

# Enabling Smart Dynamical Downscaling of Extreme Precipitation Events with Machine Learning

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## Key Points:

- Dynamical downscaling at  $\sim 1$  km resolution produces reliable estimations of extreme rainfall but is computationally expensive.
- Machine learning (ML) makes smart dynamical downscaling (SDD) possible, where ML models filter out irrelevant large-scale patterns.
- We demonstrate that SDD can be enabled by support vector machines or deep neural networks, of which the latter performs better.

## Abstract

The projection of extreme convective precipitation by global climate models (GCM) exhibits significant uncertainty due to the coarse resolution of GCMs, which cannot resolve fine-scale processes. Direct dynamical downscaling (DDD) of regional climate at convection-permitting resolutions ( $\sim 1$  km) provides valuable insight into the potential changes in extreme precipitation, but its computational expense is formidable. Here we document the effectiveness of machine learning in enabling smart dynamical downscaling (SDD), which performs downscaling only for a small subset of GCM data. Trained with reanalysis and satellite data for three Asian cities, support vector machines can filter out approximately 87% to 94% of circulation data, which are irrelevant to extremes. Deep convolutional neural networks, trained with larger data sets, can filter out more than 97% of circulation data and in the selected subset, retrieve 72% to 81% of the circulation patterns responsible for extreme events (rain intensity higher than the 99th percentile).

## Plain Language Summary

Climate scientists use supercomputers to simulate the climate and predict how it may change under global warming. Extreme precipitation, which can disrupt the society by causing disasters like floods and landslides, is of great interest in climate studies. However, replicating severe rainstorms on a supercomputer, especially those in tropical and subtropical areas, is not easy because those rainstorms often contain fine-scale details that cannot be represented confidently without an extensive amount of computational resource. If we use computationally cheap computer models to simulate those rainstorms, we obtain results with substantial uncertainties. If we use computationally expensive ones, we cannot simulate many scenarios, and thus cannot be confident about the results. The power of machine learning in pattern recognition is here used to help modelers use their computational resources more efficiently. Instead of simulating all kinds of weather events, including unimportant ones, at high resolutions, we use machine learning algorithms to search coarse resolution climate data for those large-scale weather patterns that are more likely to cause severe rainstorms. Then modelers can make more efficient use of supercomputing resources by simulating impactful weather events only and advance our understanding of extreme precipitation.

## 1 Introduction

Extreme precipitation events often disrupt the society by causing disasters such as floods and landslides. Thus, predicting the response of precipitation extremes to global warming is crucial for our adaptation to climate change. However, predicting such changes is not straightforward because the performance of numerical simulation of extreme precipitation events is sensitive to model resolution (Li et al., 2018; Van Der Wiel et al., 2016), while grid spacings of current-generation climate models are still at a coarse  $\sim 1^\circ$  resolution in the horizontal. Previous studies have demonstrated that to accurately predict future changes in extreme precipitation events, especially those associated with severe convection, it is necessary to resolve local storm dynamics with kilometer-scale resolutions, which are the so-called convection-permitting resolution (Kendon et al., 2014, 2017). Such high model resolution is necessary not only because of the small spatial scale of convective cells, but also because the essential roles played by the interaction between convection and large-scale dynamics, air-sea coupling, and topographic forcing in determining the intensity of extreme events (Nie et al., 2016; Kendon et al., 2017; Rainaud et al., 2017).

Modelers have been attempting to refine the resolution of global climate models, but the highest resolution so far is only  $\sim 25$  km (Haarsma et al., 2016). A direct dynamical downscaling (DDD) approach has been adopted in the regional climate simulations at convection-permitting resolutions and valuable findings have been obtained

63 due to improved representation of fine-scale processes (Prein et al., 2015). For example,  
 64 Prein et al. (2017) found that under the RCP8.5 scenario, the strengthening of precip-  
 65 itation intensity and the expansion of impact area will combine to give 80% increases  
 66 in the total precipitation volume of mesoscale-convective systems in the US. However,  
 67 DDD at the convection-permitting resolution has a very high demand on computational  
 68 resources (Prein et al., 2015).

69 Is there a way to avoid the expensive computational cost of long-term DDD but  
 70 still allow a convection-permitting resolution to be used? This question is the core prob-  
 71 lem we want to address in this study. When our concern is not the mean climate but in-  
 72 stead a special kind of weather (e.g., extreme precipitation), we can save a tremendous  
 73 amount of computational resources if we do not have to perform the DDD for every day  
 74 of an extended period. In this study, we harness the power of machine learning to ful-  
 75 fill the goal of selecting a small subset of GCM data for the dynamic downscaling of ex-  
 76 treme precipitation events. We call this modeling strategy smart dynamical downscal-  
 77 ing (SDD).

78 Machine learning has been increasingly used in geoscience in recent years. In the  
 79 atmospheric science community, it has applied to real-time nowcasting (Han et al., 2017;  
 80 McGovern et al., 2017), physical parameterization (Brenowitz & Bretherton, 2019; Gagne  
 81 et al., 2020), and weather forecast (Weyn et al., 2019; Chattopadhyay et al., 2020). Here  
 82 we harness the power of machine learning in pattern recognition to enable SDD. Because  
 83 previous studies have suggested that the exact strengthening rate of extreme precipita-  
 84 tion mostly relies on dynamic, instead of thermodynamic, response to warming (Lenderink  
 85 & Van Meijgaard, 2008; Shi & Durran, 2016; Pfahl et al., 2017), such an SDD approach  
 86 is urgently needed for fully utilizing the information from GCM simulations to explore  
 87 the effect of changes in large-scale eddy circulations on extreme precipitation.

## 88 2 Data and Methods

### 89 2.1 Reanalysis and Satellite Data

90 In this study, we train machine learning models with reanalysis data of circulation  
 91 and satellite data of precipitation. We use the NCEP/NCAR Global Reanalysis Prod-  
 92 ucts (Kalnay et al., 1996) to represent the state of the atmospheric circulation. This data  
 93 set has  $2.5^\circ \times 2.5^\circ$  horizontal resolution. Though the original data set is available on  
 94 17 pressure levels, we use only the lowest 8 vertical levels between 1000 hPa to 300 hPa  
 95 in this study. The variables we use to depict the large-scale circulation include 7 three  
 96 dimensional variables: geopotential height, relative humidity, temperature,  $u$ - and  $v$ -components  
 97 of horizontal wind, vertical (pressure) velocity, and vorticity. For the training of support  
 98 vector machine (SVM) models, we also included 3 additional single-level variables — sur-  
 99 face pressure, tropopause pressure, and precipitable water. The temporal resolution of  
 100 the reanalysis data is 6 hours. The period we used from the reanalysis data is June 2000  
 101 to May 2019.

102 The precipitation data we used is the final precipitation, Level 3 data of the Inte-  
 103 grated Multi-satellitE Retrievals for Global Precipitation Measurement (GPM IMERG;  
 104 Huffman et al., 2019). This data set has  $0.1^\circ$  spatial resolution and 30 min temporal res-  
 105 olution originally. We used the data set between the period of June 2000 to May 2019.  
 106 Because the reanalysis data has 6-hour temporal resolution, we average the GPM data  
 107 in time to get the mean precipitation rate in the 6-hour intervals between two consec-  
 108 utive time slices of reanalysis data. To make it represent impactful events, we also av-  
 109 erage the precipitation data spatially to obtain coarse-grained data on a  $0.5^\circ \times 0.5^\circ$  grid.

110 The precipitation data from reanalysis was not used in this study because they only  
 111 represent precipitation from large-scale circulation and have a significant bias. Supple-  
 112 mentary Figure S1 shows the histogram of precipitation intensities and the temporal dis-

113 tribution of extreme precipitation events for the grid point nearest to Hong Kong in re-  
 114 analysis and GPM data. From Figure S1a, it is evident that the reanalysis data signif-  
 115 icantly underestimate the rain rates of intense precipitation events. Figure S1b suggests  
 116 reanalysis cannot represent the correct timing of extreme events either. The satellite data  
 117 suggest that extreme precipitation events peak in May and June, consistent with rain  
 118 gauge observation (Su et al., 2019). In contrast, reanalysis data exhibit peak season of  
 119 extreme rainfall from July to September.

120 Our application of machine learning focused on the area surrounding three Asian  
 121 cities, Hong Kong (HK), Manila (MN), and Singapore (SG). In the training of support  
 122 vector machines (SVM), the input to one SVM are the circulation data (7 three-dimensional  
 123 variables and 3 two-dimensional variables) in a  $15^\circ \times 15^\circ$  region centered at one of those  
 124 three cities. Each time slice of the reanalysis data is categorized as producing “signif-  
 125 icant rain” or “no significant rain”, “light rain” or “heavy rain”, based GPM precipita-  
 126 tion in the next 6 hours at the  $0.5^\circ \times 0.5^\circ$  cell centered at the same city. The SVMs were  
 127 trained to predict the correct categories from the large-scale circulation data.

128 In our application of convolutional neural networks (CNN), we identified three “use-  
 129 ful” regions surrounding each of those three cities. Those regions share similar dynamic  
 130 characteristics of rainy weather and gave us larger data sets for training CNNs. 6-hourly  
 131 precipitation data of each  $0.5^\circ \times 0.5^\circ$  cell within a “useful” regions are used to catego-  
 132 rize the corresponding time (the beginning of 6-hour intervals) and location as produc-  
 133 ing “extreme rainfall” or “non-extreme rainfall”. The input data for CNNs are the cir-  
 134 culation data (7 three-dimensional variables) in  $15^\circ \times 15^\circ$  square regions centered at each  
 135 of the  $0.5^\circ \times 0.5^\circ$  rainfall data cells within a “useful” region.

## 136 2.2 Support Vector Machine (SVM)

137 SVM is a machine learning model for binary classification problems. At its core,  
 138 SVMs find a hyperplane in the feature space of data and separate points in the feature  
 139 space into two different groups. The hyperplane in feature space is defined as the set of  
 140 points  $\mathbf{x}$  satisfying

$$141 \quad \mathbf{w} \cdot \mathbf{x} + b = 0 \quad (1)$$

142 where the vector  $\mathbf{w}$  and scalar  $b$  for the best hyperplane are determined by an optimiza-  
 143 tion procedure which maximizes the margin between two classes in feature space. For  
 144 a linearly separable problem,  $\mathbf{w}$  and  $b$  are entirely determined by those sample points  
 145 that are closest to the best hyperplane. Those sample points are called support vectors.  
 146 When the data are not linearly separable, one can use a soft margin technique to allow  
 147 a small number of instances to be misclassified.

148 Furthermore, in nonlinear classification problems, it is common to use a kernel func-  
 149 tion to replace dot product for operating the optimization algorithm in a transformed  
 150 feature space implicitly. In our application, we used the Gaussian radial basis function,

$$151 \quad G(\mathbf{x}_i, \mathbf{x}_j) = \exp\left(-\frac{\|\mathbf{x}_i - \mathbf{x}_j\|^2}{2\sigma^2}\right) \quad (2)$$

152 where  $\sqrt{2}\sigma$  is called kernel scale. Besides  $\sigma$ , the other hyperparameter for training an  
 153 SVM is the box constraint which appears in the soft margin formula and decides the tol-  
 154 erance level of misclassification by the SVM.

155 We used MATLAB R2019a in our study to train SVMs with 10-fold cross-validation.  
 156 The hyperparameters were tuned using Bayesian optimization.

### 2.3 Convolutional Neural Network (CNN)

In its essence, a neural network transforms the signal from one layer of neurons to the next through a linear transformation and the use of a nonlinear activation function,

$$\mathbf{z}^{[k]} = \mathbf{W}^{[k]}\mathbf{a}^{[k-1]} + \mathbf{b}^{[k]}, \quad \mathbf{a}^{[k]} = g^{[k]}(\mathbf{z}^{[k]}) \quad (3)$$

where  $\mathbf{a}^{[k]}$  is the activation of Layer  $k$ ,  $\mathbf{W}^{[k]}$  is a weight matrix, and  $\mathbf{b}^{[k]}$  is a bias vector.  $g^{[k]}$  is a non-linear activation function. For Layer 0, the activation  $\mathbf{a}^{[0]}$  is simply the vector of input data  $\mathbf{x}$ . A fully connected layer in a deep neural network connects every neuron in the previous layer to every neuron in the current layer. A convolution layer, by contrast, has multiple filters, which are used to convolve a sub-block of the activation data from the previous layer and connect that subset of neurons in the previous layer to a neuron in the current layer.

We again used MATLAB R2019a to train the CNNs in this study. 75% of input data were used to train the models and 25% used for cross-validation. The stochastic gradient descent with momentum (SGDM) method was used to find the optimal weights and bias of the CNNs.

### 2.4 Performance Metrics

In the training of SVMs and CNNs, algorithms try to achieve the highest classification accuracy. However, because extreme precipitation events are only a small fraction of the entire data set, the accuracy of trained models always appears intuitively high. Thus, in our discussion below, we report the performance of trained models in terms of precision and recall.

The precision is usually defined as the number of true positive instances divided by the number of true and false positive instances. The recall is usually defined as the number of true positive instances divided by the number of true positive and false negative cases. However, because the distribution of rain intensity is continuous and we want to ensure the machine learning models can retrieve most of the extreme precipitation events, it is often necessary to train a machine learning model using a relatively low percentile of precipitation rate as the criterion for categorizing data, but evaluate the effectiveness of the trained model in retrieving the extreme events defined with a different, higher percentile. Thus, we adopt the following notation for precision and recall,

$$P_y^M = \frac{|\{r > r_y\} \cap \{r' > r_y\}|}{|\{r' > r_y\}|}, \quad (4)$$

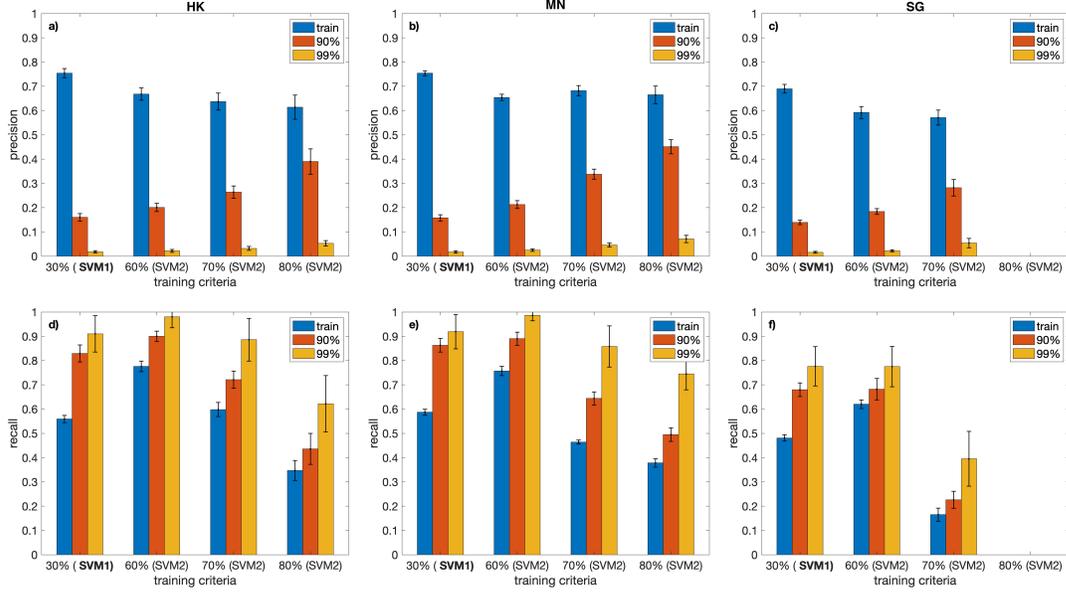
$$R_y^M = \frac{|\{r > r_y\} \cap \{r' > r_y\}|}{|\{r > r_y\}|}, \quad (5)$$

where  $P_y^M$  and  $R_y^M$  are the precision and recall of the model M when precipitation rates greater than the  $y$ -th percentile of rain rate,  $r_y$ , are labeled as positive.  $r_y$  may be *different* from the actual threshold used in categorizing data when training the model M.  $\{r > r_y\}$  represent the set of instances for which real precipitation rates ( $r$ ) are higher than  $r_y$ , and  $\{r' > r_y\}$  is the set of instances for which the model M predicts their precipitation rates ( $r'$ ) are greater than  $r_y$ .  $r'$  was not computed by the machine learning models explicitly, but rather the condition,  $r' > r_y$ , was judged by the classification model M.

## 3 Results

### 3.1 Dual SVM Model

We first attempted to select instances for extreme events by training a pair of SVMs. The first SVM (SVM1) tells whether the circulation data of a time slice can produce “sig-

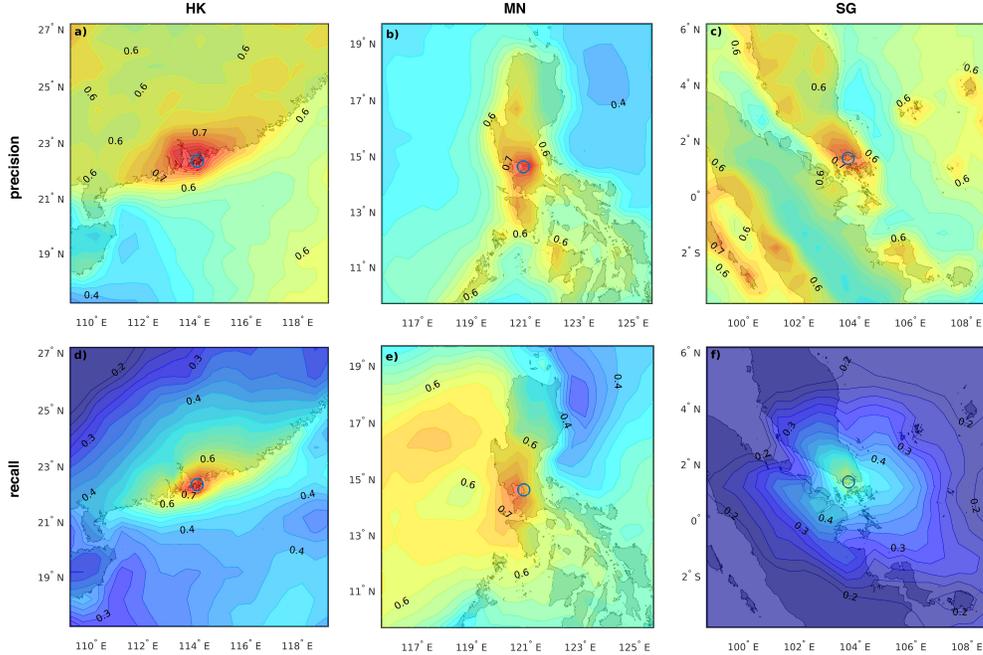


**Figure 1.** Precision (a–c) and recall (d–f) of the trained SVMs. a) and d) are the SVMs for Hong Kong (HK), b) and e) for Manila (MN), c) and f) for Singapore (SG). The SVMs were trained for the thresholds indicated below the horizontal axis, but their performance is evaluated against the training criteria and the 90th and 99th percentiles of rain rates.

202 nificant” rainfall or not. It was trained with the 30th percentile of rain rates as the thresh-  
 203 hold for “significant” rainfall. The subset of circulation data which SVM1 predicts to pro-  
 204 duce significant rain is then adopted by the second SVM (SVM2), which uses a higher  
 205 percentile (60th, 70th, or 80th) as its criterion for “extremes”. We found that this dual-  
 206 SVM strategy can yield higher precision and recall than using one SVM to predict “ex-  
 207 tremes” directly.

208 Figure 1 shows the performance of the Dual SVM model trained with the data for  
 209 the three cities, HK, MN, and SG. The precision of SVM1 for its training criteria,  $P_{30}^{\text{SVM1}}$ ,  
 210 is around 0.7, and the recall of SVM1 for its training criteria,  $R_{30}^{\text{SVM1}}$ , is between 0.48  
 211 to 0.59. These recall rates are not very high. However, if we target retrieve precipita-  
 212 tion event with rain rates higher than the 90th and 99th percentiles, we can find that  
 213 the corresponding recall rates,  $R_{90}^{\text{SVM1}}$  and  $R_{99}^{\text{SVM1}}$ , are between 0.82 to 0.92 for HK and  
 214 MN, and between 0.69 to 0.79 for SG. Thus, the trained SVM1 is effective in retrieving  
 215 the majority of extreme precipitation events. It should be noted that because we did not  
 216 include rain rates lower than  $0.05 \text{ mm h}^{-1}$  in calculating the percentiles, Thus SVM1 elim-  
 217 inates much more than 30% circulation data from all time slices. Precipitation rates in  
 218 HK, MN, and SG only exceed the corresponding 30th percentiles in 14.5%, 28.9%, and  
 219 29.4%, respectively, of the 19 years.

220 Figure 1 also shows the performance of SVM2 with respect to training criteria, as  
 221 well as for real extreme events defined by the 90th and 99th percentiles. For SG, we were  
 222 unable to obtain a converged solution when the training criterion was set as the 80th per-  
 223 centile. The precision of SVM2 when evaluation criteria are the 90th and 99th percentiles  
 224 increases as the training criteria increase, a natural result of the narrowing mismatch be-  
 225 tween training and evaluation criteria. The recall of SVM2 decreases as the training cri-  
 226 teria increases. A higher training threshold means that we can filter out more “irrele-  
 227 vant” instances. However, it also increases our chance of losing actual extreme events



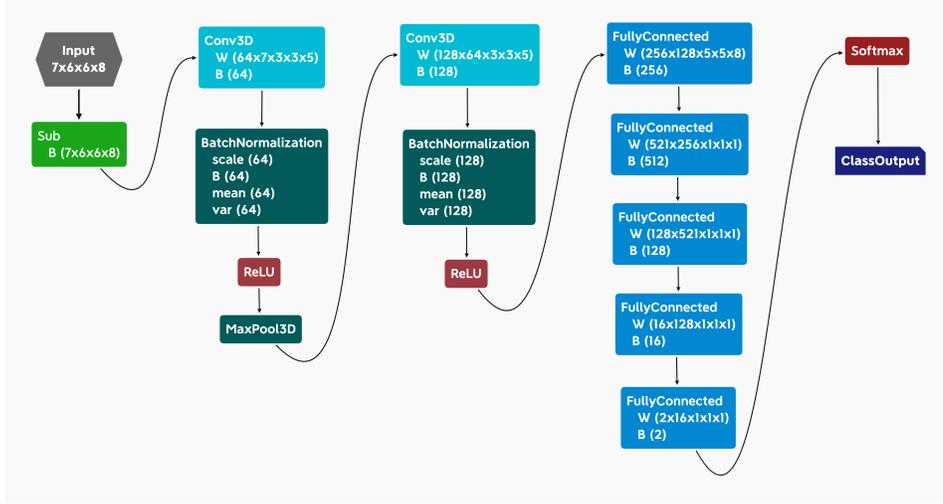
**Figure 2.** Precision (upper row) and recall (lower row) for the SVM1’s which were trained for HK, MN, and SG but are applied to areas surrounding those cities here.

228 due to misclassification. Based on Fig. 1, the SVM2 trained with the 70th percentile of  
 229 rain rates are the most balanced models for applications. If we target to retrieve extreme  
 230 events defined by the 99th percentile in the selection, the SVM1 and the SVM2 trained  
 231 with the 70th percentile can yield combined recall rates of  $R_{99}^{SVM1} R_{99}^{SVM2} = 0.81, 0.79,$  and  $0.31,$   
 232 for HK, MN, and SG, respectively.

233 As mentioned above, the number of time slices which produced significant rainfall  
 234 is smaller than 30% (15% for HK) of the entire 19-year period of our data. If we use the  
 235 SVM2 trained with the 70th percentile as the training criterion, SVM2 can eliminate ap-  
 236 proximately another 4/7 data from the subsets selected by SVM1. Thus, the Dual SVM  
 237 models, in total, can eliminate approximately more than 87% (94% for HK) of circula-  
 238 tion data from extreme events candidates. That is a significant saving of computational  
 239 cost in dynamic downscaling. However, it still means that we need to “waste” a notable  
 240 fraction of our computation to ensure most extreme events are kept by the Dual SVM  
 241 models. The unsatisfactory performance of the Dual SVM model in SG data suggests  
 242 we cannot obtain a very reliable subset of data if we want to study deep tropical extreme  
 243 rainfall. Can we overcome this difficulty with other machine learning algorithms? The  
 244 answer is positive. In Section 3.3, we will demonstrate that the use of deep neural net-  
 245 work can yield significantly better performance than the Dual SVM models.

### 246 3.2 Useful Areas

247 Large data set is needed for deep learning to prevent over-fitting. When we focus  
 248 on only one point on a map, the availability of observation data is limited. In the train-  
 249 ing of Dual SVM models above, we used 19 years of 6-hourly data, including 27,756 time  
 250 slices. The areas surrounding the place of interest should be in a similar climate regime.  
 251 Therefore, we evaluate the similarity of extreme event dynamics by applying the SVM1’s



**Figure 3.** Structure of the CNNs trained in this study. The size of one input “image” is 7 (channels/variables)  $\times$  6 (height/latitude)  $\times$  6 (width/longitude)  $\times$  8 (depth/altitude). The first convolution layer has 64 filters and the second has 128 filters. The size of filters is 3 (height)  $\times$  3 (width)  $\times$  5 (depth). The number of neurons in the five fully connected layers is 256, 512, 128, 16, and 2, respectively.

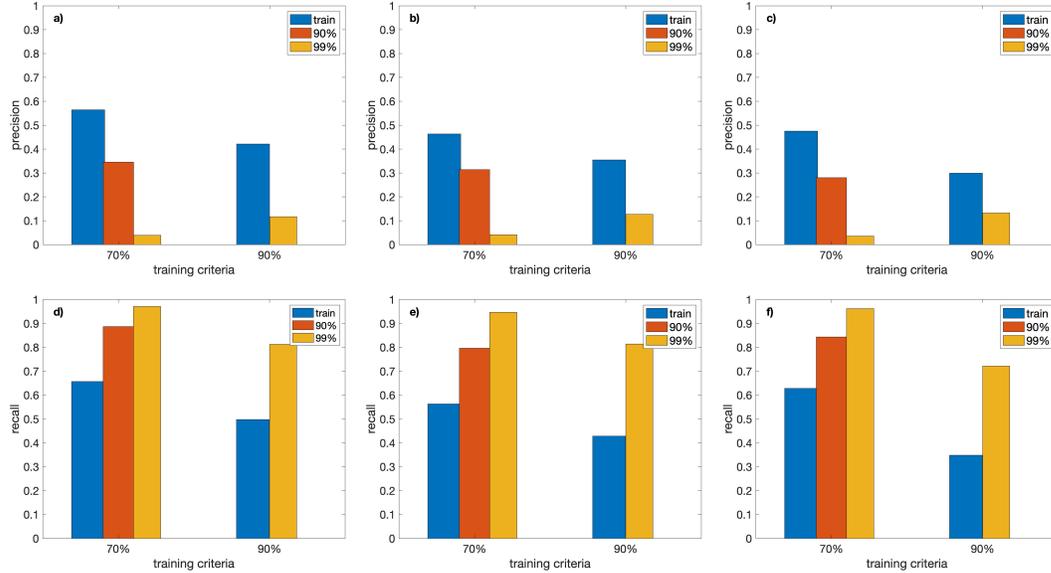
252 trained above to regions surrounding HK, MN, and SG, the data of which, except right  
 253 at the three cells of those three cities, were not seen during training SVM1.

254 Figure 2 shows the performance of the SVM1’s in relevant regions. What might  
 255 be surprising is that the spatial distribution of precision and recall exhibit some depen-  
 256 dence on the terrain. What is most impressive is the case of HK. In Figure 2a and d, pre-  
 257 cision and recall are maximized along the South China coast, suggesting that precipi-  
 258 tation events in HK are significantly affected by coastal location and topography.

259 Good precision and recall in Figure 2 indicate the applicability of the model trained  
 260 at a city only to its surrounding areas, thereby the similarity in the dynamics of extreme  
 261 events. We can define “useful” areas as those exhibiting relatively high precision and re-  
 262 call. For HK and MN, we select grid points at which  $P_{30}^{\text{SVM1}} > 0.60$  and  $R_{30}^{\text{SVM1}} > 0.50$ .  
 263 For SG, we select grid points at which  $P_{30}^{\text{SVM1}} > 0.45$  and  $R_{30}^{\text{SVM1}} > 0.35$ . Using those  
 264 “useful” areas allows us to enlarge the training data set for HK, MN, and SG to 1.2, 1.3,  
 265 and 1.4 million instances, respectively.

### 266 3.3 Convolutional Neural Networks

267 The structure of the CNNs trained in this study is shown in Fig. 3. It is a series  
 268 network with 2 three-dimensional convolution layers and 5 fully connected layers. The  
 269 convolution layers are followed by batch normalization layers, rectified linear unit (ReLU)  
 270 layers, and a three-dimensional max-pooling layer (for the first convolution layer) before



**Figure 4.** Precision (a–c) and recall (d–f) of the trained CNNs (RxNet). a) and d) are the RxNet for Hong Kong (HK), b) and e) for Manila (MN), c) and f) for Singapore (SG). The CNNs were trained for the thresholds indicated below the horizontal axis but their performance is evaluated against the training criteria and the 90th and 99th percentiles of rain rates.

271 connecting the fully connected layers. Training the CNNs is much more time-consuming  
 272 on a multi-core CPU than training the SVMs. However, training the CNNs on a GPU  
 273 is fast and can finish 100 epochs of iteration within a day. We trained our CNNs with  
 274 two criteria for categorizing “extremes”, the 70th and 90th percentiles of rain rates, and  
 275 we call them RxNet70 (RN70) and RxNet90 (RN90). RxNet70 was trained for 100 epochs  
 276 of iteration, RxNet90 was trained for 60 epochs. The latter were trained for fewer iter-  
 277 ations because we found RxNet90 appears to converge faster than RxNet70, probably  
 278 because the number of “extreme” events is significantly less in training the RxNet90’s  
 279 than that in training RxNet70’s.

280 Figure 4 shows the performance of the trained RxNet70 and RxNet90. For train-  
 281 ing criteria, RxNet70 exhibits precision around 0.5 and recall around 0.6. When evalu-  
 282 ated with higher percentiles (90th and 99th), its precision becomes lower than that for  
 283 the training criterion, but its recall becomes high.  $R_{90}^{RN70}$  is between 0.8 and 0.9 for the  
 284 three regions.  $R_{99}^{RN70}$  is above 0.95 for all three regions, which is much higher than the  
 285 recall of the Dual SVM model mentioned above ( $< 0.81$ ).

286 The trained RxNet90 exhibits precision between 0.3 to 0.4 for training criteria, which  
 287 is lower than that of RxNet70. However, when evaluating its performance in retrieving  
 288 the extreme events defined with the 99th percentile,  $P_{99}^{RN90}$  is significantly higher than  
 289  $P_{99}^{RN70}$ . The recall of RxNet90 for training criteria is slightly low, between 0.35 to 0.5  
 290 for the three regions. However, when being evaluated against the 99th percentile,  $R_{99}^{RN90}$   
 291 is 0.81, 0.81, and 0.72 for those three regions surrounding HK, MN, and SG, respectively.  
 292 Those recall rates are decent, considering the rarity of the extreme events with rain rates  
 293 higher than the 99th percentile.

294 The performance of the CNNs is significantly better than the Dual SVM models.  
 295 The training of Dual SVM models failed to converge for SG when the training criterion

296 was raised to the 80th percentile. By contrast, RxNet90 can reach a converged solution  
297 and has a decent recall for extreme events with rain rates higher than the 99th percentile.  
298 The optimal Dual SVM models can only filter out approximately 87% irrelevant instances  
299 of circulation data for MN and SG (94% for HK), but by contrast, applying RxNet90  
300 to circulation data can filter out approximately more than 97% (98% for HK) of irrel-  
301 evant instances. Meanwhile, the recall of RxNet90 for extreme events defined by the 90th  
302 and 99th percentiles is no less than that of the optimal Dual SVM models.

## 303 4 Conclusions

304 The sensitivity of tropical and subtropical extreme precipitation to global warm-  
305 ing is highly uncertain. By constraining climate model results with satellite observation,  
306 O’Gorman (2012) estimated that the sensitivity of tropical extreme rainfall to global warm-  
307 ing is 6–14 % K<sup>-1</sup>, which contains a significant range of uncertainty. The high end of this  
308 estimate represents the result from not only thermodynamic scaling, which is approx-  
309 imately 7 % K<sup>-1</sup> due to the moistening of the atmosphere, but also from enhanced up-  
310 ward motions in extreme events. This dynamic strengthening is certainly possible, given  
311 that the high percentiles of convective available potential energy (CAPE) increase ro-  
312 bustly in the tropics and subtropics of GCM simulations under warming (Singh et al.,  
313 2017). However, to what extent can the increase in CAPE be realized as ascending mo-  
314 tions in extreme rainstorms is not precisely known.

315 To narrow the uncertainty in the estimation of future extreme precipitation, dy-  
316 namic downscaling would give us the most reliable results. DDD is straightforward but  
317 prohibitively expensive regarding computational resource. Meanwhile, high degree of in-  
318 ternal climate variability (Deser et al., 2012; Wallace et al., 2012) requires us to sam-  
319 ple a reasonably large number of climate simulations if possible.

320 Here we demonstrated that machine learning can indeed enable SDD, in which only  
321 the large-scale patterns that have a high probability of producing extreme events are dy-  
322 namically downscaled. In our study, the best performance was obtained when training  
323 CNNs using the 90th percentile of rain rates as the threshold for labeling “extremes”.  
324 Because the distribution of precipitation intensities is continuous, it is unavoidable to  
325 have a significant number of misclassifications in the machine learning models. For this  
326 reason, we chose to train the machine learning model with a relatively low percentile (e.g.,  
327 90th percentile) as the categorizing criterion when we target to retrieve most of the ex-  
328 treme events defined by a higher percentile (e.g., 99th percentile). We found that trained  
329 deep neural network, RxNet90, is very effective in filtering out irrelevant large-scale cir-  
330 culation patterns and retaining the majority instances which are very likely to generate  
331 extreme events. We advocate using deep learning techniques to enable the SDD of ex-  
332 treme events in climate studies and advance our understanding of future climate.

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338 and Information Systems Laboratory (<https://rda.ucar.edu/datasets/ds090.0/>). The GPM  
339 IMERG precipitation data was provided by the Goddard Earth Sciences Data and In-  
340 formation Services Center (GES DISC) (<https://doi.org/10.5067/gpm/imerg/3b-hh/06>).

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