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2 Regional character of geomagnetic field directional circularity:  
3 Holocene Eastern North America  
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8  
9 Abstract  
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11 This study summarizes paleomagnetic secular variation (PSV) in five  
12 published Holocene records from Eastern North America. We have developed 100-  
13 year increment time series for the declinations and inclinations for all sites and  
14 compared their directional variability. We see evidence of ten correlatable features  
15 in both inclination and declination. We focus on the clockwise or counter-clockwise  
16 motion of paleomagnetic directions (termed circularity) in these PSV records. We  
17 have first calculated the incremental rate and direction of motion (clockwise or  
18 counter-clockwise) for each record over the last 4000-8000 years. We have  
19 separately looked for discernable looping in individual records. We estimate the  
20 loop sizes, durations, and circularity direction. We see the same pattern of  
21 circularity in both measurement techniques. There are seven intervals of oscillating  
22 circularity and looping in all five sites. Both techniques suggest a distinctive  
23 oscillating, teeter-totter like, behavior to PSV circularity that must be due to the  
24 pattern of fluid flow in the outer core. This teeter-totter behavior is unbalanced with  
25 more time spent in clockwise motion than in counter-clockwise motion. We think  
26 the teeter-totter oscillation may be due to torsional oscillation in the outer core fluid  
27 flow. The loops have a distribution of sizes and durations with smaller loops being  
28 shorter in duration and bigger loops having longer durations. All five PSV records  
29 show 5 intervals of  $\sim 10^2$  yr significant acceleration in circularity rate and PSV rate  
30 combined with change in circularity direction. These features are broadly analogous  
31 to historic geomagnetic jerks.  
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33  
34 Introduction  
35

36 The geomagnetic field that we measure (poloidal field) is largely generated in  
37 the Earth's liquid outer core by dynamo activity (flux regeneration). (See Merrill et  
38 al. (1998) for overview.) One goal in studying the geomagnetic field is to understand  
39 the space/time pattern of geomagnetic field variability (secular variation) and infer  
40 from that the pattern of fluid dynamo activity in the outer core that  
41 maintains/regenerates the field. Flux regeneration is associated with the turbulent  
42 flow of liquid iron in the outer core that twists magnetic field lines and generates  
43 new flux in the process.

44 Historical secular variation (HSV) of the geomagnetic field measured at a  
45 single location was first identified by Gellibrand in 1634 (Merrill et al., 1998).  
46 Halley in 1692 (Merrill, et al., 1998) noted that mapped geomagnetic field directions

47 tended to drift westward over time. Runcorn (1959) associated secular variation  
48 with movements of magnetic sources in the Earth's outer core and suggested that  
49 clockwise (counter-clockwise) motion of directions at a single locality over time  
50 (herein termed circularity) could be due to westward (eastward) motion of the  
51 magnetic sources in the outer core. Skiles (1970) developed this idea further and  
52 noted some degree of ambiguity in relating clockwise versus counter-clockwise  
53 motion of directions with westward versus eastward drift. There is now very clear  
54 evidence for both clockwise and counter-clockwise motion of directions within  
55 different regions of the Earth for both HSV (e.g., Thompson and Barraclough, 1982;  
56 Gubbins and Bloxham, 1987) and paleomagnetic field secular variation (PSV) (e.g.,  
57 Lund and Banerjee, 1985; Smith and Creer, 1986; Itota et al., 1997).

58 This study is the second in a series (Lund, 2020) to evaluate the Holocene  
59 (millennial-scale) character of directional PSV (circularity) in a region, in this case  
60 Eastern North America (Figure 1), using two different techniques to quantify the  
61 directional circularity pattern. The goal is to determine if more specific information  
62 about fluid flow in the outer core can be estimated by more carefully assessing the  
63 pattern of PSV circularity on a regional scale.

## 64 65 66 The Character of Circularity 67

68 Geomagnetic field directional secular variation at a locality that is high-  
69 resolution (good serial correlation of successive data points) can be plotted through  
70 time in inclination (I)/declination (D) space (traditionally referred to as a Bauer plot  
71 (Bauer, 1895)). Most of the time the directional variability displays open loops,  
72 either clockwise or anti-clockwise (e.g., Runcorn, 1959; Kawai et al., 1965). The loop  
73 durations run from a few hundred years to more than one thousand years, often  
74 with short loops superposed on longer loops (e.g., Lund and Banerjee, 1985). On  
75 occasion, I and D track together to create a linear trend (e.g., Doell and Cox, 1965;  
76 Turner et al., 1982; Evans, 1984). Loops can occur as a result of large dipole  
77 variations; in such a case, the looping pattern should be temporally coherent over  
78 much of the Earth (Kawai et al. 1965). However, studies of HSV or longer-term  
79 (Holocene) PSV looping tend to indicate that looping varies coherently over limited  
80 spatial domains up to ~4000 km; beyond that spatial domain, the looping ordinarily  
81 changes style (Thompson and Barraclough, 1982; Bloxham et al., 1989).

82 Open looping could be due to motion of small field sources near the  
83 core/mantle boundary in the outer core located under a locality. Two models of  
84 such localized field are radial dipoles (Alldredge and Hurwitz, 1964) or dynamo  
85 waves (Olson and Hagee, 1987; Hagee and Olson, 1989). Clockwise looping was  
86 generally associated with westward motion of small dipole sources, while  
87 counterclockwise looping was associated with eastward motion (Runcorn, 1959;  
88 Skiles, 1970). These ideas were non-unique however (Dodson, 1979), and poleward  
89 propagation of dynamo waves could produce the same clockwise or  
90 counterclockwise looping (Olson and Hagee, 1987; Hagee and Olson, 1989). More  
91 recent analyses of millennial-scale PSV suggest a variety of other ways that

92 observed circularity might occur (e.g., Dumberry and Bloxham, 2006; Constable,  
93 2011; Korte et al., 2011; Davies and Constable, 2018).

94 Models of secular variation that produce open looping are associated with an  
95 out-of-phase relationship between I and D. This distinctive directional waveform  
96 pattern is common in both HSV and PSV. On occasion, evidence has been noted for  
97 more complicated, longer-term directional waveforms (e.g., Lund et al., 1988;  
98 Negrini et al., 1994). But, this paper only considers the simplest pattern. The size of  
99 the open loops depends on the amplitude of I and D cycles; the duration depends on  
100 the time interval of each I/D cycle.

101 Looping can be considered an indicator of dynamo turbulence directly below  
102 the PSV record locality. The fact that the pattern of looping varies over the Earth  
103 suggests that dynamo turbulence has a regional character. One question is whether  
104 adjacent regions share any degree of correlation. The focus of this paper is to more  
105 carefully assess the actual pattern of circularity and its range of complexity as a  
106 starting point for later assessing its relationship to potential patterns of dynamo  
107 activity.

#### 108 109 110 Regional Pattern of PSV Circularity

111  
112 There are five sites in Eastern North America that have high-resolution, well-  
113 dated PSV records for the last 4,000-8,000 years (Figure 1; Table 1; Appendix 1).  
114 The studies come from three lake sediment studies (Sandy Lake PA (SAN), Lake  
115 LeBeouf PA (LEB), and Seneca Lake NY (SEN)), and two deep-sea sediment studies  
116 (Core 2220 and the East Canada Stack (ECS)). All of these sites have records of both  
117 inclination and declination variability. All of them have high-resolution dating that  
118 provides a chronostratigraphic framework for their comparison (Table 1). The main  
119 goal of this paper is to determine the pattern of PSV variability through time within  
120 a region where the PSV records should have strong similarity. Several of these  
121 records have been previously analyzed by Lund (1996) and Lund et al. (2021). The  
122 key features of the PSV records described below are 1) that they all have age dating  
123 with resolution to  $\sim\pm 100$  years or so, and 2) that the PSV data have strong serial  
124 correlation such that clear correlatable inclination and declination features based on  
125 multiple measurements can be discerned and correlated with the other records.  
126 Below is a summary of the paleomagnetic data and chronostratigraphy for each site.

127 Sandy Lake PA (SAN) was studied by King (1983). The lake has a 6000-yr  
128 PSV record that was dated by 8 radiocarbon dates. Lake LeBeouf PA (LEB) and  
129 Seneca Lake NY (SEN) were studied by King (1983) and King et al. (1983). LEB has a  
130 4000-yr PSV record dated by 6 radiocarbon dates. SEN has an 8000-yr PSV record  
131 that is dated by 4 radiocarbon dates. All three of these PSV records were compared  
132 with other North American PSV records by Lund (1996). Lund (1996) also provided  
133 a correction to the radiocarbon dating so the records use here are in absolute years  
134 AD/BC. Core 2220 from the St. Lawrence Estuary was studied by St. Onge et al.  
135 (2003). The core was dated by 6 calibrated radiocarbon dates. A stack for eastern  
136 Canada Holocene PSV records (ECS) was developed by Barletta et al. (2010). The  
137 stack includes core 2220 and five other PSV records from the same St. Lawrence

138 Estuary region. Barletta et al. (2010) developed a calibrated age model for all these  
139 records based on 30 radiocarbon dates.

140 An estimate of sample error for the sediment records has been determined  
141 by calculating the mean and standard deviation (1 sigma) for stratigraphic intervals  
142 of 3 successive sample measurements. The hypothesis is that the 1-sigma  
143 uncertainty is the maximum estimate of error for that interval by assuming that  
144 there is no field difference among the three measurements over such a short time  
145 interval. In reality, there will be some small trend in the three successive  
146 measurements due to real changes in the paleomagnetic field. So the 1-sigma error  
147 incorporates some real error in measurement and some variation in field.

148 Figures 2 and 3 show the inclination and declination records of the five PSV  
149 records for the last 3000 years (small closed circles). The records all have error  
150 envelopes of  $\pm 1$  sigma. We also show the summary of historical measurements  
151 (open squares) for the last  $\sim 400$  years, termed *gufm1* (Jackson et al., 2000). We  
152 have developed equi-spaced time series in 100-yr increments for all of these PSV  
153 studies (larger solid circles connected in Figures 2 and 3). There are 10 reproducible  
154 scalar features in the inclination and declination records (a-j in Figures 2, 3). The  
155 resultant equi-spaced time series are summarized in Table 1 and listed in Appendix  
156 1. These time series are part of a large group of equi-spaced Holocene PSV time  
157 series from around the World termed PSVMOD2.0 (total of 87 sites). The typical  
158 directional difference between the actual PSV data and their PSV models is less than  
159  $\pm 1^\circ$ .

160 We have grouped these five sites together because they are largely closer to  
161 one another than any other Holocene PSV sites within PSVMOD2.0. Even so, it is  
162 worth considering, as we move forward with the data analysis, whether these five  
163 sites all represent the same regional sense of dynamo activity in the outer core  
164 below them. The fact that all five sites share most or all of the same simple scalar  
165 PSV features (Figures 2, 3), is one measure that they all do covary, in some sense of  
166 the word. The fact that the individual scalar features are not exactly synchronous  
167 could simply be due to some error in the site chronologies.

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## 170 Circularity Estimates

171

172 We have estimated circularity of the vector time series in two ways. We first  
173 calculated the amplitude and direction of circularity in the smallest time interval  
174 available to us – 200 years or three successive data points. Figures 4 (a, b) show two  
175 examples of 200-yr circularity intervals. Three successive paleomagnetic directions  
176 are needed to define any arcuate motion. If the three directions fall on a straight line,  
177 then there is no circularity. But, if the three directions form a triangle with some  
178 discrete area, as in Figure 4 (a, b), then we can estimate both the direction of  
179 circularity, clockwise (C) or counterclockwise (CC), and the ‘amplitude’ of the  
180 circularity defined by the triangular area associated with the three points. We have  
181 also calculated the circularity for an interval of five successive points (400 yrs). This  
182 gives a more smoothed estimate of circularity, but helps to define intervals among  
183 the records with a common sense of circularity. All calculations were done in 100-yr

184 steps or increments with the central year (of three or five data points) defining the  
185 calculation year.

186 The results of the three-point (200 yr) circularity calculation for all five sites  
187 over the last 3000 years are shown in Figure 5 (open circles). The value magnitudes  
188 indicate the area of the three-point triangles (in arc degrees squared) with positive  
189 values indicating clockwise motion and negative values indicating counterclockwise  
190 motion. There are occasionally amplitudes that are almost zero, indicating simple  
191 linear, not arcuate, motion for each 200-yr increment. But, more than 90% of the  
192 values do indicate some sense of circularity. The results of the five-point (400 yr)  
193 circularity calculation for all five sites over the last 3000 years are shown in Figure 5  
194 (closed circles). This gives a more smoothed/integrative sense of circularity. All five  
195 sites seem to show the same general pattern of circularity with 300-900 years of  
196 one sense of circularity alternating with the other sense of circularity. We have  
197 labeled seven alternating intervals of circularity (A-G).

198 There is generally good circularity agreement among the five time series, but  
199 the interval from 500-1000 AD is marked by low amplitude circularity and SEN,  
200 2220, and ECS have some evidence of small amplitude counterclockwise circularity  
201 while the other two time series have small amplitude clockwise circularity. This is  
202 probably an artifact of the data. Overall, all five records show the same 7 alternating  
203 counter-clockwise/clockwise pattern of circularity.

204 The second way to estimate circularity is to look for notable intervals of  
205 looping in the time series. We looked primarily for complete loops (usually five or  
206 more points (>400 yrs of circularity), but accepted partial loops that appeared to be  
207 at least  $\frac{1}{2}$  loop (Figure 4c). The difference in this method is that we ignored small  
208 intervals of one sense of looping (<<  $\frac{1}{2}$  loop) if they fell within a larger pattern of  
209 looping of the opposite sense. In this way, we typically identified 7 complete or  
210 partial loops in all five time series. That is the same number of looping intervals  
211 noted above by the time series analysis. Table 2 summarizes the loops in each time  
212 series. Figure 5 shows the intervals of notable looping to the right of each site (black  
213 intervals are clockwise loops, white intervals are counterclockwise loops).  
214 Transitions between clockwise and counter-clockwise looping studied in this  
215 manner allow 100-300 year overlaps in circularity sense. We labeled the notable  
216 loops  $\alpha$ -v (numbers in parentheses indicate a whole loop or partial loop) and we see  
217 evidence for each of these loops in all five time series. The loops are present in all  
218 the PSV sites and almost all the correlatable loops are the same sense of circularity.  
219 Some loops are a bit longer or shorter in duration than others from the same time  
220 interval and there is some variation in overall size of comparable loops.

221 Figure 6 plots the pattern of circularity in four intervals. Figures 6 (a, b) plot  
222 the circularity at LEB and ECS for the last 1500 years. They clearly show the  
223 alternating C/CC oscillations in circularity that are summarized in Figure 5. Figures  
224 6 (c, d) plot the circularity at LEB and SEN for 500 AD-1000 BC. Here, too, one can  
225 see a clear alternation of circularity as summarized in Figure 5.

226 We can estimate the size of each loop by calculating the inclination and  
227 declination span for each loop (Table 2). Some loops are quite large and the  
228 declination span (but not the inclination span) is affected by site latitude. Therefore,  
229 we have normalized the declination spans by  $\text{COS}(\text{site latitude})$ . We have calculated

230 an overall ‘amplitude’ for each loop as the RMS of the inclination and normalized  
231 declination spans. The loop ‘amplitudes’ and durations (for a complete loop) are  
232 plotted in Figure 7 (top). There appears to be a fairly linear trend with smaller  
233 amplitude loops having shorter durations and larger amplitude loops having longer  
234 durations. There is also a bias for larger amplitude/longer duration loops being  
235 clockwise.

236 This is almost identical to the circularity pattern for Holocene East Asia  
237 (Lund, 2020) shown in Figure 7 (bottom). Here, too, the looping pattern has shorter-  
238 duration (longer-duration) loops being smaller (larger) in amplitude and the  
239 largest/longest loops being clockwise. Thus, there is here, too, a bias to clockwise  
240 circularity over counter-clockwise circularity. Also, in both regions, the circularity  
241 pattern is an alternation of clockwise versus counter-clockwise looping with neither  
242 lasting much more than one full loop. This teeter-totter effect is very distinctive and  
243 also seems to be presents in recent longer-duration Pleistocene PSV records now  
244 under analysis (Lund, in review). These are the only two Holocene regions to  
245 undergo this type of circularity analysis. Yet, it seems that this distinctive pattern  
246 may be normal for overall PSV. Further studies are under way to test these  
247 observations further.

248 Three of the PSV time series (SEN, 2220, ECS)) are 8000 years in duration.  
249 We plot these time series in Figure 8. We plot their circularity rates in Figure 9. The  
250 horizontal tie lines indicate intervals of clockwise or counterclockwise circularity  
251 that the sites have in common. Intervals A-G are also shown in Figure 5. Circularity  
252 is more subdued before 1000 BC. This may be a matter of reduced data resolution,  
253 but the same pattern is noted in the East Asia data (Lund, 2020).

254 One last observation with respect to Eastern North America PSV circularity is  
255 that most or all five sites share the same short-duration, but largest-rate, circularity  
256 intervals. The Circularity rates of all five sites are shown in Figure 10 (open circles)  
257 (also shown in Figure 5). We have also calculated the more traditional secular  
258 variation rates for the same time intervals. Figures 4 (a, b) illustrate how we  
259 calculate absolute PSV rate in 200-year increments. We have calculated the  
260 incremental absolute secular variation rates for the intervals 0-100 years and 100-  
261 200 years (labeled r1 and r2 in Figures 4 (a, b)) for each circularity interval and  
262 averaged them. The average absolute secular variation rates per 100 years averaged  
263 over a 200-year circularity interval are also plotted in Figure 10 (solid circles). It is  
264 clear that the narrow intervals of highest-rate circularity are also the intervals of  
265 highest-rate average absolute secular variation. Arrows in Figure 10 show 5  
266 intervals of highest secular variation/circularity rate that seem to be common to  
267 most of the records. The high rate intervals tend to occur at the boundaries between  
268 clockwise and counter-clockwise circularity. This is clearest at the onset and  
269 termination of clockwise intervals B and F in Figure 10. Similar short intervals of  
270 high secular variation/circularity rate are noted in East Asia. But they do not  
271 generally occur at the same times as in Eastern North America.

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274 Discussion

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276 Geomagnetic secular variation has been associated with a variety of different  
277 fluid motions in the Outer Core. Some motions are 'linear' in the sense that they  
278 suggest consistent movement of dynamo sources in one direction through drift  
279 (westward, eastward, poleward). Another possibility is that localized fluid flow is  
280 analogous to a 'whirlpool' with magnetic directions 'spinning' clockwise or  
281 counterclockwise in response. Both of these types of motion should produce a series  
282 of open loops of the same type (either clockwise or counterclockwise) through time.  
283 However, our data suggest a 'teeter-totter' behavior with alternating clockwise and  
284 counter-clockwise motion. We never see two consecutive full clockwise or  
285 counterclockwise loops in either the Holocene Eastern North America PSV or the  
286 East Asia PSV (Lund, 2020).

287 It seems likely that a significant component of the Outer Core fluid flow (and  
288 resulting secular variation) oscillates back and forth between clockwise and  
289 clockwise states. Figure 5 suggests maybe 3 or 4 such oscillations within the last  
290 3000 years in Eastern North America. This is seen in both estimates of circularity –  
291 circularity rates and larger –scale looping. This is also seen in Holocene East Asia  
292 (Lund, 2020). Previous PSV studies have sometimes estimated coherent intervals of  
293 circularity that last 6-10 thousand years (e.g., Lund and Banerjee, 1985). It may be  
294 that a more careful (regional) analysis, such as carried out here, might see evidence  
295 of more complexity in circularity than previously noted.

296 The amplitude and duration of coherent circularity in our study is distinctive.  
297 There are shorter intervals of clockwise or counterclockwise circularity, perhaps a  
298 little as 300-400 years in duration with relatively low circularity rates (or looping  
299 amplitudes). There is also evidence of at least one interval of circularity that lasts  
300 perhaps 1000-1200 years and has large amplitude looping. (Figure 7 top) Even  
301 larger clockwise loops (~1500 years) are seen in Holocene PSV from East Asia  
302 (Lund, 2020) (Figure 7 bottom).

303 The duration of coherent cyclicity also seems to be unbalanced. More than  
304 2/3 of the last 3000 years in both Eastern North America and East Asia have been  
305 periods of clockwise circularity. Individual periods of counterclockwise circularity  
306 always last less than 1000 years and average ~700 years (Figure 7). Clockwise  
307 loops tend to average ~1000 years. It is not clear that there is such a bias between  
308 3000-8000 ybp (Figure 9) but the data are less numerous or as high in quality as  
309 data for the last 3000 years (Figure 5).

310 Studies of anomalous historical secular variation intervals, which are termed  
311 geomagnetic jerks (Courtillot and LeMouel, 1976, 1984), have been associated with  
312 azimuthal (torsional) oscillations of outer core fluids on yearly intervals (Bloxham  
313 et al., 2002). Dumberry and Bloxham (2006) have also suggested that azimuthal  
314 oscillating flows might be a major cause of PSV on a millennial scale. If such zonal  
315 oscillations are combined regionally with more complex fluid flow that can lead to  
316 magnetic flux regeneration, then this might be the source of our circularity  
317 observations. Dumberry and Bloxham (2006) also suggested the azimuthal torsional  
318 oscillation might occur against a background of more steady fluid flow. This might  
319 account for the unbalanced time spent in clockwise versus counter-clockwise  
320 circularity. Torsional oscillation in the direction of steady flow might lead to longer  
321 time intervals of one sense of circularity (clockwise), while oscillations opposite the

322 direction of steady flow might lead to shorter time intervals of the opposite sense of  
323 circularity (counter-clockwise).

324 Another distinctive feature that all the PSV records share is that circularity  
325 rates significantly increase for short periods of time (200-400 years) at the  
326 transitions from clockwise to counterclockwise looping (Figures 5, 10). To a lesser  
327 extent absolute secular variation rates are also highest at these times (Figure 10).  
328 These short intervals of high circularity rate (labeled B, D, and F in Figure 5 and 10)  
329 are quite distinctive with rates up to 5 times that of normal circularity intervals.  
330 Similar short interval increased rates of PSV have been noted in Holocene East Asia  
331 PSV

332 These short-duration intervals of accelerated secular variation with change  
333 in circularity direction seem to be broadly analogous to historic magnetic field jerks  
334 or impulses (Courtilot and LeMouel, 1976, 1984). These impulses are abrupt  
335 accelerations of normal historical secular variation that last only 1-2 years in the  
336 context of the last ~100-200 years of historical field variability. Gallet et al. (2003)  
337 studied archeomagnetic data from Europe and identified similar abrupt ( $10^2$  years)  
338 cusps or hairpins in directional data that they associated with intervals of relatively  
339 high paleointensity. These short (~100-200 years) intervals of anomalously high  
340 PSV rate occur within the context of the last 2000-3000 years of PSV in Europe.  
341 Gallet et al. (2003) called these events archeomagnetic jerks and argued that they  
342 were intermediate between geomagnetic jerks ( $10^0$  years) and magnetic field  
343 excursions ( $10^3$  years). (It is probably better to refer to these a paleomagnetic jerks  
344 since they can be recorded in sediment PSV records as well as archeological time  
345 series.) It seems reasonable to argue that our short-duration intervals of accelerated  
346 secular variation with changes in circularity direction are also examples of  
347 paleomagnetic jerks or impulses. Altogether, these various 'short' intervals of  
348 anomalous secular variation rate that occur within the context of ongoing secular  
349 variation on a variety of time scales may reflect an intrinsic, chaotic element in the  
350 overall dynamo process.

351 Figure 11 shows the late Holocene central North American paleointensity  
352 record (Lund et al., 2021). This composite record included paleointensity estimates  
353 from the LEB, SEN, 2220, and ECS PSV records. Arrows indicate the highest rate  
354 circularity an overall PSV in our records (Figure 10). All of our accelerated intervals  
355 seem to be associated with relatively fast-changing intensity, either increasing or  
356 decreasing. There does not seem to be any indication of fast PSV at intensity highs  
357 or lows as was noted for East Asia (Lund, 2020). More regional studies are needed  
358 to carefully assess these relationships.

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361 Conclusions

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363 This study summarizes the pattern of directional paleomagnetic secular  
364 variation (PSV) in five previously published Holocene records from Eastern North  
365 America. Each record is high in resolution and well dated. We have developed equi-  
366 spaced (100-year increment) time series for the declinations and inclinations for the  
367 five sites and compared their overall directional variability. We see evidence of ten

368 correlatable scalar features in both inclination and declination. These comparisons  
369 suggest that, to first order, these five PSV records all estimate the same regional  
370 pattern of PSV for Eastern North America.

371 We specifically focus on the clockwise or counter-clockwise motion of  
372 paleomagnetic directions (termed circularity) in these PSV records. We have used  
373 two techniques to estimate the directional circularity of each PSV record. We have  
374 first calculated the incremental rate and direction of motion (clockwise or counter-  
375 clockwise) in 200-year increments for each record over the last 3000-8000 years.  
376 We have separately used a more traditional technique of looking for discernable  
377 looping (full loops down to 1/2 loops) in individual records. We estimate the loop  
378 sizes, durations, and circularity direction.

379 We largely see the same pattern of circularity in both measurement  
380 techniques. There are seven intervals of oscillating circularity (clockwise versus  
381 counter-clockwise) in all five sites. They generally agree in timing and direction of  
382 circularity. We also see evidence for seven discernable directional loops alternating  
383 between clockwise and counter-clockwise in all five records. Both techniques  
384 suggest an oscillating, teeter-totter like, behavior to PSV circularity that must be due  
385 to the pattern of fluid flow/magnetic flux regeneration in the outer core. This teeter-  
386 totter behavior is unbalanced with more time spent in clockwise motion as in  
387 counter-clockwise motion. Less than 10% of the overall time series duration is spent  
388 in linear (not circulating) behavior. The loops tend to have a distribution of sizes  
389 and durations with smaller loops being shorter in duration (400-800 years) and  
390 bigger loops having longer durations (600-1200 years).

391 The teeter-totter alternation of clockwise versus counter-clockwise  
392 circularity is distinctive and may be a normal aspect of PSV. The alternation is not  
393 consistent with several traditional ideas about fluid flow (drift, whirling motion,  
394 simple convection). Recent studies have identified torsional oscillations as a source  
395 for both historical short-term ( $10^0$ ) and millennial-scale ( $10^3$ ) secular variation  
396 (Bloxham et al., 2002; Dumberry and Bloxham, 2006).

397 One particular feature of these circularity patterns bears special note. All five  
398 PSV records show short-tern (200-400 years) significant acceleration in circularity  
399 rate combined with change in circularity direction. We see evidence for five of these  
400 short intervals. These features are also intervals of the fastest regular secular  
401 variation rates in all the records. These features are analogous to geomagnetic jerks  
402 (Courillot and LeMouel, 1976, 1984) in that they are short intervals of anomalous  
403 acceleration. But geomagnetic jerks occur historically every 20-40 years and last  
404 only 1-2 years. Gallet et al. (2003) showed evidence in PSV for similar anomalous  
405 acceleration intervals ( $\sim 10^2$  yrs), which they termed archeomagnetic jerks. We  
406 think our anomalous intervals are comparable to those of Gallet et al. (2003). We  
407 think these features are a natural and common aspect of directional PSV, but more  
408 regional PSV studies are needed to test that possibility.

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510 Figure Captions:

511

512 Figure 1: Map of Eastern North America showing the sites of eight paleomagnetic  
513 studies discussed in the text.

514

515 Figure 2: A summary of the best quality PSV inclination records for Eastern North  
516 America over the last 3000 years. Small solid circles are PSV data from  
517 published records; lines to either side indicate  $\pm 1$ -sigma. Large solid circles  
518 are equi-spaced model inclination time series for each record (100 year  
519 spacing). Open squares indicate estimates of historical field for each locality  
520 determined by Jackson et al. (2000). The typical difference between model  
521 and original data is less than  $\pm 1^\circ$ .

522

523 Figure 3: A summary of the best quality PSV declination records for Eastern North  
524 America over the last 3000 years. Small closed circles are PSV data from  
525 published records; lines to either side indicate  $\pm 1$ -sigma. Larger solid circles  
526 are equi-spaced model declination time series for each record (100 year  
527 spacing). Open squares indicate estimates of historical field for each locality  
528 determined by Jackson et al. (2000). The typical difference between model  
529 and original data is less than  $\pm 1^\circ$ .

530

531

532 Figure 4: Graphical representation of the methodology used to calculate true  
533 circularity rates (a, b) and looping patterns (c). Areas of looping in a and b  
534 are measured in arc degrees squared (area).

535

536 Figure 5: The results of two methods for calculating circularity for each model time  
537 series. True circularity rates are plotted for 3-point (open circles) and 5-  
538 point (solid circles) circularity at each site in units of arc degrees squared  
539 (area) At left in each column is an alphanumeric zonation of intervals  
540 dominated by clockwise (grey intervals) and counterclockwise (white  
541 intervals) circularity. At right, are columns labeled with greek lettering that  
542 indicate intervals of distinctive looping (black columns have clockwise  
543 looping and white columns have counterclockwise looping).

544

545 Figure 6: Bauer plots of inclination versus declination movement versus time within  
546 each time series. Clockwise (C) or counter-clockwise (CC) loops are shown  
547 for clarity.

548

549 Figure 7: Plot of individual discernable loops by duration versus overall amplitude.  
550 Figure 7 top is data from Eastern North America. Figure 7 bottom is data

551 from East Asia. Amplitudes are calculated in Table 2. The straight-line fit  
552 through the data give a sense to shorter (longer) duration loops being  
553 smaller (larger) in amplitude.

554

555 Figure 8: PSVMOD2.0 inclination and declination models of the three longest PSV  
556 records from the Eastern North America region.

557

558 Figure 9: Circularity calculation for the three longest PSV records. True circularity  
559 rates are plotted for 3-point (open circles) and 5-point (solid circles)  
560 circularity at each site. The alphanumeric letters correspond to the same  
561 zones plotted in Figure 5.

562

563 Figure 10: Comparison of true circularity rate (arc degree squared, 3-pt average,  
564 open circles) with absolute interval secular variation rate (arc degrees over  
565 same interval as circularity) irrespective of directional circularity.

566

567 Figure 11: Paleointensity record for central North America. Arrows indicate  
568 intervals of fast circularity or PSV rate.

Figures 1-11.

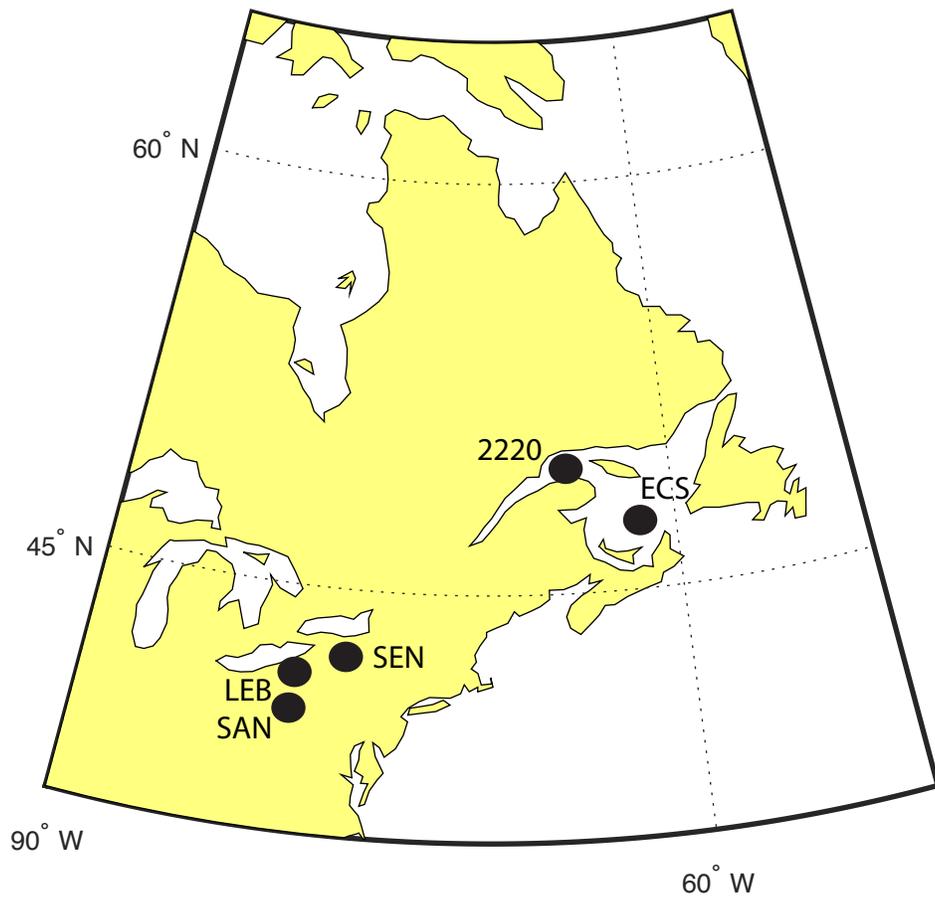


Figure 1

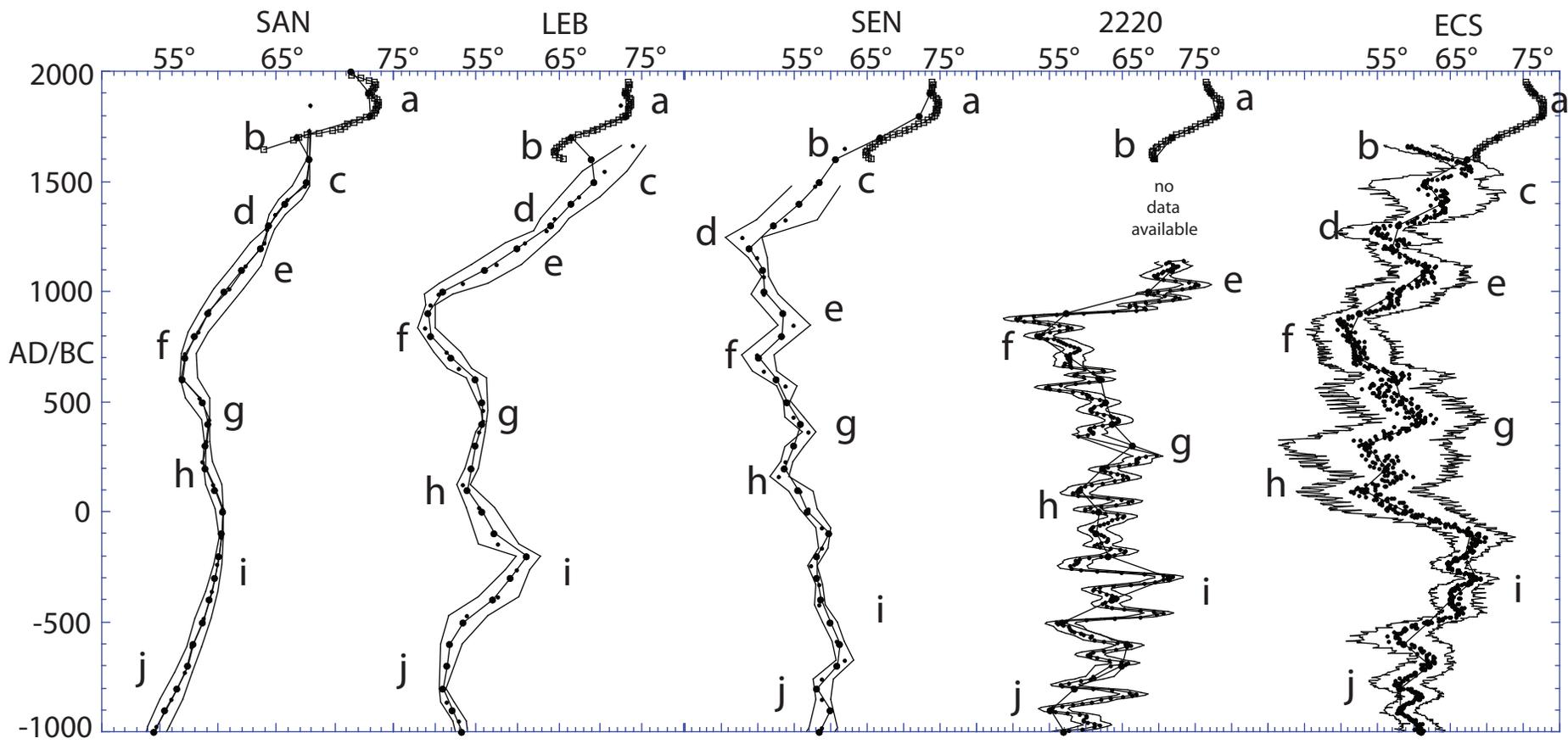


Figure 2

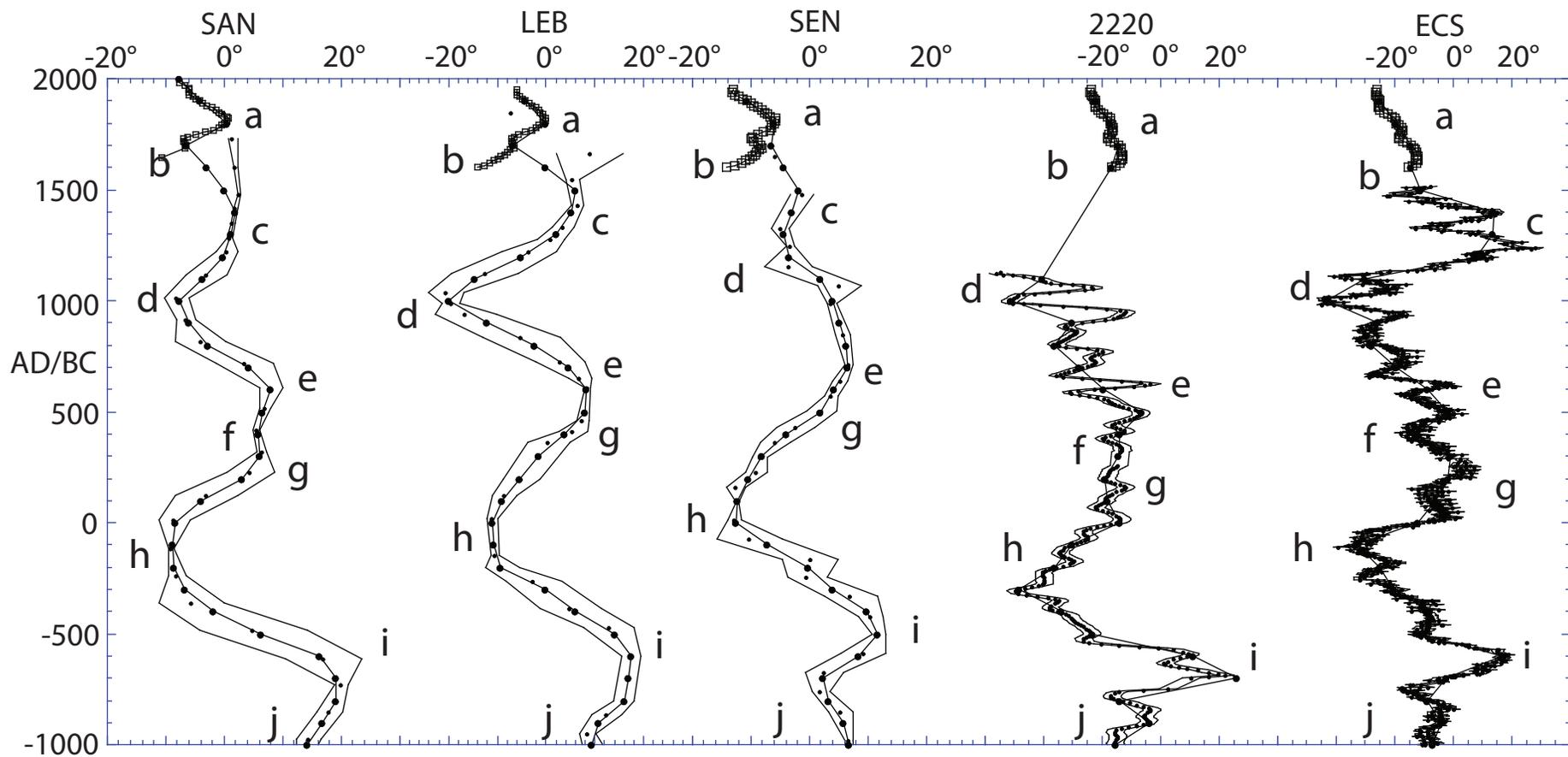


Figure 3

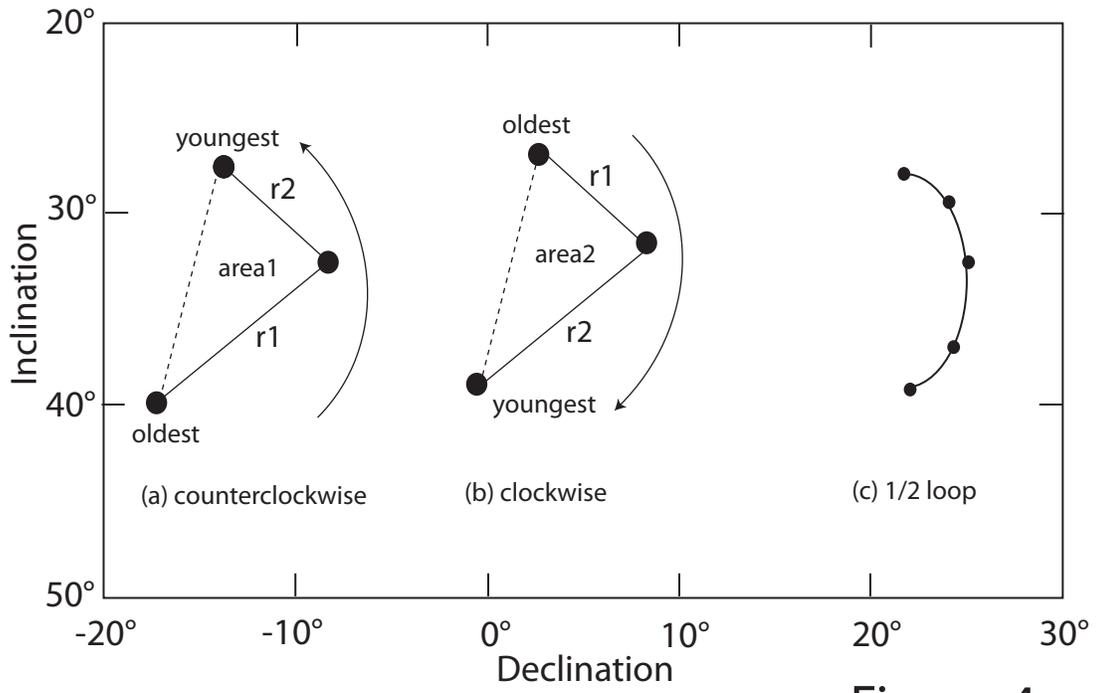


Figure 4

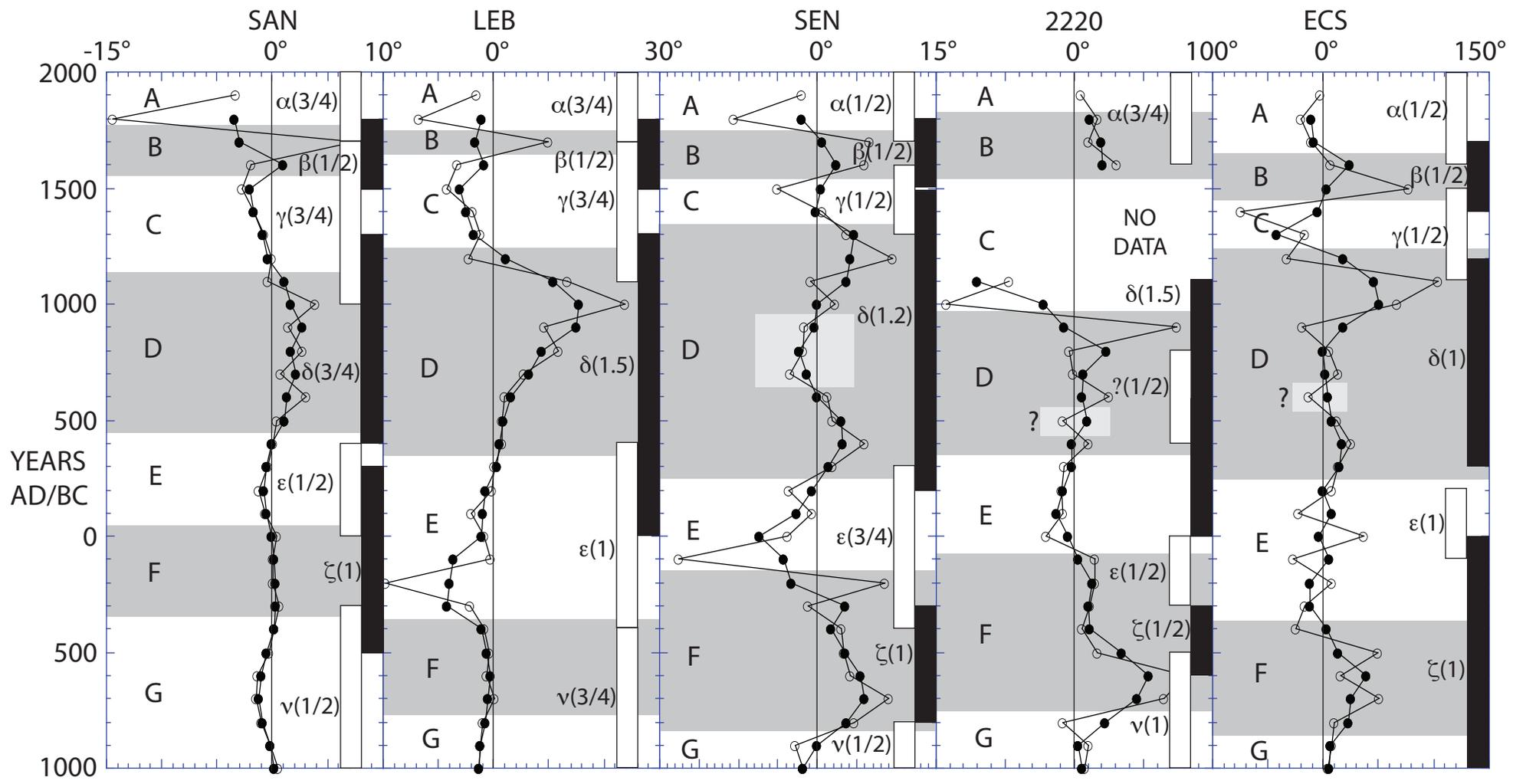


Figure 5

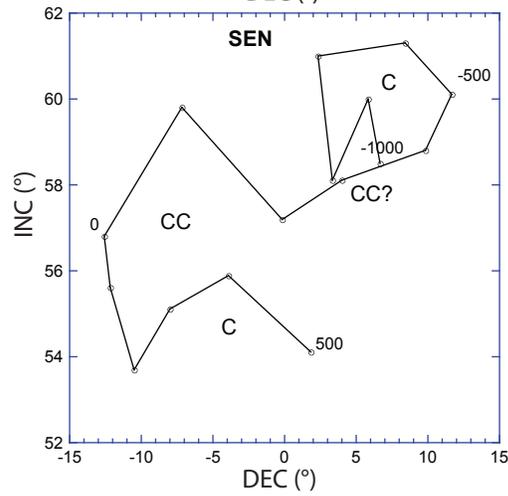
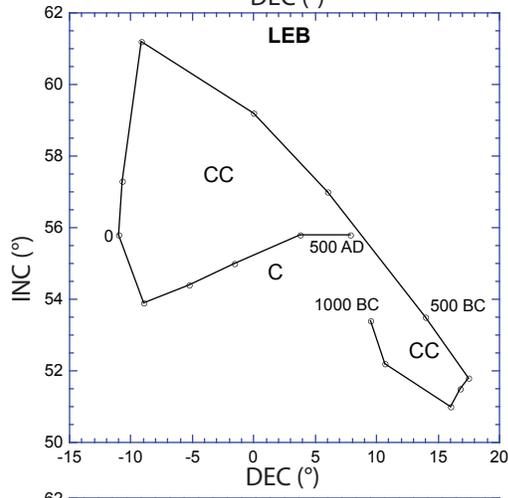
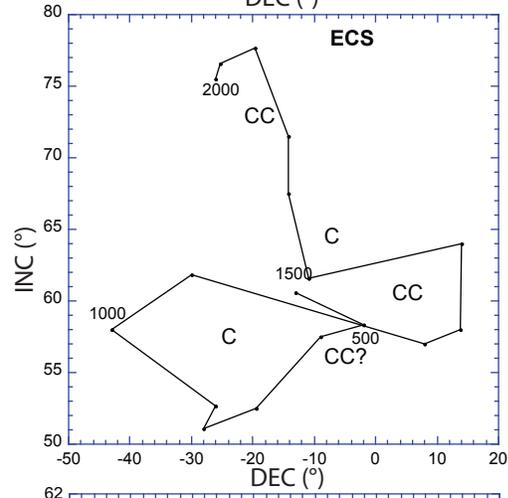
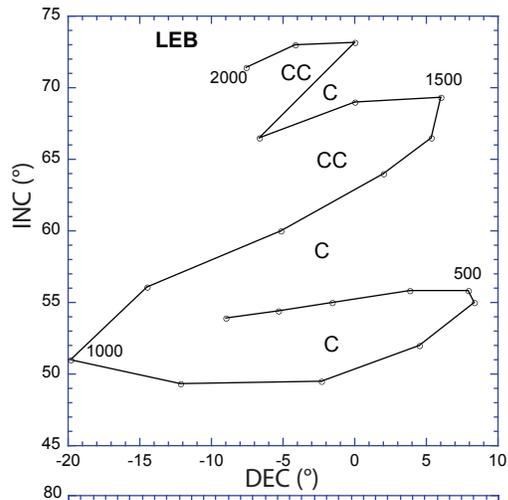


Figure 6

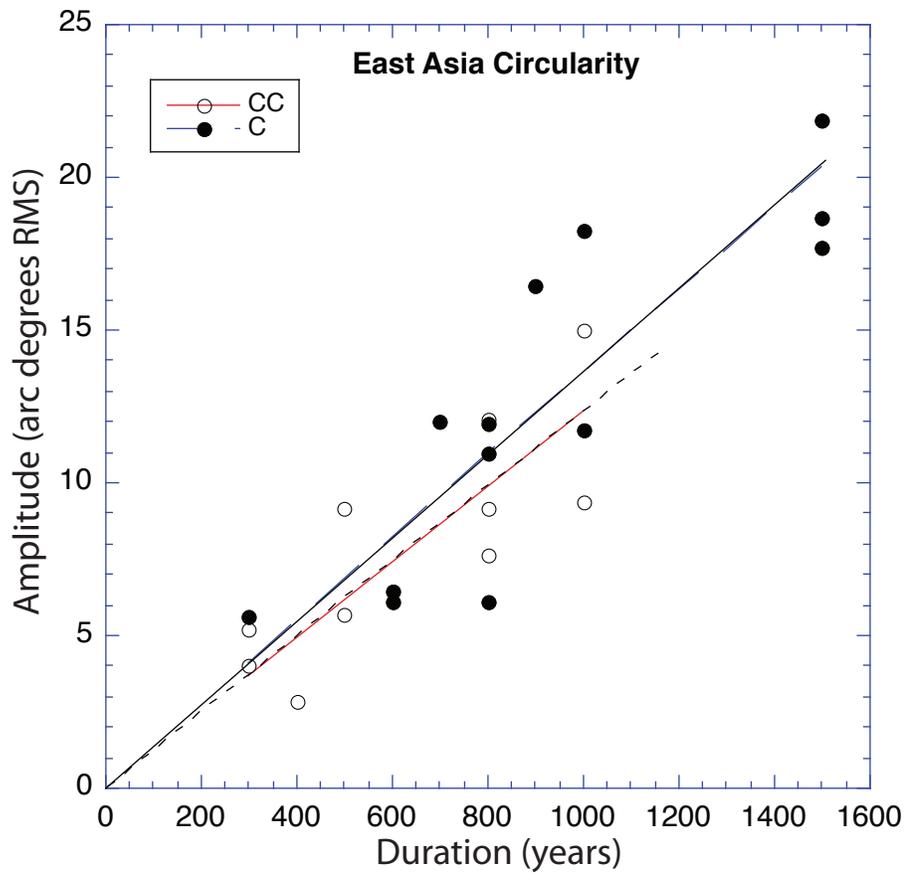
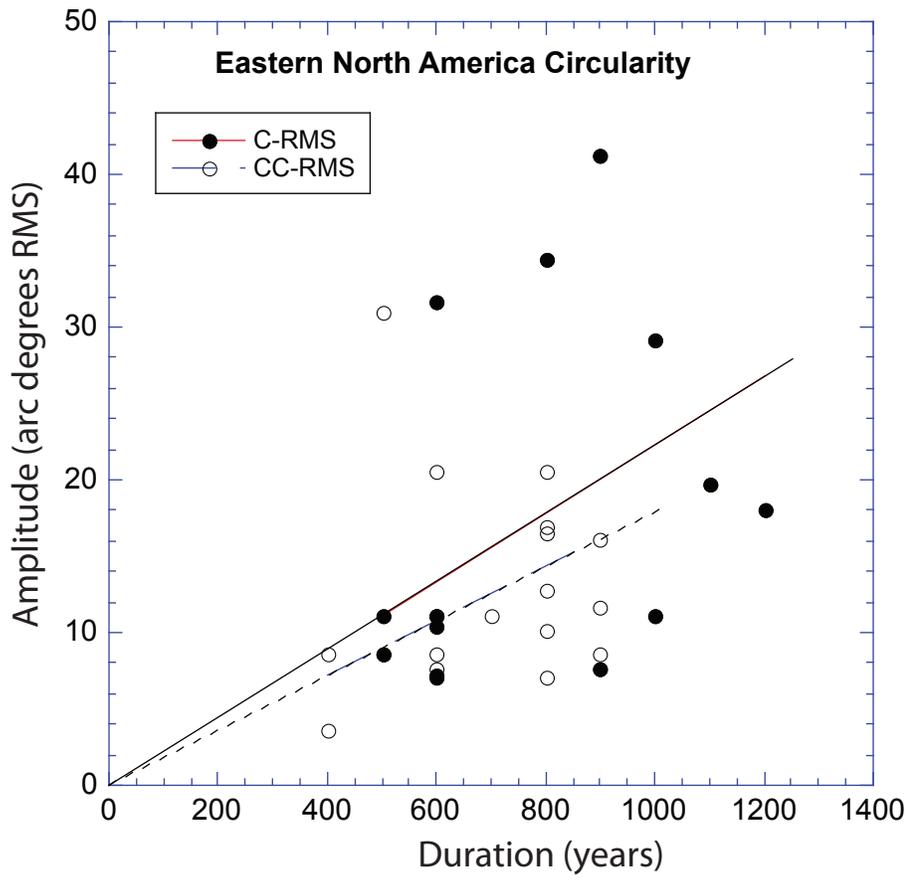


Figure 7

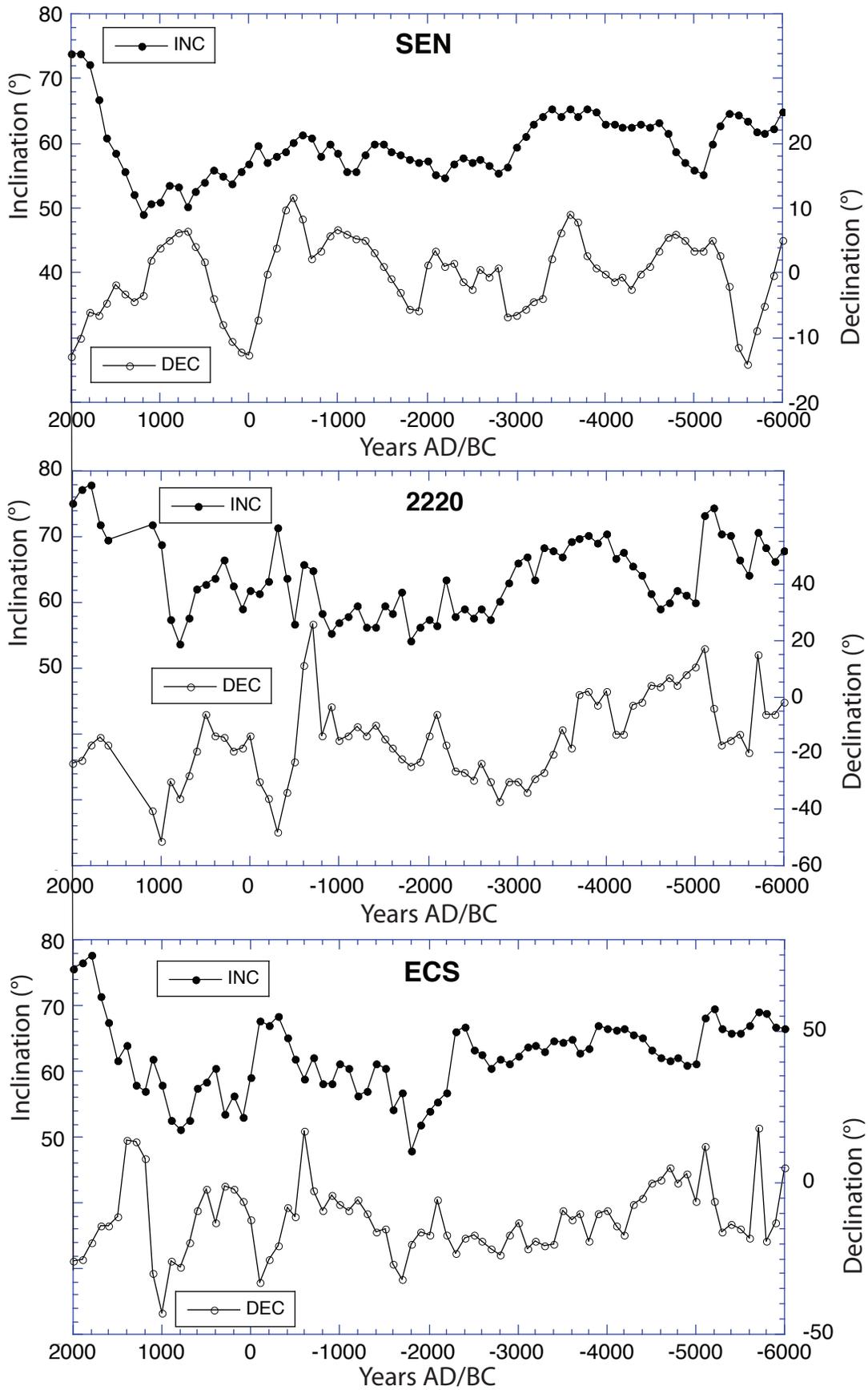


Figure 8

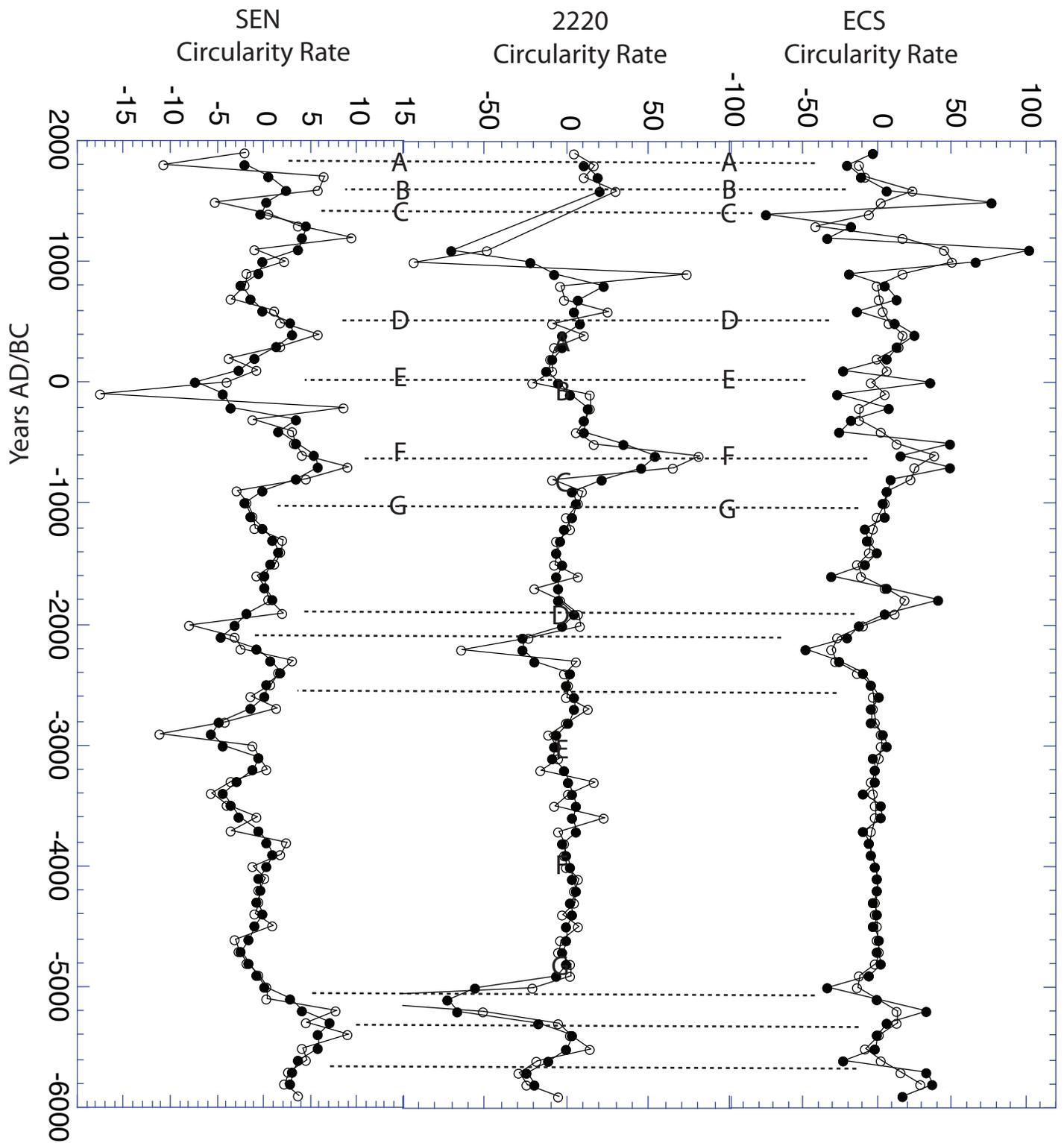


Figure 9

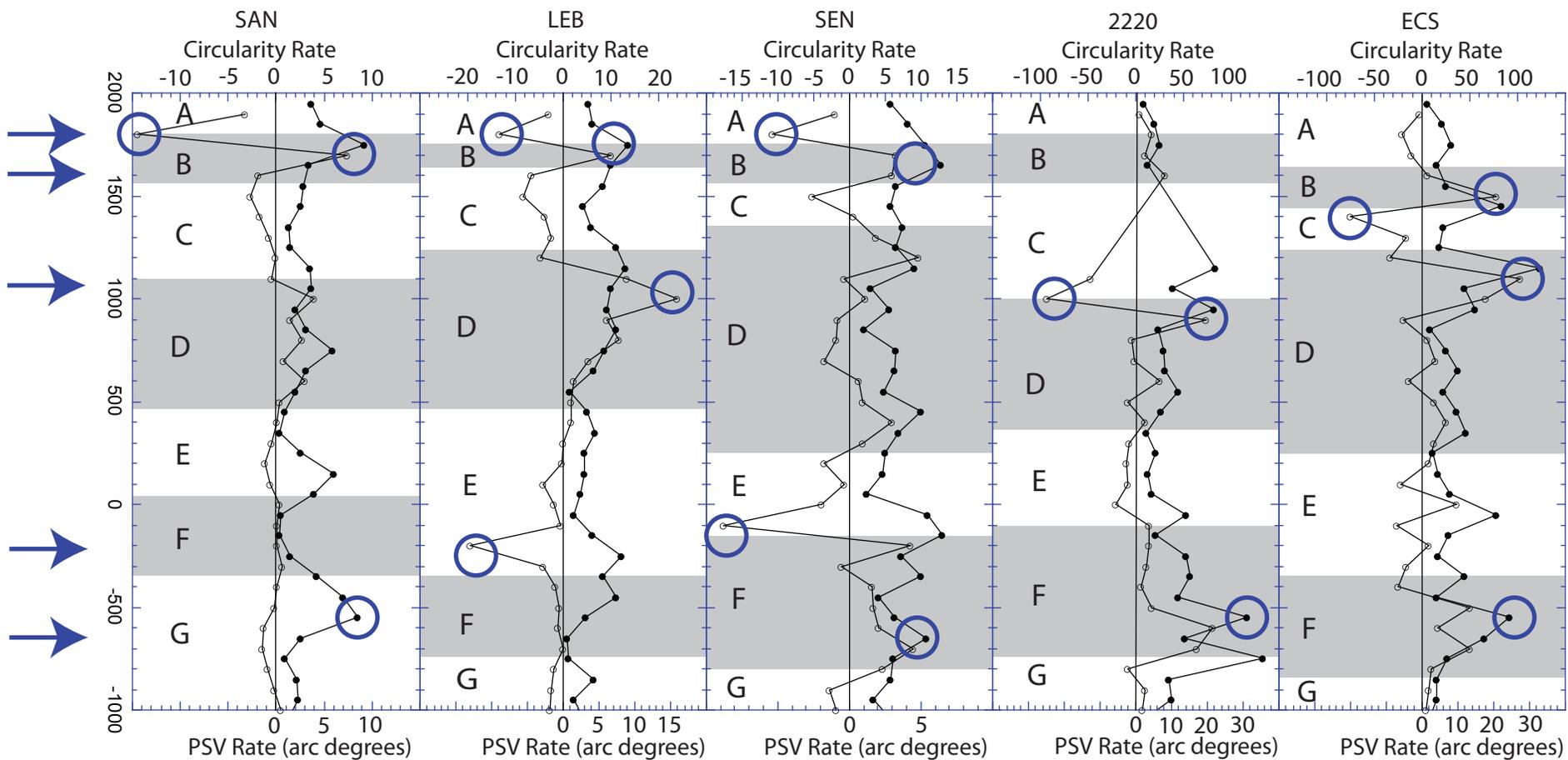
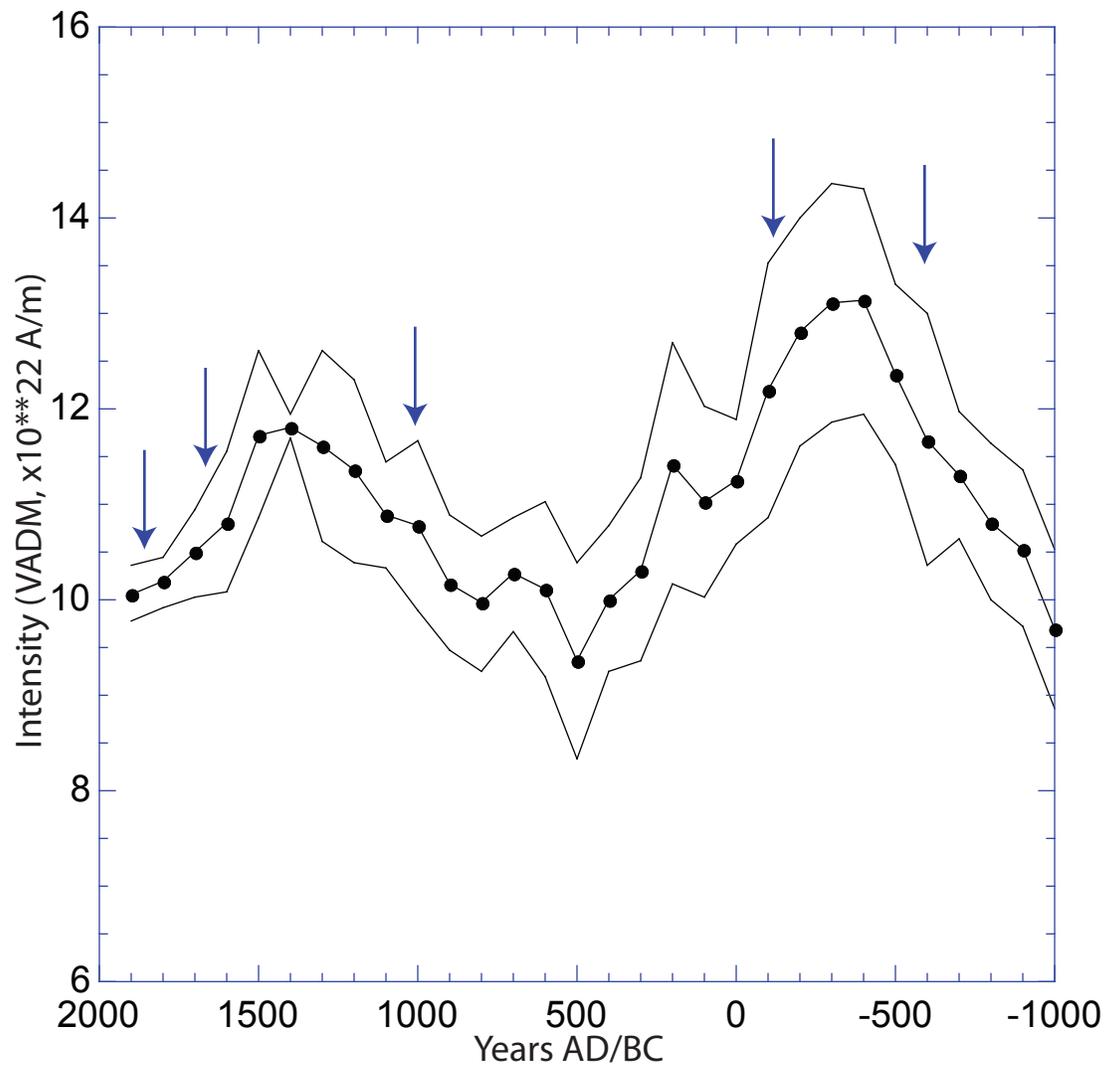


Figure 10



APPENDIX 1: PSVMOD2.0 datasets for Sandy Lake (SAN), Lake Lebeouf (LEB), Seneca

AD/BC	SAN-INC	SAN-DEC	LEB-INC	LEB-DEC
2000	71.4	-7.6		
1900	72.9	-4.2	73	-4.2
1800	73.1	0.6	73.2	0
1700	66.8	-6.5	66.5	-6.7
1600	67.8	-3	69	0
1500	67.6	0	69.3	6
1400	65.7	1.8	66.5	5.3
1300	64.4	1.3	64	2
1200	63.7	-0.2	60	-5.2
1100	62.1	-3.8	56.1	-14.5
1000	60.6	-7.7	51	-19.8
900	59.2	-6.1	49.3	-12.2
800	58	-2.7	49.5	-2.3
700	57.2	4.2	52	4.5
600	57	7.9	55	8.3
500	58.7	6.6	55.8	7.9
400	59.2	5.8	55.8	3.8
300	58.9	6	55	-1.6
200	58.9	3	54.4	-5.3
100	59.7	-3.9	53.9	-9
0	60.4	-8.4	55.8	-11
-100	60.3	-8.9	57.3	-10.7
-200	60.1	-8.5	61.2	-9.2
-300	59.7	-6.8	59.2	0
-400	59.3	-1.9	57	6
-500	58.7	6.2	53.5	14
-600	57.9	16.2	51.8	17.5
-700	57.4	19.2	51.5	16.8
-800	56.5	19	51	16
-900	55.5	16.7	52.2	10.7
-1000	54.5	14.1	53.4	9.5
-1100	53.7	13	54	13.3
-1200	53	12.7	52.8	14
-1300	53.1	10.3	52.2	12.7
-1400	54	7.5	51.8	6.5
-1500	55.2	4.5	53	-2.7
-1600	56	3	54.7	-7.8

-1700	57.4	1.5	56	-8.5
-1800	58.5	-0.1	58.3	-2
-1900	59.1	-1.6	59.5	0.8
-2000	59.1	-2.2		
-2100	59.3	-2		
-2200	59.9	-0.3		
-2300	60.9	1.5		
-2400	61.5	0.7		
-2500	62.1	1		
-2600	62.6	1.3		
-2700	63.4	0.5		
-2800	64.3	-0.4		
-2900	65	-1.6		
-3000	65.9	-2.3		
-3100	67	-3		
-3200	67.7	-2.3		
-3300	67.9	-1.9		
-3400	66.6	0.3		
-3500	64.2	3.4		
-3600	62.5	6		
-3700	62.2	4.9		
-3800	62.4	0.3		
-3900	62.7	-3.6		
-4000				
-4100				
-4200				
-4300				
-4400				
-4500				
-4600				
-4700				
-4800				
-4900				
-5000				
-5100				
-5200				
-5300				
-5400				
-5500				
-5600				
-5700				

-5800  
-5900  
-6000

ca Lae (SEN), core 2220 (2220) and the East Canada Stack (ECS).

SEN-INC	SEN-DEC	2220-INC	2220-DEC	ECS-INC
73.8	-7	77.2	-22.3	76.6
72.2	-6.1	78	-17	77.7
66.9	-6.5	71.9	-14.4	71.5
60.8	-4.5	69.5	-16.8	67.5
58.5	-1.8			61.6
55.8	-3.1			64
52.2	-4.4			58
49.001	-3.5			57
50.7	2	71.8	-40.2	61.8
51	3.9	68.8	-51	58
53.6	5.1	57.5	-30	52.7
53.4	6.3	53.7	-36	51.1
50.2	6.6	57.8	-27.7	52.5
52.7	4.2	62.1	-19.5	57.5
54.1	1.8	62.8	-6.3	58.3
55.9	-3.9	63.7	-14	60.6
55.1	-8	66.5	-14.5	53.5
53.7	-10.5	62.5	-19	56.3
55.6	-12.2	59.2	-18.2	53
56.8	-12.6	61.8	-14	59
59.8	-7.2	61.5	-30	67.8
58.2	-0.2	63.2	-36	67
58.1	4	71.5	-48.2	68.5
58.8	9.8	63.7	-34	65.2
60.1	11.7	56.8	-23	62
61.3	8.4	65.8	11	58.8
61	2.3	65	26	62.2
58.1	3.3	58.5	-14	58.2
60	5.8	55.3	-3.5	58.2
58.5	6.7	57	-15.5	61.2
55.6	6	58	-13.8	60.5
55.6	5.3	59.5	-10.3	56.2
58.2	5	56.3	-14	57
59.9	3.2	56.3	-10.2	61.3
59.9	1	59.5	-15	60.4
58.8	-0.9	58.5	-18	54.3

58.4	-2.9	61.7	-22	56.8
57.6	-5.6	54.3	-24.5	48
57	-5.9	56.2	-23	52
57.3	1.2	57.4	-14	54
55.2	3.5	56.5	-6	55.4
54.8	1	63.5	-17	56.8
56.8	1.6	58	-26.5	66
57.9	-1.3	59	-27	66.7
57.2	-2.5	57.8	-29.5	63.2
57.7	0.5	59	-23.8	62.5
56.7	-0.5	57.5	-30	60.6
55.4	0.9	60.3	-37	61.8
56.5	-6.7	63	-30	61.3
59.4	-6.5	66	-30	62.3
61.2	-5.6	67	-34	63.8
63	-4.3	63.6	-29	64
64.2	-3.9	68.5	-27	63.1
65.3	2.3	68	-20.3	64.7
64.2	6.3	67	-11.5	64.5
65.3	9.2	69.3	-18	65
64.3	7.8	69.7	1	62.9
65.5	2.8	70.2	2	63.5
65	0.7	69.2	-3	66.9
63	-0.2	70.4	2	66.5
63	-1.3	66.7	-13.5	66.4
62.5	-0.5	67.7	-13	66.5
62.5	-2.6	65.5	-3	65.7
63	-0.2	64.2	-2	65.1
62.5	1	61.5	4	63.4
63.3	3.3	59	3.8	62.2
61.5	5.5	60	7	61.7
58.8	6	61.8	4	62.2
57.2	5	61.3	8	60.9
55.9	3.5	60	10.5	61.1
55.2	3.4	73.3	17	68.1
59.9	5.1	74.5	-4.3	69.5
62.7	2.8	70.5	-17	66.5
64.6	-2.1	70.3	-15.5	65.9
64.5	-11.5	66.5	-13.5	65.9
63.6	-14	64.3	-20	67
61.8	-8.8	70.7	15	69

61.5	-5	68.5	-6	68.8
62.3	-0.3	66.2	-6	66.8
64.8	5	68	-2	66.6

ECS-DEC

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-25.2  
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Table 1: Summary of Eastern North American Paleomagnetic Secular Variation Records Used in This Study

Site Code	Site Location	Lat. (°N)	Lon. (°E)	Age Range (YBP)	Date Type	Final Sed. Rate	Qual.
2220	St. Lawr.	48.6	291.4	0-8000	C14	~100 cm/ky	A
ECS	St. Lawr.	48.2	295.5	0-8000	>10 C14	~100 cm/ky	A
LEB	Lake LeBeouf	41.9	280.1	0-4000	6 derived	~200 cm/ky	A
SAN	Sandy Lake	41.3	279.9	0-6000	8 C14	~180 cm/ky	A
SEN	Seneca Lake	43.0	286	0-8000	13 C14	~150 cm/ky	A

