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## **Formation of the double stratopause and elevated stratopause associated with the major stratospheric sudden warming in 2018/19**

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### **Key Points:**

- A hindcast of the 2018/19 stratospheric sudden warming was performed using a gravity-wave permitting high-top general circulation model.
- Planetary waves excited by gravity wave forcing contribute to the formation of a double stratopause, two temperature peaks in the vertical.
- Both planetary wave and gravity wave forcing contribute to the formation of the elevated stratopause.

## 20 **Abstract**

21 After several recent stratospheric sudden warming (SSW) events, the stratopause disappeared  
22 and reformed at a higher altitude, forming an elevated stratopause (ES). The relative roles of  
23 atmospheric waves in the mechanism of ES formation are still not fully understood. We  
24 performed a hindcast of the 2018/19 SSW event using a gravity-wave (GW) permitting  
25 general circulation model containing the mesosphere and lower thermosphere (MLT), and  
26 analyzed dynamical phenomena throughout the entire middle atmosphere. An ES formed  
27 after the major warming on 1 January 2019. There was a marked temperature maximum in  
28 the polar upper mesosphere around 28 December 2018 prior to the disappearance of the  
29 descending stratopause associated with the SSW. This temperature structure with two maxima  
30 in the vertical is referred to as a double stratopause (DS). We showed that adiabatic heating  
31 from the residual circulation driven by GW forcing (GWF) causes barotropic and/or  
32 baroclinic instability before DS formation, causing in situ generation of planetary waves  
33 (PWs). These PWs propagate into the MLT and exert negative forcing, which contributes to  
34 DS formation. Both negative GWF and PWF above the recovered eastward jet play crucial  
35 roles in ES formation. The altitude of the recovered eastward jet, which regulates GWF and  
36 PWF height, is likely affected by the DS structure. Simple vertical propagation from the  
37 lower atmosphere is insufficient to explain the presence of the GWs observed in this event.  
38

## 39 **1 Introduction**

40 Dynamical events called stratospheric sudden warmings (SSWs) greatly alter the  
41 thermal and dynamical conditions in the winter stratosphere. They are results of the  
42 interaction between upward propagating planetary waves (PWs) and zonal mean fields  
43 (Matsuno, 1971). The occurrence of an SSW is indicated by a rapid increase in the  
44 temperature and the weakening or reversal of the eastward jet in the winter polar stratosphere.  
45 The World Meteorological Organization defines a positive poleward gradient of the zonal  
46 mean temperature from 60° latitude to the pole accompanied by a reversal of the zonal-mean  
47 zonal wind at 60° latitude at or below 10hPa as a major SSW; a minor SSW only satisfies the  
48 first condition. On the basis of the shape of the polar vortex, SSWs can also be classified into  
49 displacement and splitting events (e.g., Charlton and Polvani, 2007).

50 An SSW can be recognized as a descending stratopause. After the onset of the past  
51 several SSWs, specifically the 2006, 2009, 2013 and 2019 events, the stratopause, which has  
52 descended to a lower altitude, became indistinct and then reformed at an altitude above its  
53 climatological height. This phenomenon is called an elevated stratopause (ES) (e.g., Manney  
54 et al., 2008, 2009; Siskind et al., 2010). Several previous observational and numerical studies  
55 showed that gravity wave (GW) forcing (GWF) induces the formation and descent of the ES  
56 (e.g., Tomikawa et al., 2012; Siskind et al., 2007, 2010; Thuraiajah et al., 2014). Using a

57 GW-permitting general circulation model (GCM) of the KANTO project (Watanabe et al.,  
58 2008), Tomikawa et al. (2012) analyzed a simulated major SSW event. They showed that  
59 positive PW forcing (PWF) leads to the quick recovery of the polar eastward jet after the  
60 major SSW, and negative GWF above the recovered jet contributes to the formation of the  
61 ES. Thuraiajah et al. (2014) provided observational evidence of the enhancement of GW  
62 activity after SSWs using global high-latitude temperature measurements from the Solar  
63 Occultation for Ice Experiment (SOFIE).

64 The crucial role of PWs in the initial phase of ES formation has also been suggested  
65 (e.g., Limpasuvan et al., 2012, 2016; Chandran et al., 2011, 2013). Limpasuvan et al. (2016)  
66 conducted a composite analysis of 13 SSW-ES events identified in the runs of the Whole  
67 Atmosphere Community Climate Model, Version 4 with specified dynamics (SD-WACCM)  
68 for 1990–2013. They showed that downward flow induced by negative PWF in the polar  
69 mesosphere and lower thermosphere (MLT) is responsible for ES formation. Several  
70 observational studies have pointed out that the amplitudes of PWs with zonal wavenumber  
71  $s=1-2$  increase in the MLT when an ES event occurs (e.g., Stray et al., 2015). However, it  
72 has also been indicated that PWF in the MLT is not necessarily strong during ES formation.  
73 Chandran et al. (2013) showed that in a few events in model simulations, the entire process of  
74 ES formation appears to be driven by GWF despite the climatological importance of PWF.  
75 The relative contributions of GWs and PWs to ES formation remain to be elucidated.

76 The ES phenomenon, which is accompanied by downwelling in the MLT, strongly  
77 influences downward material transport and thus the coupling between the MLT and the  
78 stratosphere (e.g., Randall et al., 2009). For example,  $\text{NO}_x$  ( $=\text{NO}+\text{NO}_2$ ) produced by  
79 energetic particle precipitation (EPP) in the MLT is transported into the stratosphere,  
80 especially during ES events that occur in early winter. In the region under the influence of the  
81 polar night,  $\text{NO}_x$  is long-lived and causes ozone depletion in the stratosphere (e.g., Holt et al.,  
82 2013; Randall et al., 2009). This effect, referred to as the EPP indirect effect, is very  
83 important in chemistry–climate models because it affects the dynamics of the stratosphere  
84 (e.g., Siskind et al., 2015). Smith et al. (2018) also pointed out that the enhanced downward  
85 flow associated with ES events results in a downward shift in the maximum altitude of ozone  
86 concentrations.

87 However, most high-top models tend to underestimate downward material transport in  
88 the MLT during ES events (e.g., Randall et al., 2015; Orsolini et al., 2017). In addition, ES  
89 height is generally lower in the model than in observation data. These model biases are the  
90 results of the underestimation (overestimation) of downward motion in the upper (lower)  
91 mesosphere (e.g., Funke et al., 2017). Meraner et al. (2016) showed that the intensity of the  
92 parameterized nonorographic GW sources affects the height of GWF in the MLT. The  
93 modulation of the height of GWF can affect the amount of downward material transport.

94 They reported that weaker GW sources in the parameterization yield a better agreement of  
95 simulations with observations.

96 To elucidate the relative importance of PWs and GWs in dynamical phenomena in the  
97 middle atmosphere, the in-situ generation of waves should be taken into consideration.  
98 Several studies showed that strong Rossby wave (RW) breaking causes the barotropic (BT)  
99 and/or baroclinic (BC) instability, which excites RWs (e.g., Baldwin and Holton, 1988;  
100 Hitchman and Huesmann, 2007; Greer et al., 2013). Smith (1996, 2003) suggested that  
101 momentum deposit by the GWs that have been filtered by planetary-scale wind structures in  
102 the stratosphere lead to in situ generation of PWs in the middle and upper mesosphere. On the  
103 basis of a case study of a boreal winter using the KANTO model, Sato and Nomoto (2015)  
104 suggested the importance of the interplay of GWs and PWs in the middle atmosphere. They  
105 provided evidence of in-situ PW generation due to the BT/BC instability resulting from the  
106 generation of a potential vorticity (PV) maximum attributed to GWF. Positive and negative  
107 PWFs associated with the PW generation act to eliminate this PV maximum. Using the  
108 KANTO model, Watanabe et al. (2009) showed that in the Antarctic winter mesosphere  
109 eastward 4-day waves are generated by the BT/BC instability which develops in the large-  
110 scale mean flow strongly distorted by GWF. Sato et al. (2018) and Yasui et al. (2018) showed  
111 that the BT/BC instability and shear instability caused by GWs originating from the lower  
112 atmosphere generate RWs and GWs in the mesosphere, respectively. Recently, Vadas and  
113 Becker (2018) suggested that momentum deposit associated with the breaking of orographic  
114 GWs generates secondary GWs in the stratosphere and lower mesosphere in the southern  
115 polar region in winter.

116 Most high-top GCMs include GW parameterizations. In general, GW  
117 parameterization schemes assume that GWs originate only from the lower atmosphere. In-situ  
118 generation of GWs in the middle atmosphere is ignored in these parameterizations. In  
119 addition, most standard GW parameterizations also assume that GWs propagate only  
120 vertically. However, using the KANTO model, Sato (2009; 2012) showed evidence of lateral  
121 propagation of GWs and provided theoretical explanations of the mechanisms involved.  
122 Conducting ray-tracing simulations, Yamashita et al. (2013) also suggested that high GW  
123 activity in the MLT during ES events observed by the Sounding of the Atmosphere using  
124 Broadband Emission Radiometry (SABER) on the Thermosphere, Ionosphere, Mesosphere  
125 Energetics Dynamics (TIMED) satellite is caused by poleward propagating GWs.

126 In this study, we used a high-top and GW-permitting GCM to examine an SSW-ES  
127 event that occurred in January 2019 in the actual atmosphere. We focused on the relative  
128 roles of GWs and PWs to elucidate the mechanism of the dynamical modification of the  
129 middle atmosphere during this event. Since GWs are explicitly resolved in the model, the in-  
130 situ generation and lateral propagation of GWs are also simulated. Three-dimensional

131 analysis methods are also applied because zonal asymmetry is pronounced especially in the  
132 ES structures associated with displacement-type SSWs (Chandran et al., 2014; France and  
133 Harvey, 2013). The methods of analysis and details of the model used in this study are  
134 described in section 2. In section 3, the results are shown and discussed particularly in terms  
135 of the mechanism of the dynamical variation associated with the SSW. Characteristics of  
136 waves observed in the middle atmosphere are also shown. Summary and concluding remarks  
137 are given in section 4.

138

## 139 **2 Methods and model description**

140 In this study, we performed simulations of the 2018/19 SSW event using the Japanese  
141 Atmospheric General circulation model for Upper Atmosphere Research (JAGUAR)  
142 (Watanabe and Miyahara, 2009). The model has 340 vertical layers from the surface to a  
143 geopotential height of approximately 150 km with a log-pressure height interval of 300 m  
144 throughout the middle atmosphere and a horizontal, triangularly truncated spectral resolution  
145 of T639 that has a minimum resolvable horizontal wavelength of ~60 km. No  
146 parameterization for subgrid-scale GWs was used in this study.

147 The model resolutions are insufficient to resolve very small-scale GWs with  
148 horizontal wavelengths of < 60 km. Using observation data from the PANSY radar (Program  
149 of the Antarctic Syowa MST/IS radar) installed at Syowa Station (69.0° S, 39.6° E), Shibuya  
150 et al. (2017) and Shibuya and Sato (2019) showed the dominance of GWs with horizontal  
151 wavelengths in excess of 1,000 km and vertical wavelengths of about 14 km in the  
152 mesosphere. On the basis of PANSY radar observation data, Sato et al. (2017) showed that  
153 most GW momentum fluxes are associated with waves having long periods of several hours  
154 to a day at the southern high latitudes in summer. Ern et al. (2018) analyzed the satellite  
155 observation data and showed that dominant GWs in the middle atmosphere on average have  
156 horizontal wavelengths in excess of 1,000 km and vertical wavelengths in excess of 10 km. In  
157 addition, Watanabe et al. (2008) showed that a T213L256 GCM (the KANTO model) that  
158 explicitly resolves GWs can reproduce major characteristics of the zonal mean flow and  
159 temperature in the middle atmosphere. Thus, it is considered that the model used in this study  
160 is able to realistically resolve a major part of GWs in the middle atmosphere.

161 Koshin et al. (2020) recently developed a four-dimensional local ensemble transform  
162 Kalman filter (4D-LETKF) assimilation system in a medium-resolution (T42L124) version of  
163 the JAGUAR, and assimilated the PrepBUFR observational dataset provided by the National  
164 Centers for Environmental Prediction (NCEP) and satellite temperature data from the Aura  
165 Microwave Limb Sounder (MLS). They also improved the quality of the analysis data by  
166 introducing a filter called incremental analysis updates (Bloom et al., 1996) and assimilating  
167 the temperature data from SABER and brightness temperature data from Special Sensor

168 Microwave Imager/Sounder (SSMIS) (private communication). Using the products from the  
 169 updated assimilation system from Koshin et al. (2020) as initial values for the high-resolution  
 170 JAGUAR, a hindcast of the 2018/19 SSW event was carried out. The time period of  
 171 simulation is from 5 December 2018 to 17 January 2019. This time period was divided into  
 172 consecutive periods of 4 days. An independent model run was performed for each 4-day  
 173 period. Each model run consists of 1-day nudging, 2-day spin up and 4-day free run. We  
 174 analyzed the output data from the 4-day free runs.

175 The transformed Eulerian mean (TEM) primitive equations were used for diagnosing  
 176 wave forcing and residual mean circulation (e.g., Andrews and McIntyre, 1976). In the TEM  
 177 system, the Eliassen–Palm (EP) flux represents the direction of wave activity flux and its  
 178 divergence (convergence) represents positive (negative) wave forcing. In addition, to  
 179 visualize the longitudinal structure of residual mean circulation, we calculated three-  
 180 dimensional residual mean vertical flow using the formula derived by Kinoshita et al. (2019):

$$\bar{w}^* = \bar{w} + \left( \frac{u_g \theta}{\theta_{0z}} \right)_x + \left( \frac{v_g \theta}{\theta_{0z}} \right)_y \quad (1)$$

181 where  $\bar{A}$  denotes the time mean of  $A$ , and  $u_g$  and  $v_g$  are geostrophic zonal and meridional  
 182 flows, respectively; the suffixes  $x$  and  $y$  denote the respective partial derivatives in the  
 183 zonal and meridional directions;  $\theta$  and  $\theta_0$  are the potential temperature and reference  
 184 potential temperature, which is defined as  $\theta_0 = (gH/R)e^{\kappa z/H}$ ;  $g$  represents the  
 185 gravitational acceleration;  $H$  is scale height ( $= 7$  km);  $R$  is the gas constant of dry air;  $\kappa$  is  
 186 a dimensionless value and is defined as  $R/c_p$ , where  $c_p$  denotes specific heat at constant  
 187 pressure. Equation (1) is the deformed form of the original equation of  $\bar{w}^*$  in Kinoshita et al.  
 188 (2019), using  $[A]_x = 0$  and  $[v_g] = 0$ , where  $[A]$  denotes the zonal mean of  $A$ . This  
 189 vertical flow contains the Stokes drift associated with transient and stationary waves.  
 190 Moreover, apparent vertical motions along the undulated isentropic surfaces associated with  
 191 the stationary waves are excluded. Thus, equation (1) represents the diabatic flow crossing  
 192 the isentropic surfaces. In this study, we set the period of the time mean to four days.

193 To analyze three-dimensional wave propagation and forcing, we also used the two  
 194 types of three-dimensional wave activity flux of Kinoshita and Sato (2013), namely 3D-flux-  
 195 W and 3D-flux-M. The components of 3D-flux-W that are associated with the flux of zonal  
 196 momentum are as follows:

$$\mathbf{F}_{W1} = \rho_0 \begin{pmatrix} \frac{1}{2} \left( \overline{u'^2} - \overline{v'^2} + \frac{\overline{\Phi_z'^2}}{N^2} \right) \\ \overline{u'v'} \\ \overline{u'w'} - f \frac{\overline{v'\Phi_z'}}{N^2} \end{pmatrix} \quad (2)$$

197 where  $\rho_0$  denotes reference density. The 3D-flux-M is given as follows:

$$\mathbf{F}_1 = \rho_0 \begin{pmatrix} \overline{u'^2} - \overline{S_{(p)}} + \bar{u}_y \frac{\overline{S_{(p)}}}{f} - \bar{u}_z \frac{\overline{u'\Phi'_z}}{N^2} \\ \overline{u'v'} - \bar{u}_x \frac{\overline{S_{(p)}}}{f} - \bar{u}_z \frac{\overline{u'\Phi'_z}}{N^2} \\ \overline{u'w'} + -\bar{u}_x \frac{\overline{u'\Phi'_z}}{N^2} + (\bar{u}_y - f) \frac{\overline{v'\Phi'_z}}{N^2} \end{pmatrix} \quad (3)$$

198 where

$$S_{(p)} = \frac{1}{2} \left( \overline{u'^2} + \overline{v'^2} - \frac{\overline{u'\Phi'_y}}{f} + \frac{\overline{v'\Phi'_x}}{f} \right) \quad (4)$$

199 These formulae were originally derived for transient waves, but they hold for stationary  
 200 waves if the wave component is extracted properly and an appropriate average is made (Sato  
 201 et al., 2013). To analyze the wave activity fluxes associated with both transient and stationary  
 202 PWs, we examined components having zonal wavenumbers  $s=1-3$  as the perturbation field  
 203 and applied an extended Hilbert transform proposed by Sato et al. (2013) to eliminate phase  
 204 dependency of waves instead of time averaging. Since the zonal mean flow is taken as the  
 205 background field,  $\bar{u}_x$  in the equation (3) is eliminated.

206 Kinoshita and Sato (2013) showed that the divergence of 3D-flux-M corresponds to  
 207 the wave forcing that causes the three-dimensional residual mean flow, and 3D-flux-W agrees  
 208 well with the direction of the group velocity of RWs. Thus, in the present study, we used the  
 209 divergence of 3D-flux-M to examine the three-dimensional structure of wave forcing, and  
 210 3D-flux-W to analyze the characteristics of PW propagation. In the figures that follow, each  
 211 component of  $\mathbf{F}_{W1}$  is shown with the sign reversed to match the direction of the group  
 212 velocity of RWs.

213 For the analysis of the dynamical stability of mean flow, we used the modified  
 214 potential vorticity (MPV) defined by Lait (1994) as the Ertel's potential vorticity weighted by  
 215  $\theta^{-9/2}$ . In this paper, MPV is denoted by  $P_M$ . It roughly represents the product of absolute  
 216 vorticity and the square of the Brunt–Väisälä frequency  $N^2$  including perturbations (e.g.,  
 217 Sato and Nomoto, 2015).

218

### 219 **3 Results and discussion**

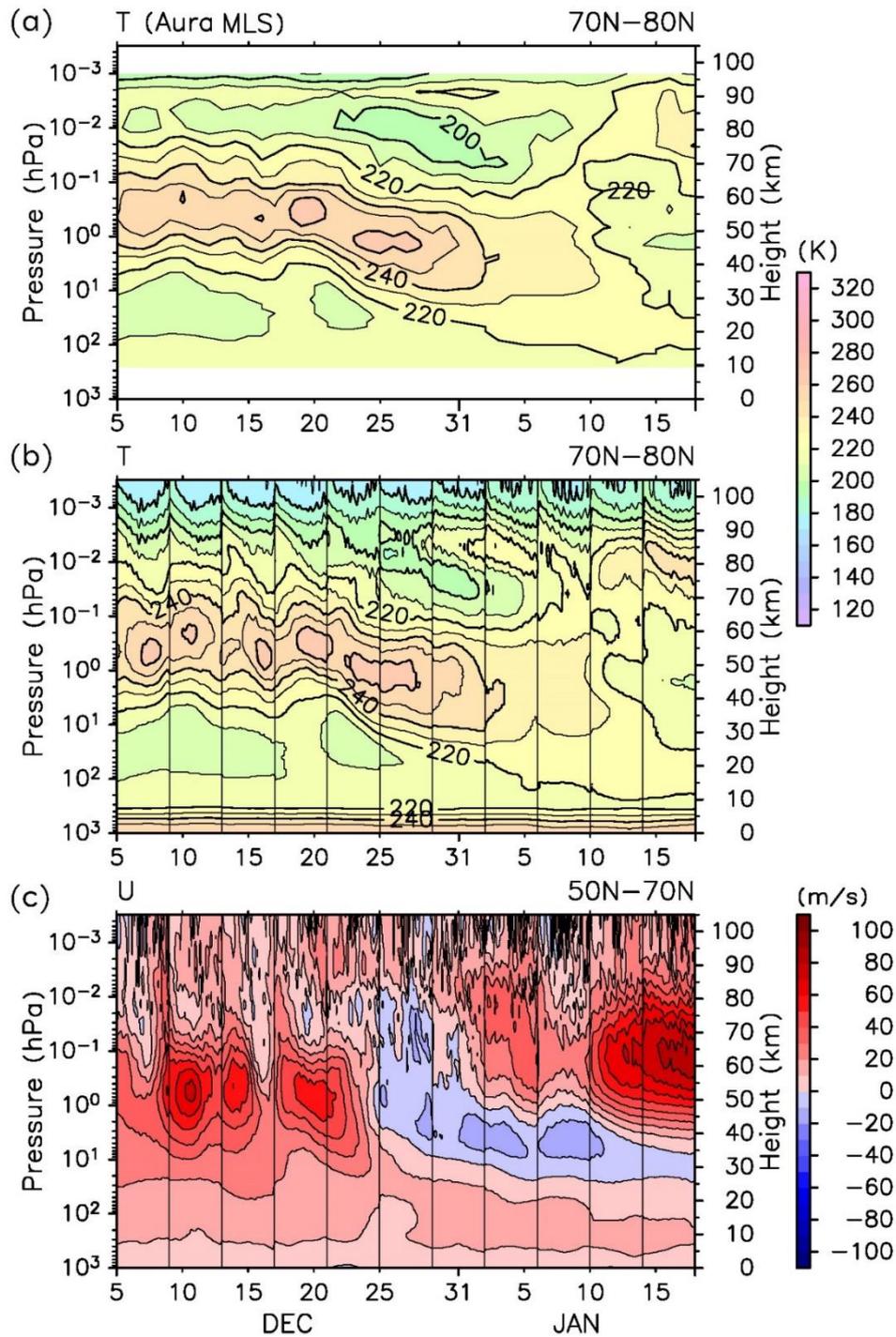
#### 220 **3.1 Overall features of the 2018/19 SSW event**

221 The 2018/19 SSW event is classified as a displacement-type ( $s=1$ ) SSW and the onset  
 222 of the major warming occurred on 1 January 2019. Figure 1 shows the time–height sections  
 223 of zonal mean temperature  $[T]$  and zonal wind  $[u]$ . Figure 1a shows temperature data from  
 224 the MLS on the Aura satellite that have been bias-corrected with TIMED SABER data  
 225 (Koshin et al., 2020). Figures 1b and 1c show model results. According to the model, the

226 stratopause begins to descend from a climatological height of  $z \sim 55$  km in association with  
 227 the SSW around 22 December 2018 (Fig. 1b). Zonal-mean zonal winds  $[u]$  are reversed in  
 228 the region of  $z = 40\text{--}80$  km around 25 December (Fig. 1c). Following that, the stratopause  
 229 and the peak of westward wind gradually descend to  $z \sim 35$  km.

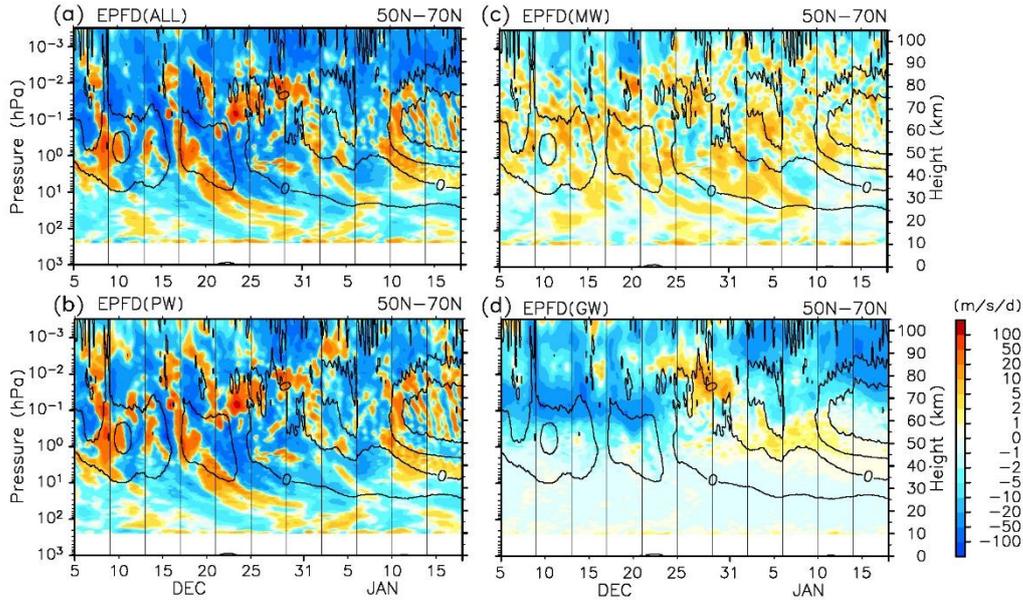
230 A strong temperature maximum is formed at  $z \sim 85$  km around 28 December during  
 231 the descent of the stratopause. This characteristic vertical structure of temperature with two  
 232 peaks is referred to as the double stratopause (DS) in this study. After 10 January, the  
 233 eastward wind is accelerated at  $z \sim 65$  km and the ES is at  $z \sim 80$  km. The heights of the  
 234 DS and ES in the model are consistent with those indicated by the temperature data from the  
 235 Aura MLS (Fig. 1a) within  $z = \pm 5$  km. The higher DS peak is located at  $z \sim 90$  km and the  
 236 ES is at  $z \sim 80$  km in the Aura MLS data. Other temperature structures in the model results  
 237 are generally consistent with the observation data. Note that the ES is separated from the  
 238 upper stratopause of the DS.

239 Waves were divided into three components and analyzed separately: PWs having  
 240 zonal wavenumber  $s = 1\text{--}3$ , medium-scale waves (MWs) having  $s > 3$  and total horizontal  
 241 wavenumber  $n < 21$  and GWs having  $n = 21\text{--}639$ . Figure 2 shows the time–height sections  
 242 of EP flux divergence (EPFD) [ $\text{EPFD} = (\rho_0 a \cos \varphi)^{-1} \nabla \cdot \mathbf{F}$ , where  $a$  is the earth's radius  
 243 and  $\mathbf{F}$  is EP flux] for respective wave components. Positive (negative) EPFD represents  
 244 eastward (westward) momentum deposit by waves. In the present study, ‘positive (negative)’  
 245 wave forcing means eastward (westward) momentum deposit. The EPFD was smoothed with  
 246 a lowpass filter with a cutoff of one day. During 23–31 December including the period when  
 247 the DS is present, GWF is strongly positive in the region of  $z = 65\text{--}90$  km. Around the time  
 248 of the formation of the DS, PWF takes a strongly negative value of  $\sim -50 \text{ m s}^{-1} \text{ d}^{-1}$  above  $z =$   
 249 83 km. This negative PWF likely contributes to DS formation. Around 10 January when the  
 250 ES is formed, GWF and PWF are negative above  $z = 70$  km and 80 km, respectively,  
 251 suggesting that both negative wave forcings are responsible for ES formation. The  
 252 mechanisms of the formation of the DS and ES are discussed in detail in sections 3.2.  
 253 Because forcing by MWs is always weak at any height or time, the following sections focus  
 254 only on PWF and GWF.  
 255



256

257 **Figure 1.** Time–height sections of 70° N–80° N regional mean  $[T]$  from (a) the Aura MLS  
 258 and (b) JAGUAR-T639L340 simulation, and (c) 50° N–70° N regional mean  $[u]$  from the  
 259 JAGUAR-T639L340 simulation. Vertical lines in (b) and (c) represent the boundaries of the  
 260 model runs.



261 **Figure 2.** Time–height sections of 50° N–70° N regional mean EPFD of (a) all wave  
 262 components, (b) PW, (c) MW, and (d) GW (shadings) and 50° N–70° N regional mean  $[u]$   
 263 (contour interval: 20 m s<sup>-1</sup>). Vertical lines represent the boundaries of the model runs.  
 264

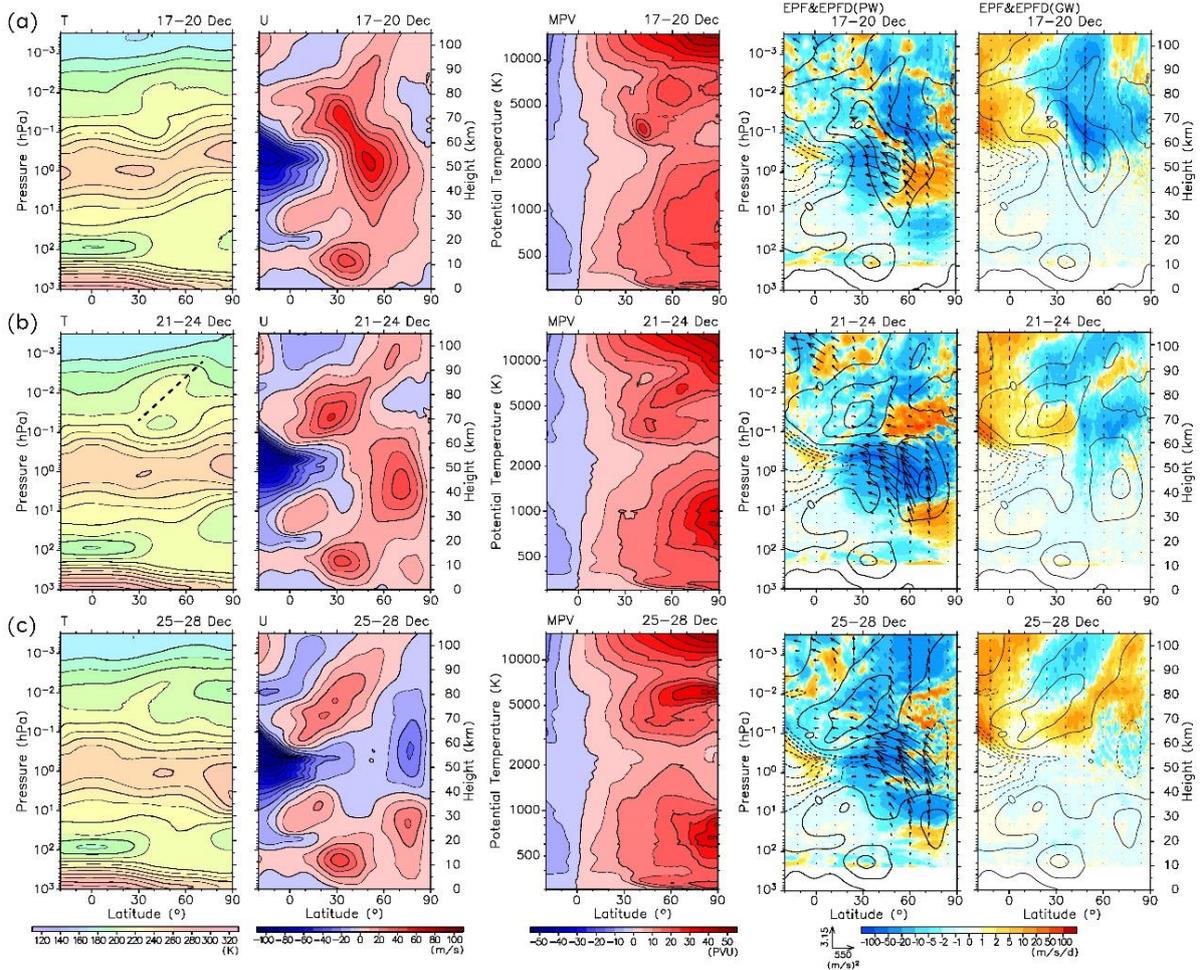
### 265 3.2 Mechanisms of the formation of the DS and ES

266 To elucidate the mechanisms of the formation of the DS and ES, time evolutions of  
 267 the zonal mean fields and horizontal structures of the mean flow and wave forcing are  
 268 examined in this section.

#### 269 3.2.1 The formation of the DS during 25–28 December 2018

##### 270 3.2.1.1 Meridional cross section

271 Figure 3 shows the meridional cross sections of zonal mean and four-day mean fields  
 272 of temperature, zonal wind, MPV, and EP flux and EPFD of PWs and GWs for 17–20, 21–24  
 273 and 25–28 December 2018. The DS is formed around 28 December (Figs. 1a and 1b). To  
 274 accentuate vectors in the middle atmosphere, EP flux vectors are divided by  $\rho_0 a$  in all the  
 275 figures. In 17–20 December, there is a strong eastward polar night jet, and its axis is at ~50°  
 276 N and  $z = \sim 52$  km (Fig. 3a). Westward wind is observed equatorward of this eastward jet;  
 277 GWF is strongly negative up to  $\sim 50$  m s<sup>-1</sup> d<sup>-1</sup> at ~50° N and  $z = \sim 65$  km above the eastward  
 278 jet, and positive above the westward wind region. These GWF features are likely results of  
 279 the filtering effect by the eastward and westward mean wind below.



280 **Figure 3.** Latitude–height sections of (from left to right) 4-day mean  $[T]$ ,  $[u]$ ,  $[P_M]$  and EP  
 281 flux scaled by  $\rho_0 a$  (vectors) and EPFD (shadings) of PWs and GWs for (a) 17–20, (b) 21–  
 282 24, and (c) 25–28 December 2018. Contours in the figures of EP flux and EPFD denote  $[u]$   
 283 (contour interval =  $20 \text{ m s}^{-1}$ ). A dashed line in the temperature figure in (b) shows the region  
 284 with relatively high temperature in the mesosphere (see section 3.2).

285

286 There is a notable peak of  $[P_M]$  at  $\sim 40^\circ \text{ N}$  and  $\theta = \sim 3,500 \text{ K}$  ( $z = \sim 65 \text{ km}$ ), which is  
 287 located on the boundary between the negative and positive GWs. Wave-induced residual  
 288 mean vertical wind is upward in the lower region on the poleward (equatorward) side of  
 289 positive (negative) wave forcing. These GWF and  $[P_M]$  features suggest that the  $[P_M]$  peak  
 290 is a result of an increase in  $N^2$  above the residual mean upward flow at  $\sim 40^\circ \text{ N}$  (not shown,  
 291 cf. section 3.2.1b), which is induced by the positive and negative GWs.

292 During 17–20 December, PWF is positive poleward of  $\sim 55^\circ \text{ N}$  at  $z = 35\text{--}55 \text{ km}$ ; PW  
 293 packets propagate toward the region with weak  $[u]$  at  $\sim 30^\circ \text{ N}$ ,  $z = 40\text{--}65 \text{ km}$  and toward  $40^\circ$   
 294  $\text{N}\text{--}70^\circ \text{ N}$ ,  $z = 60\text{--}85 \text{ km}$  by way of the eastward jet, which has its axis at  $\sim 50^\circ \text{ N}$ ,  $z = \sim 52 \text{ km}$ .  
 295 In both regions, PWF is negative. The negative PWF in the latter region may also contribute

296 to the upwelling at  $\sim 40^\circ$  N and the increase in  $N^2$  and  $[P_M]$ . However, the boundary of the  
 297 positive and negative total wave forcing (not shown) match well with that of the positive and  
 298 negative GWFs. Thus, the location and strength of the upwelling are mainly determined by  
 299 the GWFs.

300 During 21–24 December, the eastward jet is split into two segments. One segment is  
 301 shifted poleward and downward and located at  $\sim 72^\circ$  N,  $z = \sim 42$  km and the other segment  
 302 tilts poleward from the equator at  $z = \sim 65$  km to the winter pole at  $z = \sim 100$  km with its axis  
 303 at  $\sim 25^\circ$  N,  $z = \sim 72$  km (Fig. 3b). This segmentation of the jet may be caused by negative  
 304 GWF and PWF that are present during 17–20 December in the region where the split occurs.  
 305 During 21–24 December, GWF is negative (positive) above (below) the latter, poleward-  
 306 tilting eastward jet, and is consistent with the GW filtering effect of this jet. The temperature  
 307 cross section shows relatively high temperature between  $30^\circ$  N,  $z = \sim 70$  km and  $70^\circ$  N,  $z =$   
 308  $\sim 95$  km. The region with relatively high temperature is marked by a dashed line in Fig. 3b  
 309 and corresponds to the area between the negative and positive GWFs along the mesospheric  
 310 jet. This fact suggests that the high temperature is caused by adiabatic heating associated with  
 311 residual mean downwelling (not shown) induced by these GWFs.

312 Poleward of  $10^\circ$  N in the middle and upper stratosphere at  $z = 35$ – $60$  km during 21–  
 313 24 December, PWF is strongly negative with a maximum of over  $50 \text{ m s}^{-1} \text{ d}^{-1}$ , and is present  
 314 continuously until 25–28 December (Fig. 3c). It is inferred that the SSW is caused by this  
 315 PWF. During 21–24 December, PWF is positive to the north of  $\sim 40^\circ$  N at  $z = 60$ – $80$  km (Fig.  
 316 3b), and the  $[P_M]$  peak that is present during 17–20 December at  $\sim 40^\circ$  N and  $\theta = \sim 3,500$  K  
 317 becomes weak. According to the quasi-geostrophic theory, a positive EPFD is equivalent to a  
 318 poleward PV flux, while a negative EPFD indicates an equatorward PV flux (Andrews et al.,  
 319 1987). The observed PWF features suggest that the positive wave forcing is associated with  
 320 the PW generation due to the BT/BC instability weakening the negative  $[P_M]_y$ , which is a  
 321 necessary condition for the BT/BC instability. During this period, a  $[P_M]$  peak becomes  
 322 obvious from  $\sim 50^\circ$  N,  $\theta = \sim 5,500$  K ( $z = \sim 80$  km) to  $\sim 80^\circ$  N,  $\theta = \sim 7,000$  K ( $z = \sim 85$  km). It is  
 323 slightly below the region with relatively high temperature, which is marked by the dashed  
 324 line in Fig. 3b. Thus, it is implied that this  $[P_M]$  peak is caused by the increase of  $N^2$  under  
 325 the temperature maximum associated with the isothermal folding.

326 During 25–28 December, a westward jet with a peak at  $z = \sim 57$  km,  $\sim 80^\circ$  N is formed  
 327 in the polar upper stratosphere and mesosphere (Fig. 3c). The stratopause shifts downward  
 328 from  $z = \sim 52$  km in 21–24 December to  $z = 38$  km corresponding to the SSW. A relatively  
 329 weak maximum in the vertical profile of  $[T]$  is formed to the north of  $60^\circ$  N at  $z = \sim 88$  km.  
 330 This structure with two maxima in the vertical profile is the DS. Poleward of  $55^\circ$  N at  $z =$   
 331  $67$ – $82$  km, where the  $[P_M]_y$  is negative in 21–24 December, PWF becomes positive during  
 332 25–28 December and the  $[P_M]_y < 0$  region almost disappears. These results suggest in-situ

333 PW generation due to the BT/BC instability at  $z=67\text{--}82$  km during 25–28 December, which  
 334 is similar to the model results at  $>40^\circ$  N,  $z=60\text{--}80$  km from 21–24 December.

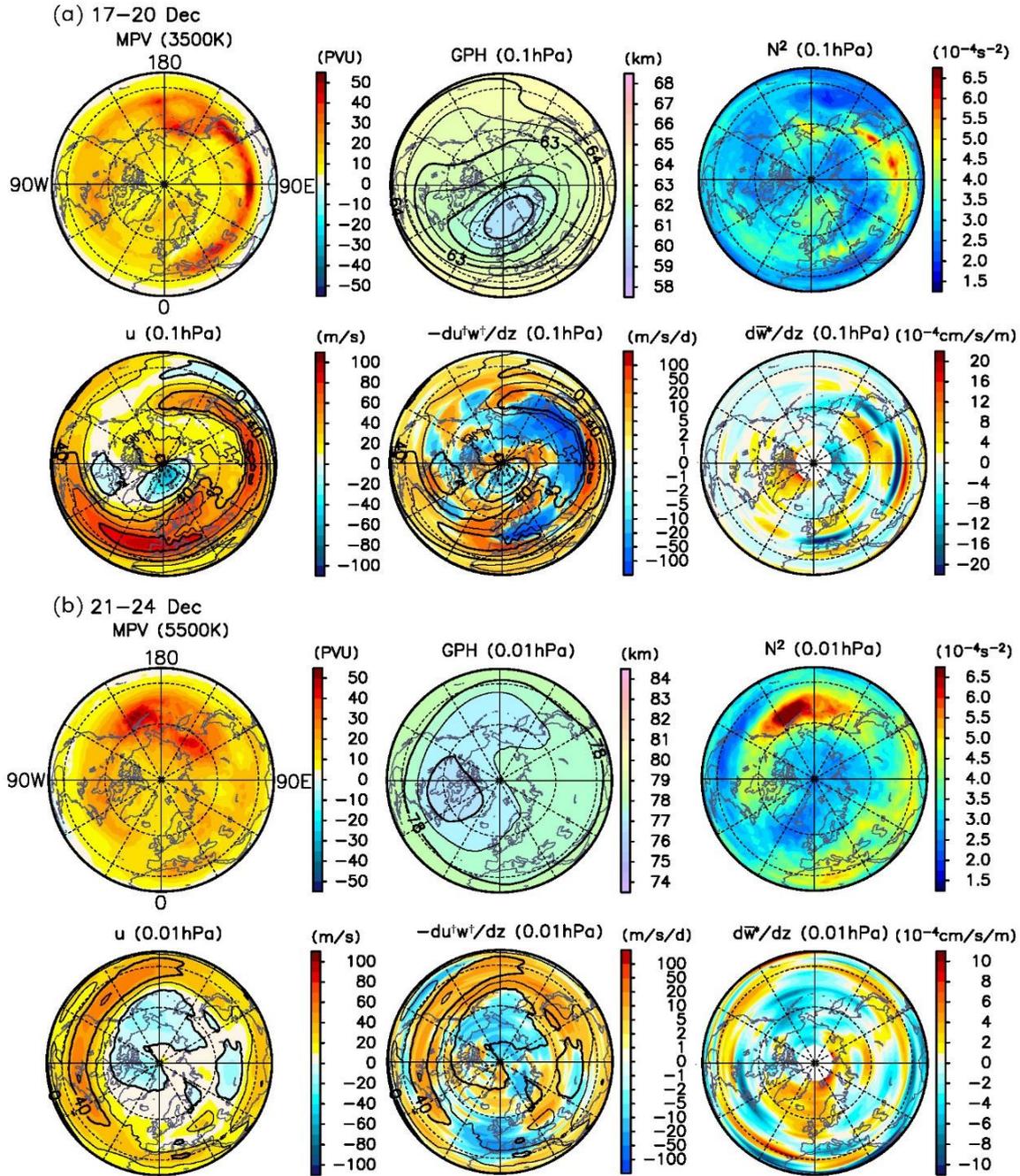
335 During 25–28 December, a negative PWF of  $\sim -20$  m s<sup>-1</sup> d<sup>-1</sup> extends to the north of  
 336  $35^\circ$  N above  $z=85$  km, and a positive GWF of  $\sim 10$  m s<sup>-1</sup> d<sup>-1</sup> is in the polar MLT. Because  
 337 the positive GWF is weaker than the negative PWF, the total wave forcing is negative in the  
 338 polar MLT ( $z > 80$  km) (Fig. 2a). Thus, the negative PWF at the middle and high latitudes in  
 339 the MLT is responsible for DS formation by causing downwelling in the polar MLT and the  
 340 subsequent adiabatic heating.

341 During 25–28 December, the mean zonal wind is westward over a wide area above  
 342  $z > 40$  km in the polar upper stratosphere and mesosphere. According to the Charney and  
 343 Drazin theorem (1961), PWs from the troposphere hardly propagate upward in the westward  
 344 wind and reach the MLT. Thus, it is inferred that the in situ generated PWs propagate upward  
 345 and exert negative forcing in the MLT, leading to the formation of the DS.

#### 346 3.2.1.2 Horizontal structure

347 To analyze the horizontal structures of  $P_M$  and wave forcing, orthographic projection  
 348 maps of the Northern Hemisphere for  $P_M$ , geopotential height (GPH),  $N^2$ ,  $u$ ,  $-du^\dagger w^\dagger/dz$   
 349 due to GWs, where  $\dagger$  denotes the GW components, and the vertical gradient of residual  
 350 mean vertical flow  $d\bar{w}^*/dz$  at  $\theta = \sim 3,500$  K and 0.1 hPa ( $z = \sim 65$  km) during 17–20  
 351 December are shown in Fig. 4a. The maps for  $-du^\dagger w^\dagger/dz$  and  $d\bar{w}^*/dz$  fields have been  
 352 smoothed with a lowpass filter with a cutoff of  $s=6$  to show the large-scale structures more  
 353 clearly. Calculations of  $d\bar{w}^*/dz$  were performed using  $\bar{w}^*$  at  $\pm 5$  km adjacent vertical  
 354 levels;  $-du^\dagger w^\dagger/dz$  approximately corresponds to GWF, and  $P_M$  is roughly proportional to  
 355 the product of absolute vorticity  $f + \zeta$  and  $N^2$  (Sato and Nomoto, 2015).

356 The region of high  $P_M$  at  $\sim 40^\circ$  N, which corresponds to the region of  $[P_M]$   
 357 maximum in Fig. 3a, matches with the region of high  $N^2$  and does not match with the region  
 358 of the center of the polar vortex in the GPH maps. High  $N^2$  is distributed along a strip at  
 359  $\sim 40^\circ$  N,  $0^\circ\text{--}150^\circ$  E, between the regions of strongly positive and negative GWFs near the  
 360 eastward jet. The strongly negative  $d\bar{w}^*/dz$ , which is located above strong upwelling at  $\sim 0.2$   
 361 hPa ( $z = \sim 60$  km) (not shown), is observed at almost the same latitudes and longitudes as high  
 362  $N^2$ . These features indicate that the  $[P_M]$  enhancement in the zonal mean field (Fig. 3a) is  
 363 mainly caused by  $N^2$  increase in the region of  $\bar{w}^*$  convergence at the top of the upwelling  
 364 induced by GWF, and is similar to the mechanism shown by Sato and Nomoto (2015).



365

366 **Figure 4.** Orthographic projection maps of the Northern Hemisphere showing 4-day mean  
 367 (top left to bottom right)  $P_M$ , GPH,  $N^2$ ,  $u$ ,  $-du^\dagger w^\dagger/dz$ , and  $d\bar{w}^*/dz$  at (a) 0.1 hPa and  
 368  $\theta = 3,500$  K ( $z \sim 65$  km) for 17–20 December 2018 and (b) 0.01 hPa and  $\theta = 5,500$  K ( $z =$   
 369  $\sim 80$  km) for 21–24 December 2018. Contours in the figures of  $-du^\dagger w^\dagger/dz$  denote  $u$   
 370 ( $\text{contour interval} = 20 \text{ m s}^{-1}$ ). The maps for  $-du^\dagger w^\dagger/dz$  and  $d\bar{w}^*/dz$  have been zonally  
 371 smoothed with a lowpass filter with a cutoff of  $s = 6$ . Note that the color bar of  $d\bar{w}^*/dz$  in  
 372 (a) is different from that in (b).

373

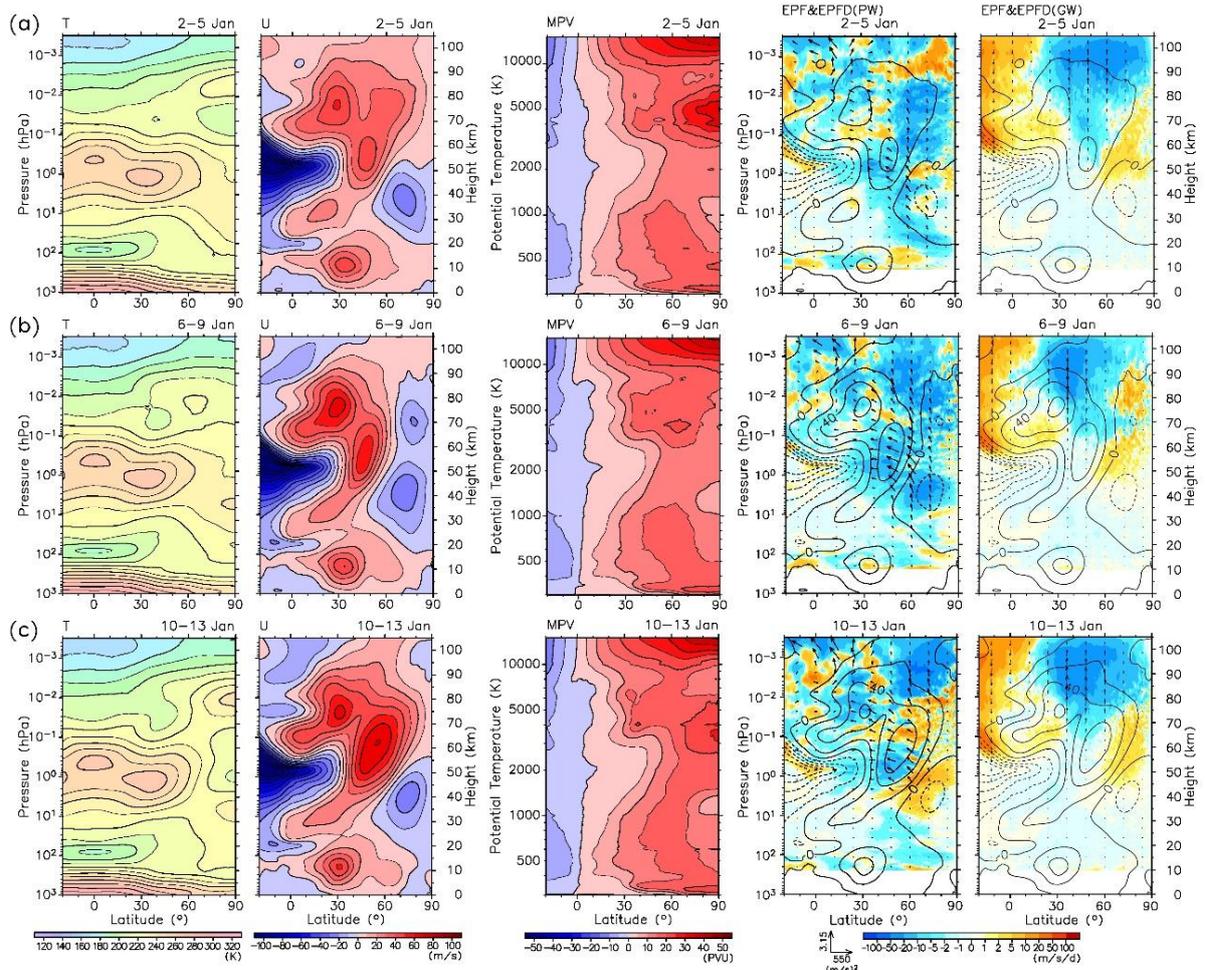
374 Figure 4b shows orographic projection maps of  $P_M$ , GPH,  $N^2$ ,  $u$ ,  $-du^\dagger w^\dagger/dz$  and  
 375  $\bar{w}^*$  for 21–24 December at  $\theta = \sim 5,500$  K and 0.01 hPa ( $z = \sim 80$  km) in the Northern  
 376 Hemisphere. Similar to the period of 17–20 December, the region of high  $P_M$  at  $\sim 50^\circ$  N,  
 377  $120^\circ$  E– $120^\circ$  W roughly corresponds to the region of high  $N^2$ . For the region of  $\bar{w}^*$   
 378 convergence (divergence),  $N^2$  is high (low), and  $\bar{w}^* > 0$  lies below and  $\bar{w}^* < 0$  lies above  
 379 (not shown). The region of convergence is located near the region of strongly positive GWF  
 380 (i.e., positive  $-du^\dagger w^\dagger/dz$ ), which is found along the eastward jet. In addition, negative  
 381 GWF is found equatorward of the region of positive GWF. The zonal mean of these GWFs  
 382 are tilted toward the higher latitudes at the same altitudes as the tilted mesospheric eastward  
 383 jet (Fig. 3b). The residual mean downward flow is induced between the negative and positive  
 384 GWFs, while the residual mean upward flow is below and poleward of the positive GWF.  
 385 Thus, it is inferred that the region of  $\bar{w}^*$  convergence near the positive GWF is caused by  
 386 this residual mean flow structure. The features observed in the maps support the inference  
 387 from the zonal mean fields that the  $P_M$  peak is formed as a result of  $N^2$  increase induced by  
 388 the convergence of the residual mean vertical flow, which is caused by the pair of negative  
 389 and positive GWFs around the mesospheric eastward jet.

390

391 3.2.2 The formation of the ES during 10–13 January, 2019

392 3.2.2.1 Meridional cross section

393 To examine the mechanism of ES formation, latitude–height sections of  $[T]$ ,  $[u]$ ,  
 394  $[P_M]$  and EP flux and EPFD of PWs and GWs after the SSW onset on 1 January for the time  
 395 periods of 2–5, 6–9 and 10–13 January are shown in Fig. 5. The ES becomes visible at  $z =$   
 396  $\sim 80$  km to the north of  $70^\circ$  N during 10–13 January (Fig. 5c). The upper  $[T]$  maximum in  
 397 the polar MLT is 220–230 K during 2–5 January, which is higher than the upper maximum  
 398 (200–210 K) of the DS during 25–28 December (Fig. 3c). During 2–5 January, GWF is  
 399 strongly negative above  $z = 80$  km to the north of  $20^\circ$  N. This forcing probably acts to  
 400 reinforce the DS structure by causing downwelling in the polar MLT. During 2–5 January, the  
 401 zonal mean zonal wind  $[u]$  is westward in the winter polar stratosphere and eastward in the  
 402 mesosphere. According to the Charney and Drazin theorem (1961), the westward wind in the  
 403 stratosphere prevents the upward propagation of PWs from the troposphere. Model results  
 404 show that PWF through the stratosphere and mesosphere is weaker (but negative) after the  
 405 SSW onset, when the zonal wind is westward in the polar stratosphere.



406 **Figure 5.** Same as Fig. 3 but for (a) 2–5, (b) 6–9 and (c) 10–13 January 2019.

407

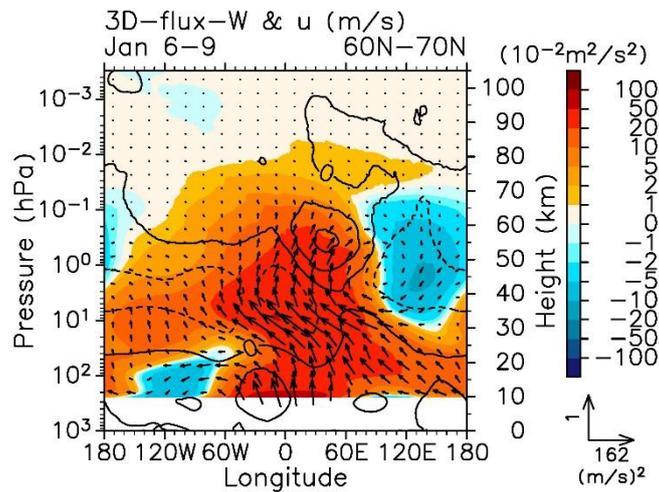
408 During 6–9 January, the prevailing PWF through the entire winter polar middle  
 409 atmosphere is negative with values of about  $-10$  to  $-20$   $\text{m s}^{-1} \text{d}^{-1}$  (Fig. 5b). A westward  
 410 wind is dominant in the polar mesosphere. After the SSW onset, it has descended to the  
 411 stratosphere, and is reformed during 6–9 January. Thus it is implied that the reformation of  
 412 the mesospheric westward wind is caused by this negative PWF. In the  $[P_M]$  cross section,  
 413 there is a peak at  $\sim 60^\circ$  N and  $\theta = 3,000$ – $6,000$  K ( $z = 60$ – $80$  km), below which is a weak  
 414  $[P_M]$  peak at  $\sim 60^\circ$  N in the stratosphere at  $\theta = 500$ – $2,000$  K ( $z = 22$ – $50$  km). The weak peak  
 415 is formed during 25–29 December, just before the onset of the major warming on 1 January  
 416 (not shown). This peak is likely to be caused by negative PWF associated with the SSW.  
 417 During 6–9 January, another weak peak also appears at  $\sim 40^\circ$  N and  $\theta = 4,000$ – $6,000$  K ( $z =$   
 418  $70$ – $80$  km).

419 During 6–9 January, PWs propagate upward into the mesosphere despite the westward  
 420 wind below in the polar stratosphere. According to the Charney and Drazin theorem (1961),  
 421 RWs hardly propagate in a westward wind region. In the meridional cross section of  $[P_M]$  of

422 2–5 January (Fig. 5a), there is a maximum at  $\sim 60^\circ$  N in the stratosphere ( $\theta = 600\text{--}1,100$  K).  
 423 On the poleward side of this maximum, the necessary condition for the BT/BC instability  
 424 (i.e.,  $[P_M]_y < 0$ ) is fulfilled. The region of negative  $[P_M]_y$  is continuously maintained for a  
 425 long time over the periods of 6–9 and 10–13 January (Figs. 8b and 8c) after 2–5 January.  
 426 However, significant positive PWF, which suggests PW generation, is not observed during  
 427 the period of 2–5 January or 6–9 January (Figs. 8a and 8b). Thus, we need a different  
 428 mechanism from generation in the middle atmosphere to explain PWs propagating into the  
 429 upper mesosphere during 6–9 January.

430 We examined the longitudinal characteristics of PW propagation from the upper  
 431 troposphere to the mesosphere during 6–9 January. The longitude-height sections of the 3D-  
 432 flux-W  $\mathbf{F}_{W1}$  from Kinoshita and Sato (2013) averaged over  $60^\circ$  N– $70^\circ$  N for 6–9 January are  
 433 shown in Fig. 6. The vectors represent the zonal and vertical components of the flux, the  
 434 shading represent the vertical components of  $\mathbf{F}_{W1}$  and the contours represent the zonal wind  
 435 averaged over  $60^\circ$  N– $70^\circ$  N at each longitude. To show the vertical structure more clearly,  
 436  $\mathbf{F}_{W1}$  is weighted by  $\rho_0^{-1/2}$ .

437 The upward propagation of waves occurs mainly in the region of  $60^\circ$  W– $60^\circ$  E, where  
 438 the zonal wind has a westward tilting structure at  $z = 20\text{--}55$  km. This westward tilting  
 439 structure is consistent with the structure of upward propagating RWs and similar structure  
 440 was observed during the major SSW in February 2018 (e.g., Harada et al., 2019). Thus, the  
 441 westward winds in this region can be regarded as part of the PWs. It is inferred that waves  
 442 propagate upward in the region of  $60^\circ$  W– $60^\circ$  E, even though the zonal mean zonal wind is  
 443 westward.



444 **Figure 6.** Longitude–height section of the 3D-flux-W  $\mathbf{F}_{w1}$  weighted by  $\rho_0^{1/2}$  (shading and  
 445 vectors) averaged over  $60^\circ$  N– $70^\circ$  N for 6–9 January 2019. Shading indicates the vertical  
 446 component of  $\mathbf{F}_{w1}$ . Solid contours indicate  $u$  averaged over the same region (contour  
 447 interval =  $20 \text{ m s}^{-1}$ ). Dashed contours indicate negative values.

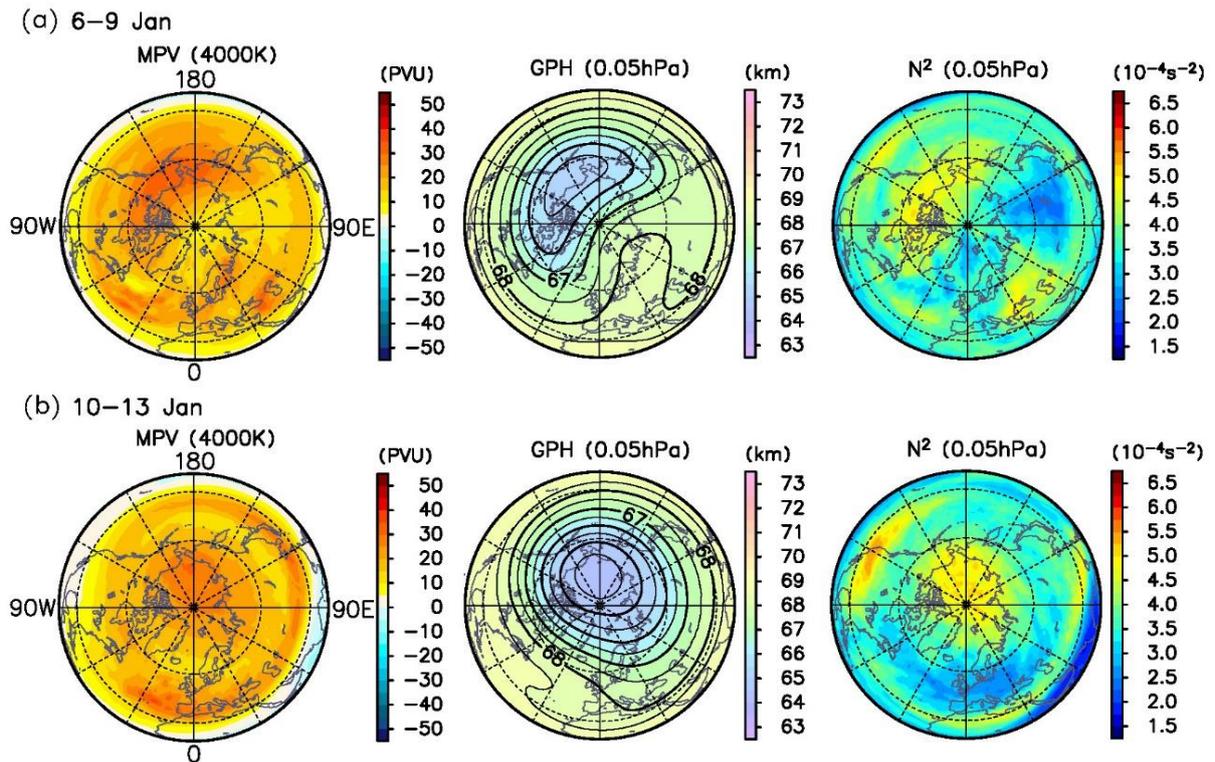
448

449 As seen in Fig. 5c, during 10–13 January, the eastward jet becomes stronger and  
 450 extends to the polar mesosphere. The PWs and GWs provide strong negative forcing at  $z >$   
 451 80 km poleward of  $50^\circ$  N and  $20^\circ$  N, respectively. There is a  $[T]$  maximum corresponding to  
 452 the ES poleward of  $\sim 60^\circ$  N at  $z = \sim 80$  km. Thus, it is considered that both negative PWF and  
 453 GWF are responsible for ES formation by causing downwelling below and poleward of the  
 454 forcing regions.

455 The  $[P_M]$  maximum at  $\sim 40^\circ$  N and  $\theta = 3,500\text{--}6,000$  K ( $z = 65\text{--}80$  km), which is  
 456 already present during 6–9 January, is enhanced in 10–13 January. It is at  $\sim 38^\circ$  N,  $\theta = \sim 4,000$   
 457 K ( $z = \sim 70$  km) and is sandwiched between negative and positive GWFs. The GWFs lead to  
 458 the formation of the  $[P_M]$  peak at  $\sim 38^\circ$  N,  $\theta = \sim 4,000$  K ( $z = \sim 70$  km) via a similar process  
 459 that leads to the formation of the  $[P_M]$  peak at  $\sim 40^\circ$  N,  $\theta = \sim 3,500$  K ( $z = \sim 65$  km) during  
 460 17–20 December. The negative or near zero  $[P_M]_y$ , which is poleward of  $\sim 60^\circ$  N and over  
 461 the wide region of  $\theta = 500\text{--}6,000$  K ( $z = 22\text{--}80$  km) during 6–9 January, has disappeared  
 462 from  $\theta = 1,200\text{--}6,000$  K ( $z = 40\text{--}80$  km) in 10–13 January (Fig. 5c). During 10–13 January,  
 463 PWF is strong and positive poleward of  $60^\circ$  N at  $z = 35\text{--}80$  km. This region of positive PWF  
 464 roughly matches the region where the negative  $[P_M]_y$  in 6–9 January becomes positive in  
 465 10–13 January. These features suggest in-situ PW generation due to the BT/BC instability.

#### 466 3.2.2.2 Horizontal structure

467 To examine the formation of the  $[P_M]$  peak at  $\sim 60^\circ$  N,  $\theta = 3,000\text{--}6,000$  K ( $z = 60\text{--}80$   
 468 km) during 6–9 January in terms of the horizontal structure, orthographic projection maps of  
 469  $P_M$ , GPH and  $N^2$  at  $\theta = \sim 4,000$  K and 0.05 hPa ( $z = \sim 70$  km) for 6–9 and 10–13 January are  
 470 shown in Fig. 7. In contrast to the results from 17–20 and 21–24 December (Fig. 4), high  $P_M$ ,  
 471 low GPH (i.e., the center of the polar vortex) and high  $N^2$  appear roughly in the same  
 472 regions. During 6–9 January, the polar vortex is shifted equatorward at  $\sim 135^\circ$  W. The region  
 473 of low GPH is stretched and distorted into a comma-like shape at  $\sim 60^\circ$  E. This is a typical  
 474 structure for PW breaking. Thus, it is inferred that the mixing caused by PW breaking  
 475 eliminates the  $P_M$  minimum at  $\sim 60^\circ$  E associated with the polar vortex shift, and only the  
 476  $P_M$  maximum at  $\sim 135^\circ$  W remains in the zonal mean field  $[P_M]$ . During 10–13 January, the  
 477 polar vortex and the  $P_M$  maximum approach the pole, corresponding to the elimination of  
 478  $[P_M]_y < 0$  in the zonal mean field (Figs. 5b and 5c). High  $P_M$  is distributed along a strip at  
 479  $\sim 40^\circ$  N, and corresponds to the weak  $[P_M]$  peak at  $\sim 38^\circ$  N,  $\theta = \sim 4,000$  K ( $z = \sim 70$  km)  
 480 between negative and positive GWFs (Figs. 5b and 5c).



481 **Figure 7.** Orthographic projection maps of the Northern Hemisphere showing 4-day mean  
 482 (left to right)  $P_M$ , GPH and  $N^2$  at 0.05 hPa and  $\theta = 4,000$  K ( $z \sim 70$  km) for (a) 6–9 and (b)  
 483 10–13 January 2019.

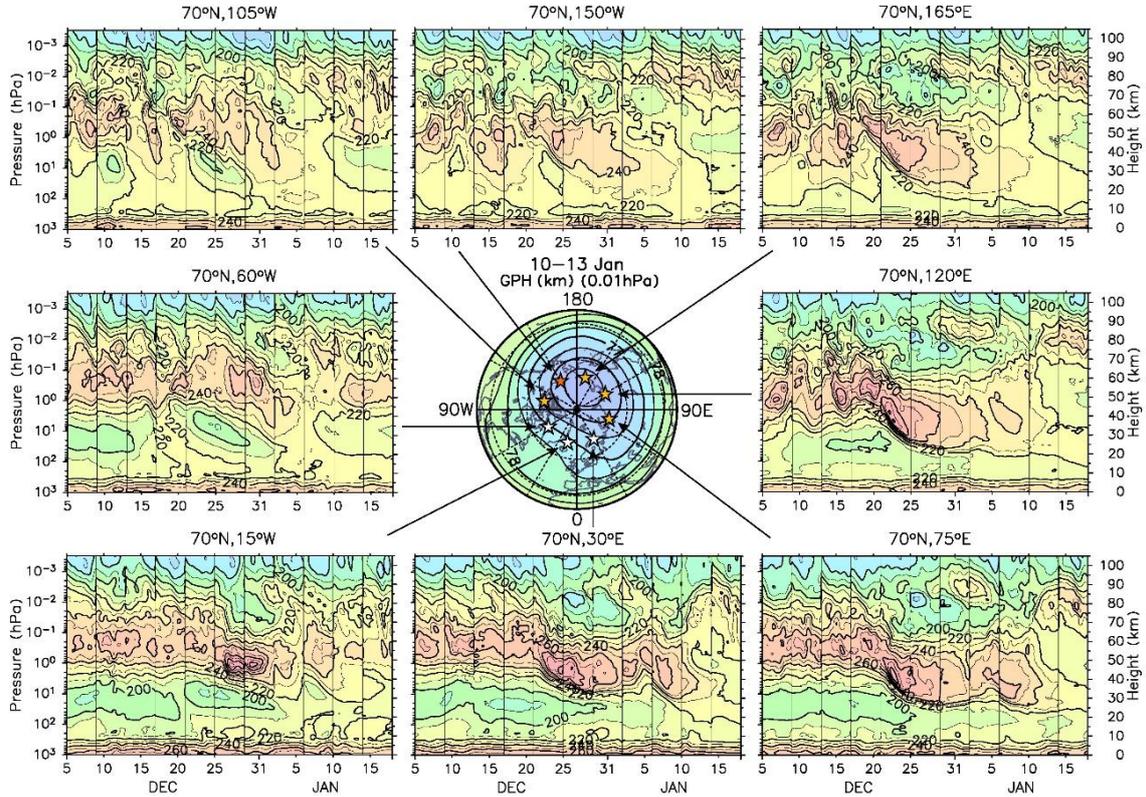
484

485 During 10–13 January when the ES is formed, PWs from the troposphere hardly reach  
 486 the polar MLT because of the prevailing westward wind in the polar stratosphere (Fig. 5c).  
 487 Thus, it is considered that the negative PWF, which is responsible for ES formation together  
 488 with the negative GWF, is caused by the breaking of PWs that are generated in the  
 489 mesosphere (via the process discussed above) propagating into the MLT. The recovered  
 490 mesospheric eastward jet provides an environment in which these in-situ generated PWs can  
 491 propagate vertically. The recovered eastward jet also affects GW propagation through its  
 492 filtering effect.

### 493 3.2.2.3 Zonal asymmetry of the ES

494 As shown in previous studies (e.g., France and Harvey, 2013), the ES has zonal  
 495 asymmetry especially after displacement-type SSWs such as the 2018/19 event. Figure 8  
 496 shows the GPH map at 0.01 hPa ( $z \sim 80$  km) during 10–13 January and the time–height  
 497 sections of the temperature at  $70^\circ$  N latitude and longitudes of  $30^\circ$  E,  $75^\circ$  E,  $120^\circ$  E,  $165^\circ$  E,  
 498  $150^\circ$  W,  $105^\circ$  W,  $60^\circ$  W and  $15^\circ$  W. The ES, i.e., a temperature maximum at  $z \sim 80$  km that  
 499 appears around 10 January, is present at  $75^\circ$  E,  $120^\circ$  E,  $165^\circ$  E,  $150^\circ$  W and  $105^\circ$  W (as  
 500 denoted by yellow and orange stars in the GPH map). However, its presence at  $60^\circ$  W,  $15^\circ$  W

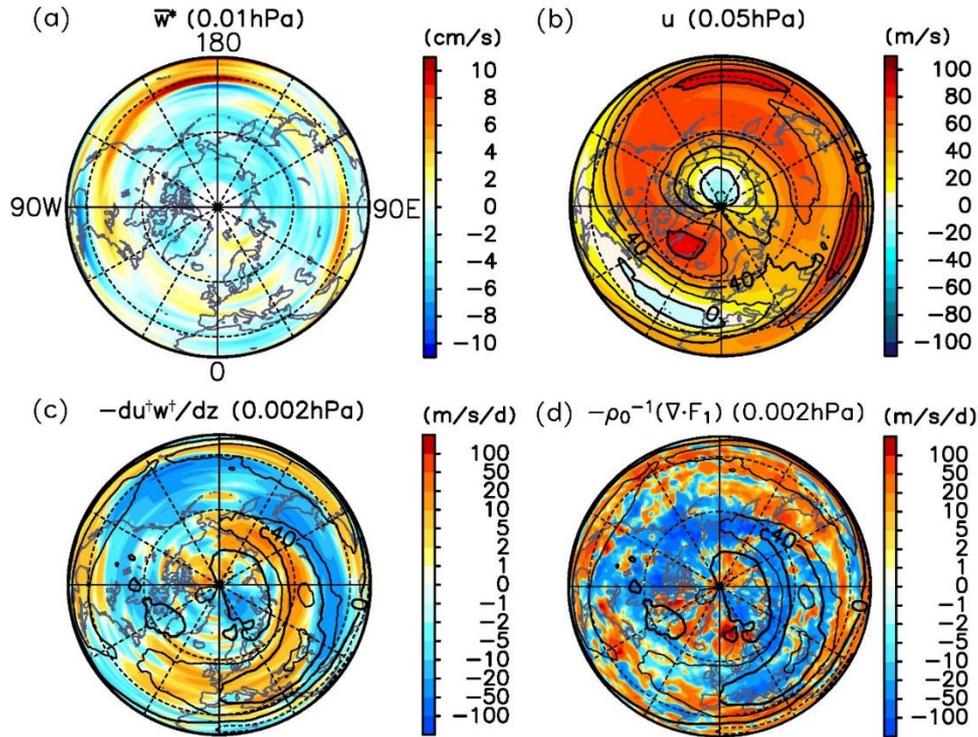
501 and 30° E is unclear (open stars). The clearest and strongest ES structure appears at 70° N,  
 502 150° W (an orange star). The sites where the ES is observed are located inside of the polar  
 503 vortex. Thus, it is indicated that the ES is not an apparent phenomenon that is only seen in the  
 504 zonal mean field associated with a shift of the polar vortex, but is a real warming of the  
 505 atmosphere inside of the polar vortex.  
 506



507 **Figure 8.** An orthographic projection map of the Northern Hemisphere showing 4-day mean  
 508 GPH (unit: km) at 0.01 hPa for 10–13 January 2019 and time–height sections of  $T$  (unit: K)  
 509 smoothed with a lowpass filter with a cutoff of one day at a latitude of 70° N and longitudes  
 510 of 30° E, 75° E, 120° E, 165° E, 150° W, 105° W, 60° W and 15° W. Star symbols in the  
 511 GPH map denote the locations for the  $T$  figures. Vertical lines in the  $T$  figures represent the  
 512 boundaries of the model runs.

513

514 Figure 9 shows the maps of  $\bar{w}^*$  at 0.01 hPa ( $z \sim 80$  km),  $u$  at 0.05 hPa ( $z \sim 70$   
 515 km), and  $-du^\dagger w^\dagger/dz$  due to GWs and  $-\rho_0^{-1}(\nabla \cdot \mathbf{F}_1)$  due to PWs at 0.002 hPa ( $z \sim 92$   
 516 km), which correspond to GWF and PWF, respectively. Downward flow at 70° N latitude is  
 517 weak in the region of 30° W–0°–60° E and strong in the region of 90°E–180°–135°W (Fig.  
 518 9a). The GWF is negative at 30° N–60° N, 120° E–180°–60° W (Fig. 9c), and positive inside  
 519 of the eastward jet streak extending from 45° N, 30° W to 70° N, 180°. The PWF at 50° N–  
 520 80° N, 30° E–180°–90° W is strongly negative, with values below  $-100 \text{ m s}^{-1} \text{ d}^{-1}$  (Fig. 9d).  
 521 At 90° W–0°–30° E, PWF is positive poleward of 60° N.



522 **Figure 9.** Orthographic projection maps of the Northern Hemisphere showing 4-day mean (a)  
 523  $\bar{w}^*$  at 0.01 hPa, (b)  $u$  at 0.05 hPa, (c)  $-du^+w^+/dz$  due to GWs at 0.002 hPa and (d)  
 524  $-\rho_0^{-1}(\nabla \cdot \mathbf{F}_1)$  due to PWs at 0.002 hPa for 10–13 January 2019. Note that  $\bar{w}^*$  and  
 525  $-du^+w^+/dz$  are zonally smoothed with a lowpass filter with a cutoff of  $s=6$ .

526

527 Equatorward of the region at around  $70^\circ$  N,  $150^\circ$  W, where the ES is clear and strong,  
 528 both GWF and PWF are negative. In contrast, at  $60^\circ$  W– $30^\circ$  E, where the ES is very weak or  
 529 absent, GWF and PWF are positive equatorward and poleward of  $\sim 60^\circ$  N, respectively. The  
 530 net forcing of these two waves is positive in this region. Negative (positive) net wave forcing  
 531 induces downward (upward) flow poleward. Thus, it is inferred that the asymmetric ES is  
 532 caused by vertical flow induced by the zonally asymmetric wave forcing.

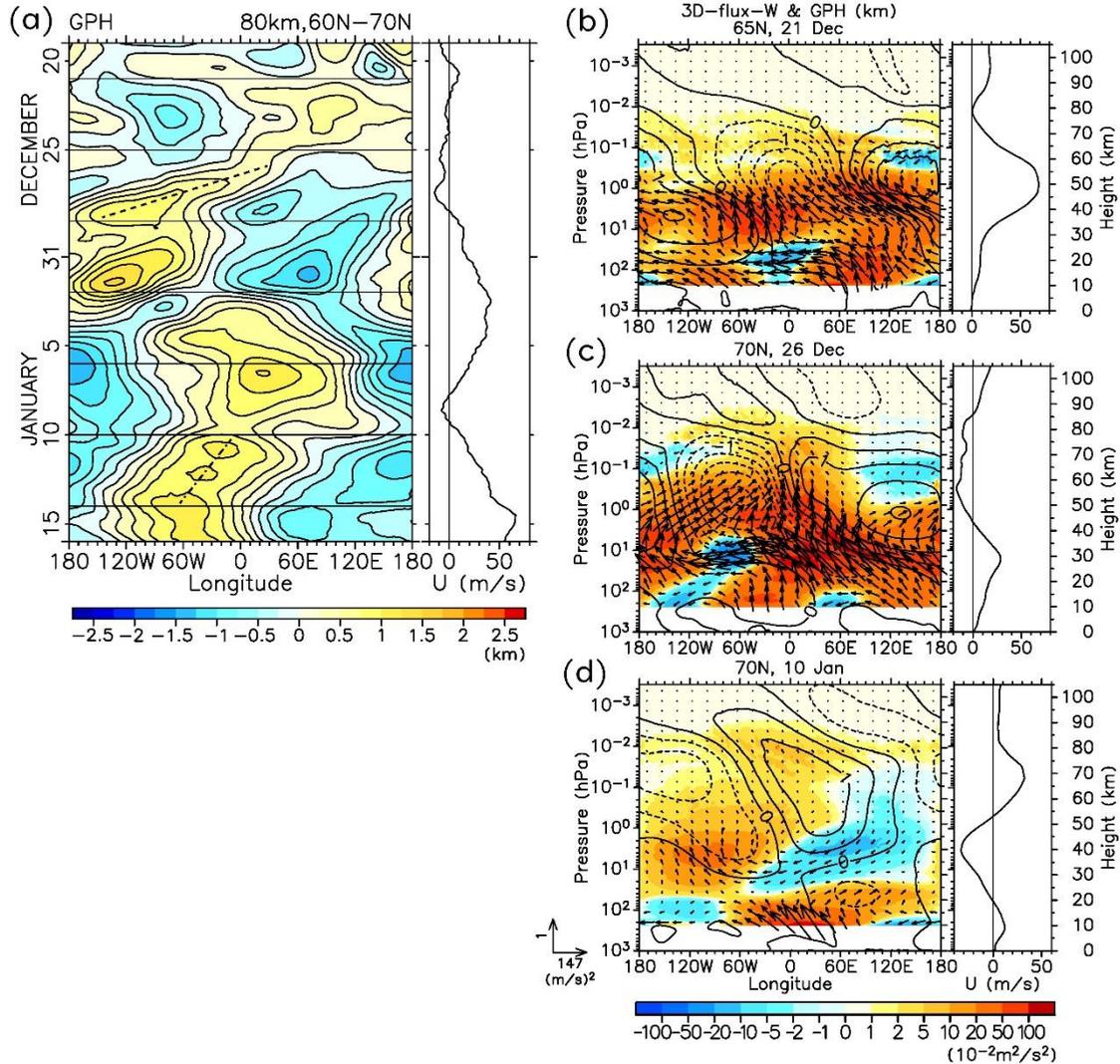
533 Why are GWF and PWF positive at  $60^\circ$  W– $30^\circ$  E? At 0.05 hPa ( $z \sim 70$  km), where  
 534 the eastward jet is recovered in the polar mesosphere (see Fig. 5c), eastward wind is  
 535 particularly strong poleward of  $50^\circ$  N (Fig. 9b). Equatorward of this eastward wind, a weak  
 536 westward wind appears. This recovered mesospheric eastward jet provides suitable  
 537 conditions for upward propagation of PWs and westward GWs. However, it is implied that  
 538 PWs are refracted and are unable to propagate upward at  $>60^\circ$  N,  $60^\circ$  W– $30^\circ$  E because  
 539 eastward winds are too strong in this region. In addition, the westward wind at  $<60^\circ$  N,  $60^\circ$   
 540 W– $30^\circ$  E prevents upward propagation of PWs as well as westward GWs through its filtering  
 541 effect. Thus, it is inferred that this  $u$  structure prevents the appearance of negative GWF and  
 542 PWF in the MLT above.

## 543 3.3 Characteristics of PWs generated in the middle atmosphere

544 To examine the characteristics of PWs that are generated in the middle atmosphere via  
 545 the processes described in section 3.2, the longitude–time section of GPH deviation from  
 546 zonal mean at  $60^\circ\text{N}$ – $70^\circ\text{N}$ ,  $z = 80\text{ km}$  is shown in Fig. 10a. During 21–24 December, PWF  
 547 is positive north of  $\sim 40^\circ\text{N}$  at  $z = 60$ – $80\text{ km}$  (Fig. 3b) and stationary PWs with  $s = 1$  are  
 548 dominant. During 25–28 December, PWF is positive poleward of  $55^\circ\text{N}$  at  $z = 67$ – $82\text{ km}$ , the  
 549 DS is formed (Fig. 3c) and westward propagating PWs have periods of  $\sim 6$  days (indicated by  
 550 the dashed line in Fig. 10a) and  $s = 1$ – $2$ . During 10–13 January, when the ES is formed, PWs  
 551 have periods of  $\sim 24$  days (the dash-dotted line) and  $s = 1$ .

552 Figures 10b, 10c and 10d show the longitude–height sections of GPH deviation and  
 553 the 3D-flux- $\mathbf{F}_{W1}$  on 21, 26 December and 10 January, respectively. On 21 December, the  
 554 westward tilting structure of GPH and upward propagation indicated by  $\mathbf{F}_{W1}$  associated with  
 555 waves from the troposphere are attenuated at  $z = \sim 55\text{ km}$  (Fig. 10b). This is because the wave  
 556 packet from the lower atmosphere propagates equatorward below this level (see Fig. 3b). The  
 557 westward tilting structure of GPH and positive vertical component of  $\mathbf{F}_{W1}$  are also present  
 558 above  $z = \sim 65\text{ km}$ ; as discussed in section 3.2, these features are associated with PWs that are  
 559 generated by the BT/BC instability in the middle atmosphere.

560 On 26 December (Fig. 10c) and 10 January (Fig. 10d), layers with  $[u] < 0\text{ m s}^{-1}$  are  
 561 observed at  $z = 43$ – $85\text{ km}$  and  $20$ – $53\text{ km}$ , respectively. In these layers, upward wave  
 562 propagation is markedly attenuated. The features suggesting upward wave propagation (i.e.,  
 563 westward tilting structure of GPH and a positive vertical component of  $\mathbf{F}_{W1}$ ) are present at  
 564 higher altitudes. For both 26 December and 10 January, PWs having  $s = 1$  are dominant in  
 565 the regions of upward wave propagation.



566

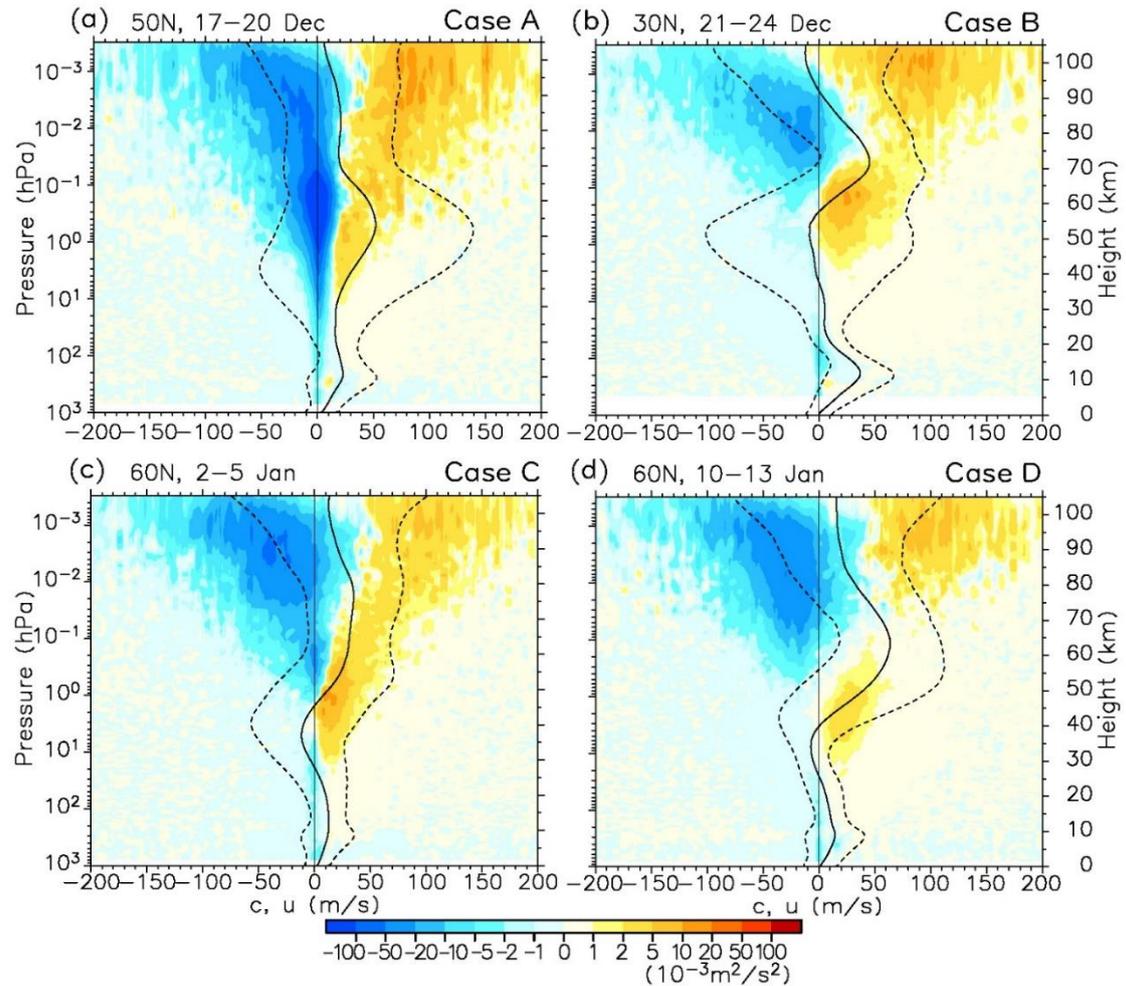
567 **Figure 10.** (a) Left panel: longitude–time section at 60° N–70° N,  $z = 80$  km. Thin horizontal  
 568 lines represent the boundaries of the model runs. A dashed line and a dash-dotted line denote  
 569 propagations with periods of 6 days and 24 days, respectively; (b–d) left panel: latitude–  
 570 height sections of geopotential height deviation from zonal mean (contours), vertical  
 571 component of 3D-flux- $\mathbf{F}_{w1}$  weighted by  $\rho_0^{1/2}$  (shading) and the vertical and zonal  
 572 components of 3D-flux- $\mathbf{F}_{w1}$  weighted by  $\rho_0^{1/2}$  (vectors) at (b) 65° N on 21 December  
 573 2018, (c) 70° N on 26 December 2018, and (d) 70° N on 10 January 2019; (a–d) right panels:  
 574 variations with height of  $[u]$  averaged over the same latitudinal region and time periods as  
 575 the figures on the left.

## 576 3.4 Propagation of GWs

577 The GWs which play crucial roles in the formation of the ES and DS is further  
 578 analyzed. Figure 11 shows the vertical flux of zonal momentum  $[u^\dagger w^\dagger]$  of GWs as a  
 579 function of the ground-based phase velocity  $c$  at each height. The solid and dashed curves  
 580 denote the mean  $[u]$  and  $[u] \pm 1.65\sigma$  over a  $20^\circ$  latitude range centered around  $50^\circ$  N (Fig.  
 581 11a),  $30^\circ$  N (Fig. 11b),  $60^\circ$  N (Fig. 11c), and  $60^\circ$  N (Fig. 11d). Assuming normal distribution  
 582 for  $[u]$ , the area between each pair of dashed curves encompasses 90% of the values of  $[u]$ .  
 583 Figures 11a, 11b, 11c and 11d are the profiles for GWs at  $50^\circ$  N for 17–20 December (Case  
 584 A),  $30^\circ$  N for 21–24 December (Case B),  $60^\circ$  N for 2–5 January (Case C) and  $60^\circ$  N for 10–  
 585 13 January (Case D), respectively. As discussed in section 3.2, it is likely that in Cases A and  
 586 B, GWs are responsible for the  $[P_M]$  peaks that appear before the formation of the DS. The  
 587 GW momentum flux in Case C is likely related to the reinforcement of the DS structure after  
 588 SSW onset. In case D, GWs exert strong negative forcing in the MLT during the formation  
 589 phase of the ES.

590 The vertical flux of zonal momentum  $[u^\dagger w^\dagger]$  for Case A (Fig. 11a) is strongly  
 591 negative around  $c = \sim 0 \text{ m s}^{-1}$  at all altitudes. At its strongest, its absolute value exceeds  $\sim 0.1$   
 592  $\text{m}^2 \text{ s}^{-2}$ . In Cases B, C and D, the negative  $[u^\dagger w^\dagger]$  peaks around  $c = \sim 0 \text{ m s}^{-1}$  in the  
 593 troposphere and the lower stratosphere are absent in the upper stratosphere. This is likely  
 594 because of weak wind layers in the lower or middle stratosphere.

595 In Case B, there is a weak wind layer with  $[u] = \pm 10 \text{ m s}^{-1}$  at  $z = 20\text{--}55 \text{ km}$ ; in  
 596 addition to the small  $[u]$ , the variation of  $[u]$ , as indicated by the area between the two  
 597 dashed lines is also small at  $z = 20\text{--}30 \text{ km}$ . In Cases C and D, the weak wind layers of  $[u] =$   
 598  $\pm 10 \text{ m s}^{-1}$  are at  $z = 25\text{--}50 \text{ km}$  and  $z = 20\text{--}45 \text{ km}$ , respectively. Because the meridional wind  
 599 is generally weaker than  $[u]$  and the meridional component of the ground-based phase  
 600 velocity of a GW is smaller than the zonal component in most cases, GWs having  $c = \sim 0 \text{ m}$   
 601  $\text{s}^{-1}$  such as orographic waves break down at a critical layer, a layer with  $[u] = \sim 0 \text{ m s}^{-1}$ .  
 602 However,  $[u^\dagger w^\dagger]$  of GWs having  $c = \sim 0 \text{ m s}^{-1}$  above these layers are strongly negative at  
 603  $z = 65\text{--}100 \text{ km}$  in Case B,  $z > 47 \text{ km}$  in Case C and  $z > 55 \text{ km}$  in Case D. The lowest values  
 604 of  $[u^\dagger w^\dagger]$  are  $\sim -1 \times 10^{-2} \text{ m}^2 \text{ s}^{-2}$  at  $z = 70\text{--}90 \text{ km}$  in Case B,  $\sim -1 \times 10^{-2} \text{ m}^2 \text{ s}^{-2}$  at  $z = 75\text{--}95$   
 605  $\text{km}$  in Case C and  $\sim -1 \times 10^{-2} \text{ m}^2 \text{ s}^{-2}$  at  $z = 75\text{--}95 \text{ km}$  in Case D. These negative momentum  
 606 fluxes of GWs having  $c = \sim 0 \text{ m s}^{-1}$  cannot be explained only by pure vertical propagation  
 607 from the lower atmosphere, which is the assumption that is made in most GW  
 608 parameterizations. This result indicates that these waves propagate from other latitudes and/or  
 609 are excited in the middle atmosphere.



610 **Figure 11.** Vertical profiles of  $[u^\dagger w^\dagger]$  of GWs as a function of the ground-based zonal phase  
 611 velocity at each height (shading) at (a)  $50^\circ \text{N}$  for 17–20 December 2018 (Case A), (b)  $30^\circ \text{N}$   
 612 for 21–24 December 2018 (Case B), (c)  $60^\circ \text{N}$  for 2–5 January 2019 (Case C), and (d)  $60^\circ \text{N}$   
 613 for 10–13 January 2019 (Case D). The values  $[u^\dagger w^\dagger]$  are smoothed by the 3-point moving  
 614 average in the phase velocity direction. Solid curves denote the mean  $[u]$  over a  $20^\circ$  latitude  
 615 range centered around (a)  $50^\circ \text{N}$ , (b)  $30^\circ \text{N}$ , (c)  $60^\circ \text{N}$ , and (d)  $60^\circ \text{N}$ . Dashed curves on either  
 616 side of the solid curve denote  $[u] \pm 1.65\sigma$ , where  $\sigma$  is the standard deviation. Assuming  
 617 normal distribution for  $[u]$ , the area between each pair of dashed curves encompasses 90%  
 618 of the values of  $[u]$ .

619

#### 620 **4 Summary and Conclusions**

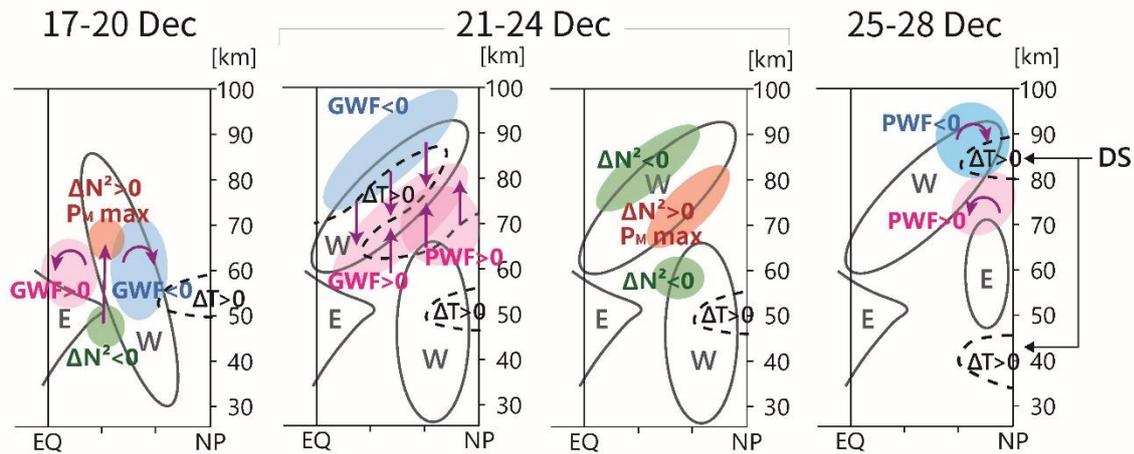
621 To clarify the middle atmosphere dynamics in a significant SSW ES event in 2018/19,  
 622 we performed a hindcast using a GW-permitting model that covers the ground surface to the  
 623 lower thermosphere. Detailed analysis of the output data indicates crucial importance of the  
 624 interplay between PWs and GWs.

625 We have first reported a double stratopause (DS) structure: A temperature maximum  
626 was located at a height of  $z \sim 85$  km in the polar region before the disappearance of the  
627 lowered stratopause associated with an SSW (Figs. 1a and 1b). Thus, there are two  
628 temperature maxima in the vertical profile during the time period.

629 To examine the mechanism of the formation of the DS, a schematic of the mechanism  
630 is shown in Fig. 12. Prior to DS formation, during 17–20 December, GWF above the  
631 eastward polar night jet was strongly negative at  $\sim 50^\circ$  N,  $z \sim 65$  km (Fig. 3a); GWF was  
632 positive above the westward wind at  $< 35^\circ$  N and  $z \sim 65$  km, equatorward of the negative  
633 GWF. Because of the residual mean upward flow induced below, the residual mean vertical  
634 flow converged in the region between the negative and positive GWFs (Fig. 4a). A peak of  
635  $P_M$  appeared as a result of  $N^2$  increase in this region of convergence, which was located at  
636  $\sim 40^\circ$  N,  $\theta \sim 3,500$  K ( $z \sim 65$  km).

637 During 21–24 December, PWF was positive poleward of the  $[P_M]$  peak that was  
638 present in 17–20 December (Fig. 3b). This feature suggests the in-situ generation of PWs due  
639 to the BT/BC instability. During this period, negative (positive) GWF appeared above  
640 (below) the eastward jet with its axis at  $\sim 25^\circ$  N and  $z \sim 72$  km in the mesosphere. This  
641 GWF distribution can be explained by a filtering effect by the mesospheric eastward jet. This  
642 jet tilted from the equatorial region in the lower mesosphere to the winter polar region in the  
643 upper mesosphere. A weak temperature maximum extending toward higher altitudes and  
644 latitudes was formed at the height of residual mean downwelling, which was located between  
645 the negative and positive GWFs in the mesosphere. There was also a residual mean upward  
646 flow poleward of the positive GWF. Then, a  $[P_M]$  peak caused by high  $N^2$  appeared in the  
647 region where the vertical flow converged (Fig. 4b). Poleward of this peak,  $[P_M]_y$  was  
648 negative, which satisfied the necessary condition of the BT/BC instability.

649 During 25–28 December, PWF was positive where  $[P_M]_y < 0$  in 21–24 December  
650 (Fig. 3c). It is also likely that PWs were generated due to the BT/BC instability induced by  
651 the GWFs in the mesosphere. In addition, PWF in the MLT was strongly negative. This  
652 negative PWF was probably a result of the PWs generated in the mesosphere because the  
653 prevailing wind was westward in the stratosphere during the major SSW, and PWs excited in  
654 the troposphere hardly propagate through into the MLT. It is inferred that a downward flow  
655 induced by the negative PWF in the polar MLT caused the upper maximum of the DS at  $z \sim$   
656  $\sim 85$  km.

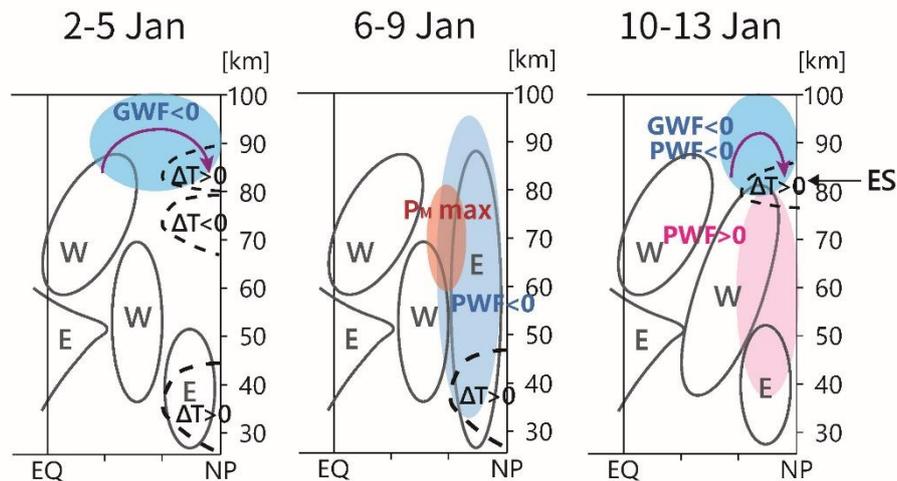


657 **Figure 12.** A schematic of the formation mechanism of the DS in the latitude–height section;  
 658 W and E denote westerly (eastward) and easterly (westward) winds;  $\Delta$  represents the  
 659 anomaly of each value; purple vectors indicate the residual mean flows.

660

661 To examine the mechanism of the formation of the ES, a schematic of the mechanism  
 662 is shown in Fig. 13. During 2–5 January, after the onset of major warming on 1 January, the  
 663 DS structure was reinforced by the negative GWF in the polar MLT (Figs. 2d and 5a). Then,  
 664 PWF was negative throughout the entire polar middle atmosphere during 6–9 January (Figs.  
 665 2b and 5b). As a result, the westward wind in the polar mesosphere, which had disappeared in  
 666 2–5 January, was reformed at  $z < 90$  km in 6–9 January. Then, a  $[P_M]$  maximum appeared at  
 667  $\sim 60^\circ$  N and  $\theta = 3,000\text{--}6,000$  K ( $z = 60\text{--}80$  km) (Fig. 5b). The orthographic projection map of  
 668  $\theta = 4,000$  K ( $z = \sim 70$  km) shows high  $P_M$  inside of a comma-like polar vortex, which is a  
 669 typical feature of PW breaking (Fig. 7a).

670 During 10–13 January, PWF was positive poleward of  $60^\circ$  N at  $z = 35\text{--}80$  km (Fig.  
 671 5c), in a region that roughly matches the region of  $[P_M]_y < 0$  in 6–9 January. These features  
 672 suggest that PWs were generated in-situ by the BT/BC instability. During 10–13 January,  
 673 GWF and PWF were negative at  $z > 80$  km above the recovered eastward jet in the polar  
 674 mesosphere (Fig. 5c, also Figs. 2b and 2d). These wave forcings were comparable in strength  
 675 and had values of  $-20$  to  $-50$   $\text{m s}^{-1} \text{d}^{-1}$  in the polar MLT. The ES was formed at  $z = \sim 80$   
 676 km around 11 January (Fig. 5c, also Figs. 1a and 1b). The PWF appeared above the  
 677 prevailing westward wind in the stratosphere. Thus, this forcing may be from PWs generated  
 678 at  $> 60^\circ$  N,  $z = 35\text{--}80$  km on 10 January. These results indicate that both GWF and PWF  
 679 played significant roles in the formation of the ES. Observed longitudinal structure of the  
 680 polar temperature suggests that the zonally asymmetric ES was a warming inside of the polar  
 681 vortex (Fig. 8). The structure of the ES was likely to be determined by the zonally  
 682 asymmetric GWF and PWF (Fig. 9).



683 **Figure 13.** A schematic of the formation mechanism of the ES in the latitude–height section.  
 684 Symbols are the same as those in Fig. 12.

685

686 Our results also suggest that the DS structure may have affected the process of ES  
 687 formation. The reformation of the mesospheric westward wind during 6–9 January prevented  
 688 upward PW propagation. Without adiabatic heating associated with wave forcing, the  
 689 latitudinal gradient of zonal mean temperature  $[T]_y$  tends to decline gradually because of  
 690 radiative relaxation in the polar night region. The height dependency of  $[T]_y$  may be  
 691 affected by the temperature structure as a result of the DS, as shown in Fig. 13 for the first  
 692 period of 2–5 January. The DS structure had a  $[T]$  minimum at  $z=65\text{--}77$  km and a  
 693 maximum at  $z=80\text{--}90$  km. At the altitudes where the  $[T]$  minimum was present,  $[T]_y$   
 694 became strongly negative. The altitude of the recovered eastward jet was determined by  $[T]_y$   
 695 via the thermal wind balance. Thus, the height of the eastward jet was probably modified by  
 696 the DS structure. The eastward jet affected the propagation of GWs and PWs and their  
 697 forcings in the polar MLT, leading to the formation of the ES. In this way, it is likely that the  
 698 height of the ES was affected by the DS structure.

699 From the relationship between phase velocity spectra of GW momentum fluxes and  
 700 the vertical profile of zonal-mean zonal wind, it is shown that vertical propagation from the  
 701 lower atmosphere alone is insufficient to explain the presence of the GWs, which play  
 702 important roles in the formation of the DS and ES (Fig. 11). It is suggested that a part of these  
 703 GWs propagated laterally and/or were generated in the middle atmosphere. This result  
 704 indicates that the assumptions generally underlying GW parameterizations are not necessarily  
 705 appropriate for representing GWs in the MLT.

706 Results from the high-resolution JAGUAR are generally consistent with  
 707 observations and enable quantitative analysis of the middle atmosphere dynamics including  
 708 GWs. Although this study focused on the dynamics in the Northern Hemisphere, JAGUAR

709 provides promising data that can be used to examine the mechanisms of various dynamical  
710 phenomena observed in the entire middle atmosphere, such as interhemispheric coupling  
711 (e.g., Körnich and Becker, 2010).

712

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721 [tokyo.ac.jp/en/archive\\_data/Okui\\_etal\\_2021/](http://pansy.eps.s.u-tokyo.ac.jp/en/archive_data/Okui_etal_2021/). The Aura MLS observation data can be  
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726

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