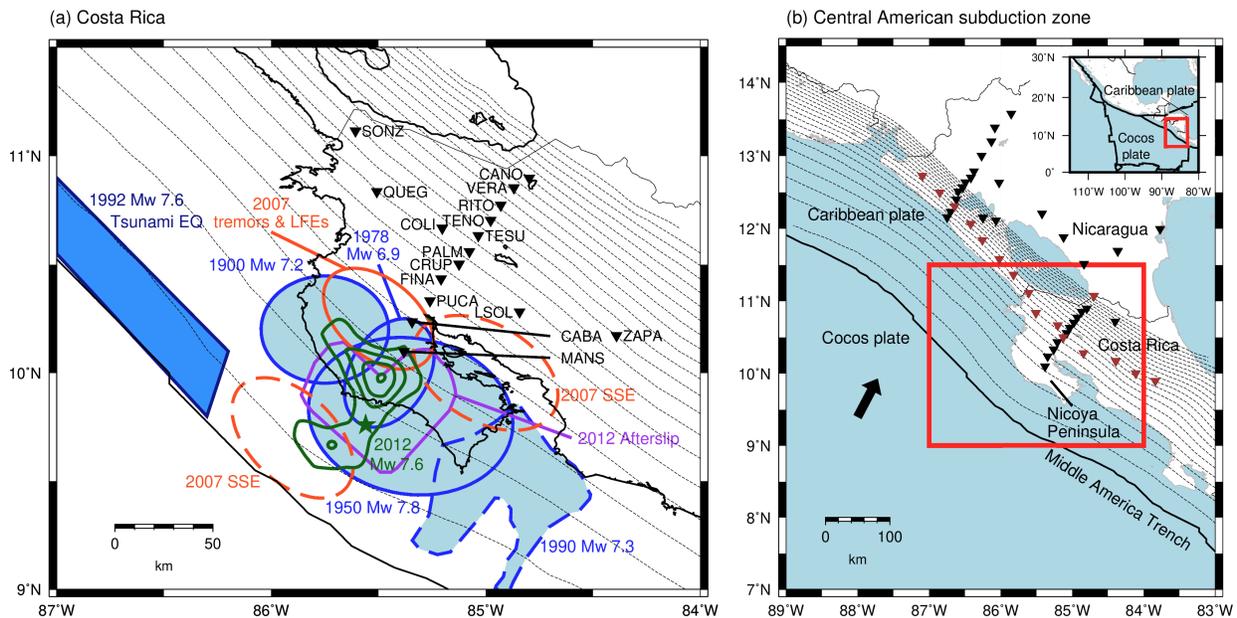
- 671 *Journal of Geophysical Research: Solid Earth*, 115(10), 1–17.
 672 <https://doi.org/10.1029/2009JB006845>
- 673 Protti, M. (1995). The March 25, 1990 (Mw=7.0, ML=6.8), earthquake at the entrance of the
 674 Nicoya Gulf, Costa Rica: its prior activity, foreshocks, aftershocks, and triggered seismicity.
 675 *Journal of Geophysical Research*, 100(B10), 345–358. <https://doi.org/10.1029/94jb03099>
- 676 Protti, M., González, V., Newman, A. V., Dixon, T. H., Schwartz, S. Y., Marshall, J. S., et al.
 677 (2014). Nicoya earthquake rupture anticipated by geodetic measurement of the locked plate
 678 interface. *Nature Geoscience*, 7(2), 117–121. <https://doi.org/10.1038/ngeo2038>
- 679 Rogers, G., & Dragert, H. (2003). Episodic Tremor and Slip on the Cascadia Subduction Zone:
 680 The Chatter of Silent Slip. *Science*, 300(5627), 1942–1943.
 681 <https://doi.org/10.1126/science.1084783>
- 682 Rost, S., & Thomas, C. (2002). Array seismology: Methods and applications. *Reviews of*
 683 *Geophysics*, 40(3), 2-1-2–27. <https://doi.org/10.1029/2000RG000100>
- 684 Ruiz, S., Aden-Antoniow, F., Baez, J. C., Otarola, C., Potin, B., del Campo, F., et al. (2017).
 685 Nucleation Phase and Dynamic Inversion of the M w 6.9 Valparaíso 2017 Earthquake in
 686 Central Chile. *Geophysical Research Letters*, 44(20), 10,290-10,297.
 687 <https://doi.org/10.1002/2017GL075675>
- 688 Saffer, D. M., & Wallace, L. M. (2015). The frictional, hydrologic, metamorphic and thermal
 689 habitat of shallow slow earthquakes. *Nature Geoscience*, 8(8), 594–600.
 690 <https://doi.org/10.1038/ngeo2490>
- 691 Satake, K. (1994). Mechanism of the 1992 Nicaragua Tsunami Earthquake. *Geophysical*
 692 *Research Letters*, 21(23), 2519–2522. <https://doi.org/10.1029/94GL02338>
- 693 Sato, H., Fehler, M., & Maeda, T. (2012). Seismic Wave Propagation and Scattering in the
 694 Heterogeneous Earth Structure, 2nd ed., New York, Springer-Verlag.
- 695 Scripps Institution of Oceanography. (1986). IRIS/IDA Seismic Network. International
 696 Federation of Digital Seismograph Networks. <https://doi.org/10.7914/SN/II>
- 697 Shelly, D. R., Beroza, G. C., Ide, S., & Nakamura, S. (2006). Low-frequency earthquakes in
 698 Shikoku, Japan, and their relationship to episodic tremor and slip. *Nature*, 442(7099), 188–
 699 191. <https://doi.org/10.1038/nature04931>
- 700 Shelly, D. R., Beroza, G. C., & Ide, S. (2007). Non-volcanic tremor and low-frequency
 701 earthquake swarms. *Nature*, 446(7133), 305–307. <https://doi.org/10.1038/nature05666>
- 702 Solomon, E. A., Kastner, M., Wheat, C. G., Jannasch, H., Robertson, G., Davis, E. E., & Morris,
 703 J. D. (2009). Long-term hydrogeochemical records in the oceanic basement and forearc
 704 prism at the Costa Rica subduction zone. *Earth and Planetary Science Letters*, 282(1–4),
 705 240–251. <https://doi.org/10.1016/j.epsl.2009.03.022>
- 706 Sugioka, H., Okamoto, T., Nakamura, T., Ishihara, Y., Ito, A., Obana, K., et al. (2012).
 707 Tsunamigenic potential of the shallow subduction plate boundary inferred from slow
 708 seismic slip. *Nature Geoscience*, 5(6), 414–418. <https://doi.org/10.1038/ngeo1466>
- 709 Syracuse, E. M., van Keken, P. E., Abers, G. A., Suetsugu, D., Bina, C., Inoue, T., et al. (2010).
 710 The global range of subduction zone thermal models. *Physics of the Earth and Planetary*
 711 *Interiors*, 183(1–2), 73–90. <https://doi.org/10.1016/j.pepi.2010.02.004>
- 712 Takemura, S., Kobayashi, M., & Yoshimoto, K. (2017). High-frequency seismic wave
 713 propagation within the heterogeneous crust: Effects of seismic scattering and intrinsic
 714 attenuation on ground motion modelling. *Geophysical Journal International*, 210(3), 1806–
 715 1822. <https://doi.org/10.1093/gji/ggx269>

- 716 Takemura, S., Matsuzawa, T., Noda, A., Tonegawa, T., Asano, Y., Kimura, T., & Shiomi, K.
 717 (2019). Structural Characteristics of the Nankai Trough Shallow Plate Boundary Inferred
 718 From Shallow Very Low Frequency Earthquakes. *Geophysical Research Letters*, *46*(8),
 719 4192–4201. <https://doi.org/10.1029/2019GL082448>
- 720 Takemura, S., Okuwaki, R., Kubota, T., Shiomi, K., Kimura, T., & Noda, A. (2020). Centroid
 721 moment tensor inversions of offshore earthquakes using a three-dimensional velocity
 722 structure model: slip distributions on the plate boundary along the Nankai Trough.
 723 *Geophysical Journal International*, *222*(2), 1109–1125. <https://doi.org/10.1093/gji/ggaa238>
- 724 Tamaribuchi, K., Kobayashi, A., Nishimiya, T., Hirose, F., & Annoura, S. (2019).
 725 Characteristics of Shallow Low-Frequency Earthquakes off the Kii Peninsula, Japan, in
 726 2004 Revealed by Ocean Bottom Seismometers. *Geophysical Research Letters*, *46*(23),
 727 13737–13745. <https://doi.org/10.1029/2019GL085158>
- 728 Voss, N., Dixon, T. H., Liu, Z., Malservisi, R., Protti, M., & Schwartz, S. (2018). Do slow slip
 729 events trigger large and great megathrust earthquakes? *Science Advances*, *4*(10), 1–6.
 730 <https://doi.org/10.1126/sciadv.aat8472>
- 731 Voss, N. K., Malservisi, R., Dixon, T. H., & Protti, M. (2017). Slow slip events in the early part
 732 of the earthquake cycle. *Journal of Geophysical Research: Solid Earth*, *122*(8), 6773–6786.
 733 <https://doi.org/10.1002/2016JB013741>
- 734 Walter, J. I., Schwartz, S. Y., Protti, J. M., & Gonzalez, V. (2011). Persistent tremor within the
 735 northern Costa Rica seismogenic zone. *Geophysical Research Letters*, *38*(1), 1–5.
 736 <https://doi.org/10.1029/2010GL045586>
- 737 Walter, J. I., Schwartz, S. Y., Protti, M., & Gonzalez, V. (2013). The synchronous occurrence of
 738 shallow tremor and very low frequency earthquakes offshore of the Nicoya Peninsula, Costa
 739 Rica. *Geophysical Research Letters*, *40*(8), 1517–1522. <https://doi.org/10.1002/grl.50213>
- 740 Wang, L., & Barbot, S. (2020). Excitation of San Andreas tremors by thermal instabilities below
 741 the seismogenic zone. *Science Advances*, *6*(36). <https://doi.org/10.1126/sciadv.abb2057>
- 742 Wessel, P., Smith, W. H. F., Scharroo, R., Luis, J., & Wobbe, F. (2013). Generic mapping tools:
 743 Improved version released. *Eos*, *94*(45), 409–410. <https://doi.org/10.1002/2013EO450001>
- 744 Xie, S., Dixon, T. H., Malservisi, R., Jiang, Y., Protti, M., & Muller, C. (2020). Slow Slip and
 745 Inter-transient Locking on the Nicoya Megathrust in the Late and Early Stages of an
 746 Earthquake Cycle. *Journal of Geophysical Research: Solid Earth*, *125*(11), 1–22.
 747 <https://doi.org/10.1029/2020JB020503>
- 748 Yabe, S., Tonegawa, T., & Nakano, M. (2019). Scaled Energy Estimation for Shallow Slow
 749 Earthquakes. *Journal of Geophysical Research: Solid Earth*, *124*(2), 1507–1519.
 750 <https://doi.org/10.1029/2018JB016815>
- 751 Yabe, S., Baba, S., Tonegawa, T., Nakano, M., & Takemura, S. (2021). Seismic energy radiation
 752 and along-strike heterogeneities of shallow tectonic tremors at the Nankai Trough and Japan
 753 Trench. *Tectonophysics*, 228714. <https://doi.org/10.1016/j.tecto.2020.228714>
- 754 Yao, S., & Yang, H. (2020). Rupture Dynamics of the 2012 Nicoya Mw 7.6 Earthquake:
 755 Evidence for Low Strength on the Megathrust. *Geophysical Research Letters*, *47*(13), 1–11.
 756 <https://doi.org/10.1029/2020GL087508>
- 757 Yokota, Y., & Ishikawa, T. (2020). Shallow slow slip events along the Nankai Trough detected
 758 by GNSS-A. *Science Advances*, *6*(3), 1–12. <https://doi.org/10.1126/sciadv.aay5786>
- 759 Yoshimoto, K., Sato, H., & Ohtake, M. (1993). Frequency-Dependent Attenuation of P and S
 760 Waves In the Kanto Area, Japan, Based On the Coda-Normalization Method. *Geophysical*

761 *Journal International*, 114(1), 165–174. <https://doi.org/10.1111/j.1365->
 762 246X.1993.tb01476.x

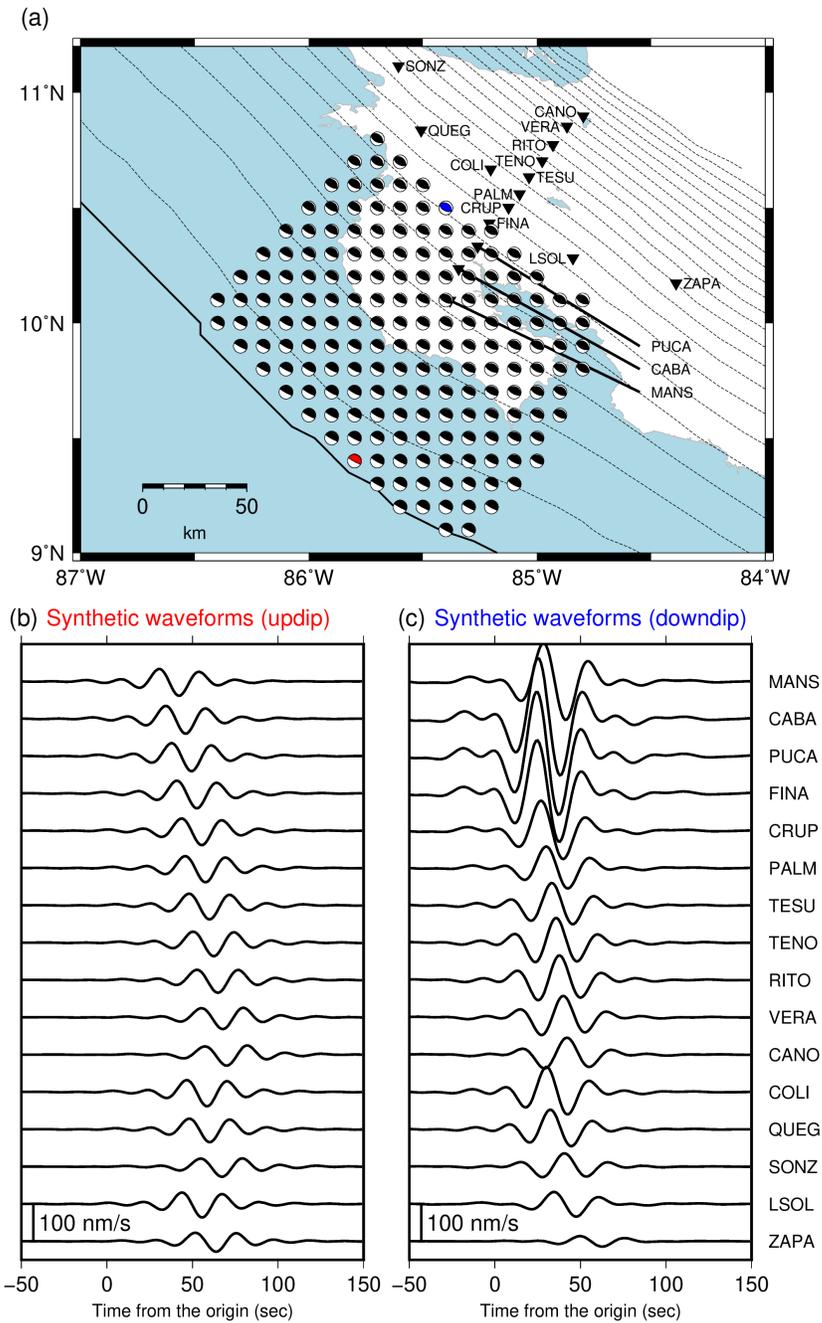
763 Yue, H., Lay, T., Schwartz, S. Y., Rivera, L., Protti, M., Dixon, T. H., et al. (2013). The 5
 764 September 2012 Nicoya, Costa Rica Mw 7.6 earthquake rupture process from joint
 765 inversion of high-rate GPS, strong-motion, and teleseismic P wave data and its relationship
 766 to adjacent plate boundary interface properties. *Journal of Geophysical Research: Solid*
 767 *Earth*, 118(10), 5453–5466. <https://doi.org/10.1002/jgrb.50379>
 768

769 Figures



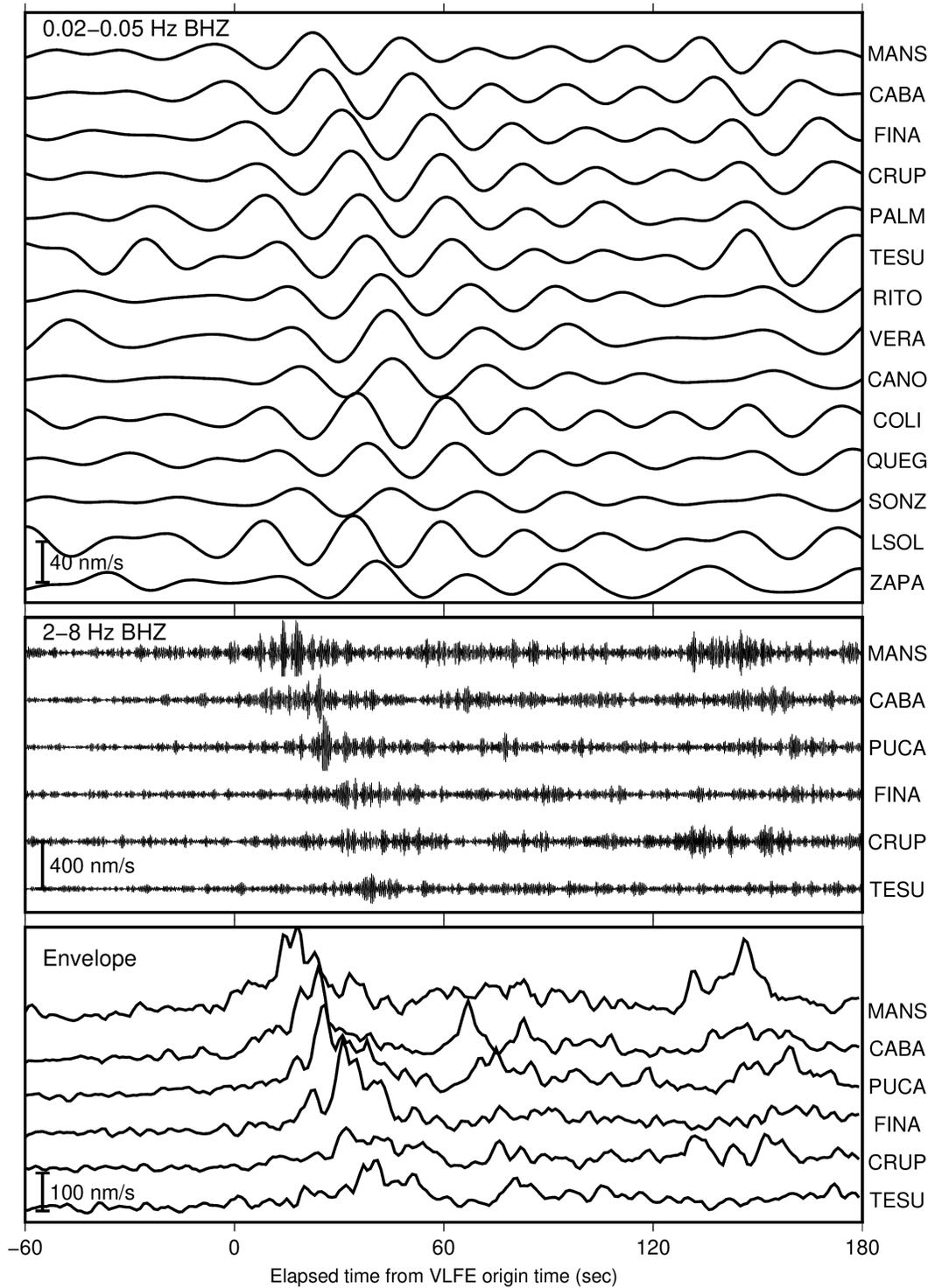
770

771 **Figure 1.** (a) Large regular and slow earthquake areas based on previous studies around the Nicoya
 772 Peninsula, in Costa Rica. Green contours show the coseismic slip distribution of the 2012 Mw 7.6
 773 earthquake with a 1-m interval (Yue et al., 2013). Blue areas show the slip areas of large regular
 774 earthquakes (1990 Mw 7.3: Protti et al., 1995 (surrounded by dashed blue line); others: Yue et al.,
 775 2013 (surrounded by solid blue lines)). Dark blue area surrounded by solid dark blue line indicate
 776 the slip area of the 1992 tsunami earthquake (Satake, 1994). Orange ellipses with dashed lines
 777 show large slip areas of the 2007 SSE, which were separated in updip and downdip areas (Jiang et
 778 al., 2017). The orange ellipse with a solid line shows the distributions of LFEs (Brown et al., 2009)
 779 and tremors (Outerbridge et al., 2010). The purple polygon shows the area whose afterslip of the
 780 2012 Mw 7.6 earthquake is more than 150 mm (Malvervisi et al., 2015). Black inverted triangles
 781 show the station locations of the TUCAN network used in VLFE detection (Section 2.2). Dashed
 782 contours indicate the isodepths of the top of the Cocos Plate with 10 km intervals (Slab2; Hayes
 783 et al., 2018). (b) Map of the Central American subduction zone. Solid line represents the Middle
 784 America Trench (Slab2; Hayes et al., 2018). Dashed contours are the same as (a). Black arrow
 785 indicates the convergence direction of the Cocos Plate, which subducts below the Caribbean plate
 786 from the Middle America Trench (NUVEL-1A; DeMets et al., 1994). Inverted triangles show the
 787 locations of stations of the TUCAN network. Brown triangles are stations which were used in
 788 beamforming (Section 2.3). The black lines in the inset show plate boundaries.



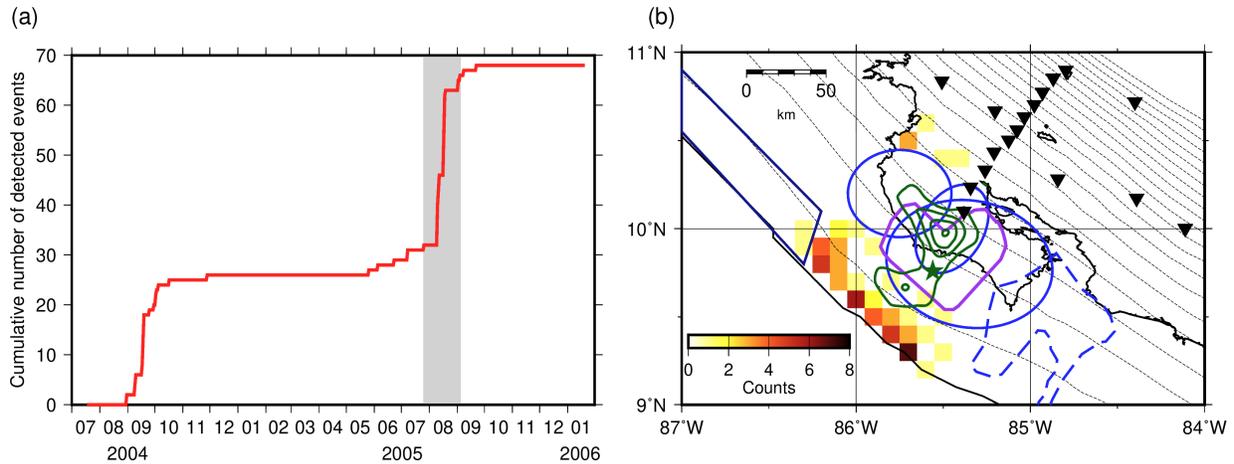
789

790 **Figure 2.** (a) Virtual source grids assumed in this study. Beach balls show the locations and focal
 791 mechanisms of the virtual sources. Inverted triangles and the black line are the same as in Figure
 792 1. Dashed contours indicate the isodepths of the top of the Cocos Plate with 10 km intervals (Slab2;
 793 Hayes et al., 2018). Examples of waveforms of virtual sources with Mw 4 in the (b) updip and (c)
 794 downdip areas. Sources of Figures 1b and 1c are shown by the red and blue beachballs in Figure
 795 2a, respectively. Amplitudes of the updip source are small due to the long distance between the
 796 source and stations, whereas amplitudes of the downdip source in the stations near the Nicoya
 797 Peninsula are large due to the short distance between the source and stations.



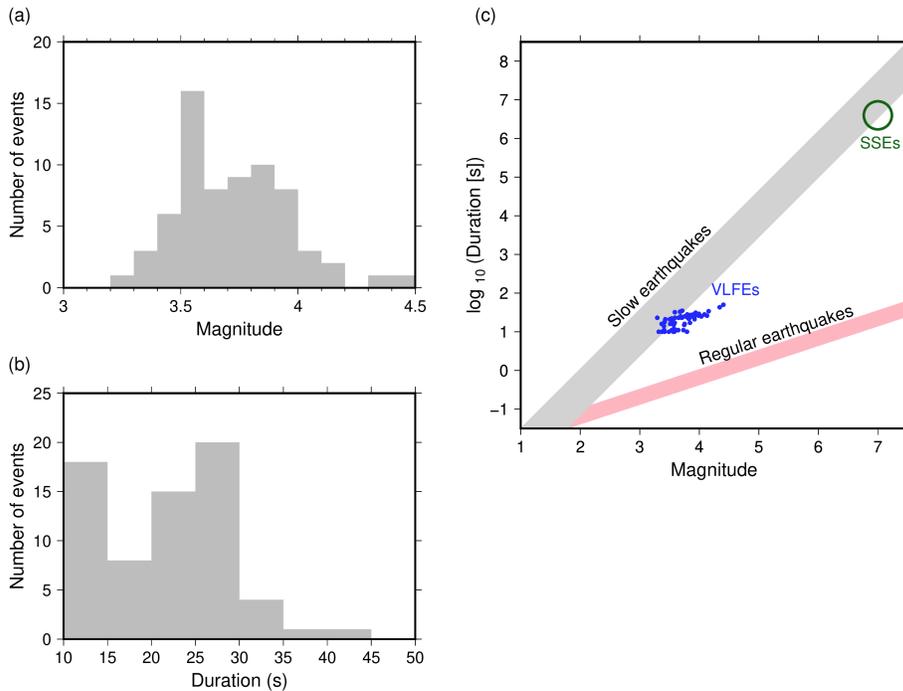
798

799 **Figure 3.** Example of waveforms of a VLFE and the corresponding tremor located at 85.8°W and
 800 9.4°N (shown by a red beachball in Figure 2a) in the frequency range of 0.02–0.05 Hz and 2–8 Hz,
 801 and smoothed root-mean-square envelope in the frequency range of 2–8 Hz. Seismograms are
 802 shown from the origin time of the VLFE, 03:53:47 (UTC), August 10, 2005.



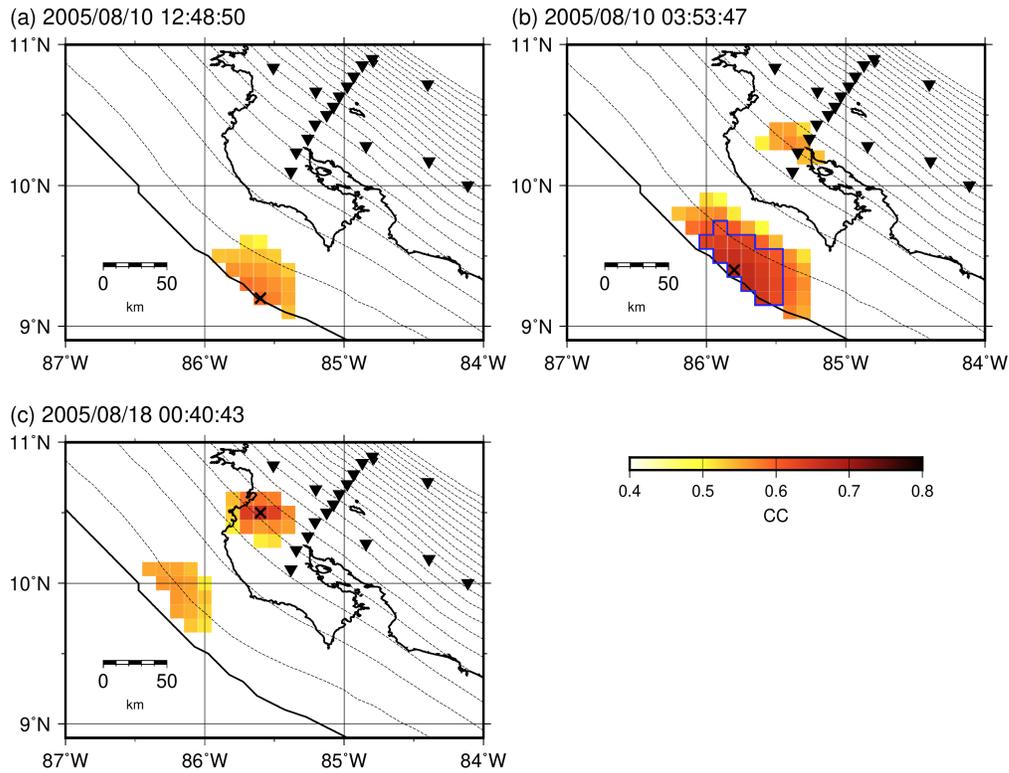
803

804 **Figure 4.** (a) Cumulative number of the VLFs from July 2004 to January 2006. Gray shading
 805 shows the period of the 2005 SSE (Jiang et al., 2012). (b) Distribution of the number of detected
 806 events at each virtual source. Blue ellipses and polygons, dark blue quadrangle, inverted triangles,
 807 black line, the purple polygon, and dashed contours are the same as in Figure 1.



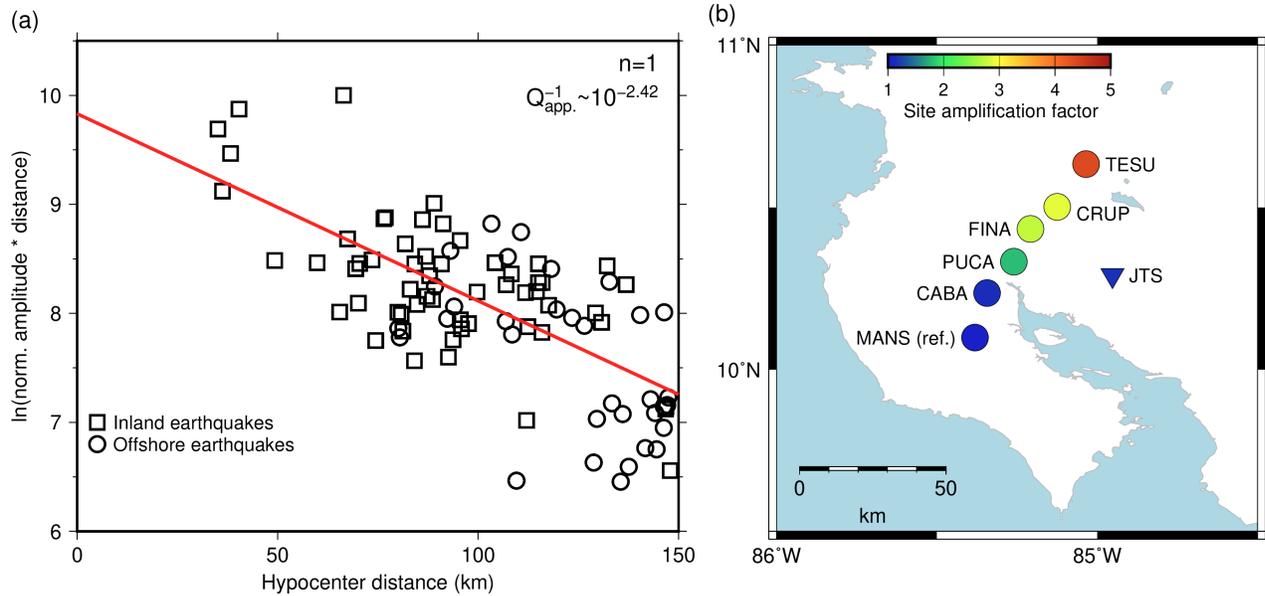
808

809 **Figure 5.** Distribution of (a) magnitudes and (b) source durations of VLFs. (c) Relationship
 810 between durations and magnitudes of slow earthquakes. Gray and pink shadings show the ranges
 811 of the scaling law for slow and regular earthquakes by Ide et al. (2007). Blue dots indicate the
 812 relationship between source durations and magnitudes of VLFs located in this study. Green circle
 813 represents the relationship between durations and magnitudes of SSEs in Costa Rica (Jiang et al.,
 814 2012; Voss et al., 2017).



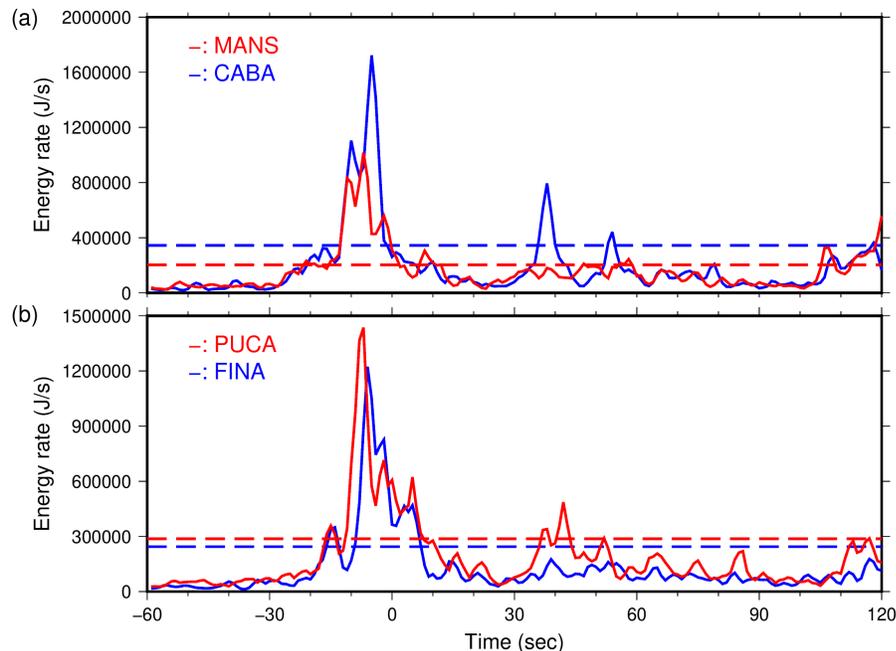
815

816 **Figure 6.** Examples of CC distributions of (a) an event which has large CCs only in updip grids,
 817 (b) an event which has large CCs both in updip and downdip grids but is located in an updip grid,
 818 and (c) an event which has large CCs both in updip and downdip grids but is located in a downdip
 819 grid. Cross mark in each map indicates the epicenter of the VLFE. Inverted triangles, black line,
 820 and dashed contours are the same as in Figure 1. The blue polygon in (b) indicates the grids whose
 821 CC are more than 0.9 times of the maximum CC.



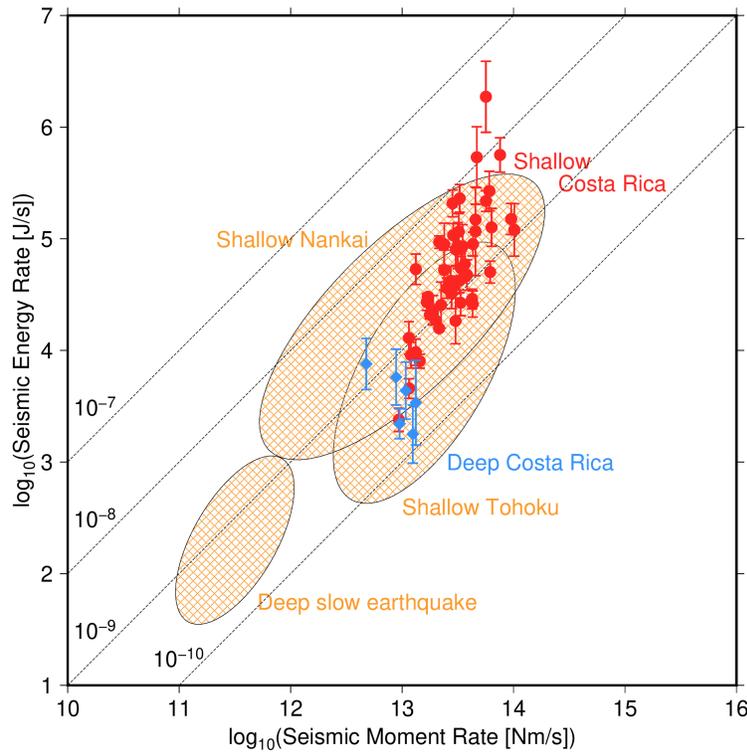
822

823 **Figure 7.** (a) Relationship between logarithm of coda-normalized maximum S-wave amplitudes
 824 and hypocentral distances. To eliminate effects of geometrical spreading of S-wave, coda-
 825 nomadized S-wave amplitudes were multiplied by their hypocentral distance. Red line shows the
 826 regression line using Equation (2). (b) Site amplification factors relative to MANS based on
 827 relative coda amplitude measurements.



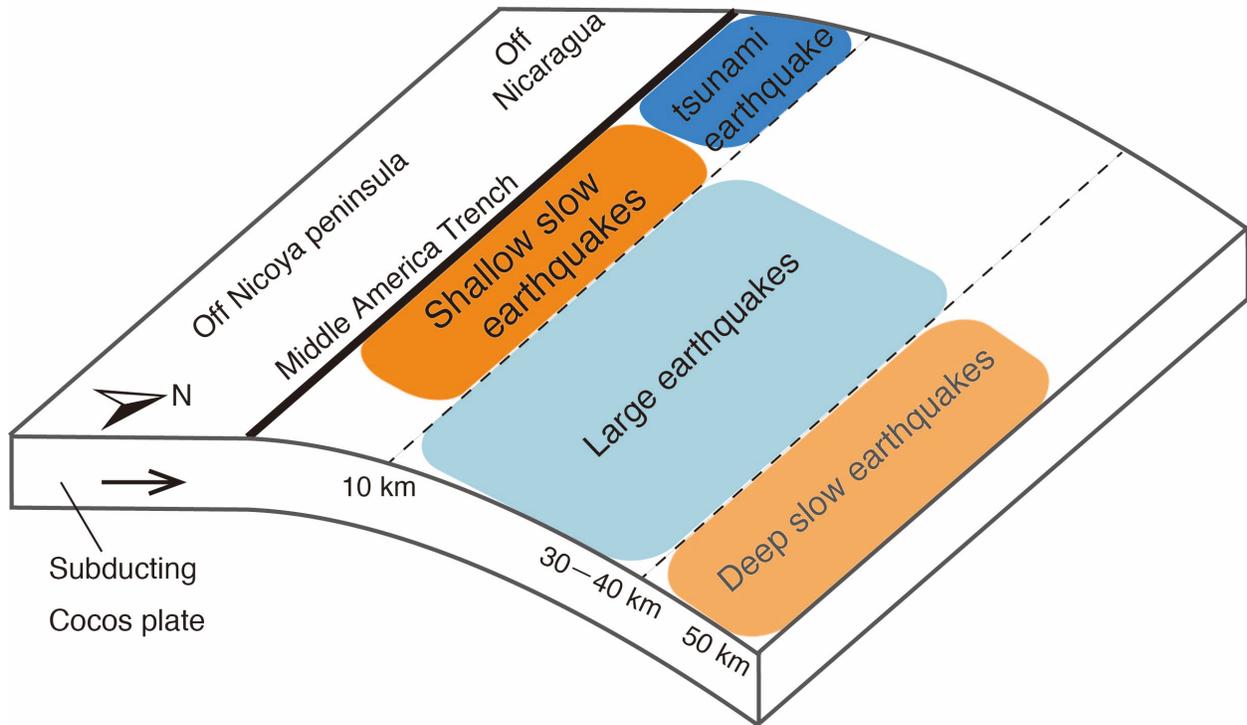
828

829 **Figure 8.** Temporal changes of energy rate functions of a tremor in (a) MANS and CABA and (b)
 830 PUCA and FINA. The corresponding VLFE occurs on 03:53:47 (UTC), August 10, 2012. Dashed
 831 lines indicate the threshold, which is set as 20% of the maximum value of the energy rate functions.



832

833 **Figure 9.** Relationship between seismic moment rates of VLFs and seismic energy rates of
 834 tremors estimated in this study. Red circles and blue diamonds show the events of updip and
 835 downdip regions, respectively. Dashed lines show scaled energies of 10^{-7} , 10^{-8} , 10^{-9} , and 10^{-10} .
 836 Orange shadings show the relationships between seismic moment rates of VLFs and seismic
 837 moment rates of tremors of shallow slow earthquakes in the Nankai (Yabe et al., 2019) and Tohoku
 838 subduction zones (Yabe et al., 2021), and deep slow earthquakes in southwest Japan (Ide & Yabe,
 839 2014), Cascadia (Ide, 2016), and Mexico (Ide & Maury, 2018). We note that scaled energies of
 840 shallow slow earthquakes were estimated for individual events, whereas those of deep slow
 841 earthquakes were estimated for stacked events.



842

843 **Figure 10.** A schematic illustration showing the interpretation of distributions of slow, tsunami,
844 and large regular earthquakes in the Central American subduction zone. The areas of large
845 earthquakes, the 1992 tsunami earthquake, and deep slow earthquakes are referred from Yue et al.
846 (2013), Satake (1994), and Outerbridge et al. (2010), respectively.

847