

# 1 Optimal Stacking of Noise Cross-Correlation Functions

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## 5 SUMMARY

6 Cross-correlations of ambient seismic noise are widely used for seismic velocity imaging, mon-  
7 itoring, and ground motion analyses. A typical step in analyzing Noise Cross-correlation Func-  
8 tions (NCFs) is stacking short-term NCFs over longer time periods to increase the signal qual-  
9 ity. Spurious NCFs could contaminate the stack, degrade its quality, and limit its use. Many  
10 methods have been developed to improve the stacking of coherent waveforms, including earth-  
11 quake waveforms, receiver functions, and NCFs. This study systematically evaluates and com-  
12 pares the performance of eight stacking methods, including arithmetic mean or linear stacking,  
13 robust stacking, selective stacking, cluster stacking, phase-weighted stacking, time-frequency  
14 phase-weighted stacking,  $N^{th}$ -root stacking, and averaging after applying an adaptive covari-  
15 ance filter. Our results demonstrate that, in most cases, all methods can retrieve clear ballistic  
16 or first arrivals. However, they yield significant differences in preserving the phase and am-  
17 plitude information. This study provides a practical guide for choosing the optimal stacking  
18 method for specific research applications in ambient noise seismology. We evaluate the per-  
19 formance using multiple onshore and offshore seismic arrays in the Pacific Northwest region.  
20 We compare these stacking methods for NCFs calculated from raw ambient noise (referred to  
21 as Raw NCFs) and from ambient noise normalized using a one-bit clipping time normalization  
22 method (referred to as One-bit NCFs). We evaluate six metrics, including signal-to-noise ratios,  
23 phase dispersion images, convergence rate, temporal changes in the ballistic and coda waves,  
24 relative amplitude decays with distance, and computational time. We show that robust stacking

25 is the best choice for all applications (velocity tomography, monitoring, and attenuation stud-  
26 ies) using Raw NCFs. For applications using One-bit NCFs, all methods but phase-weighted,  
27 time-frequency phase-weighted, and  $N^{th}$ -root stacking are good choices for seismic velocity  
28 tomography. Linear, robust, and selective stacking methods are all equally appropriate choices  
29 when using One-bit NCFs for monitoring applications. For applications relying on accurate  
30 relative amplitudes, both the robust and cluster stacking methods perform well with One-bit  
31 NCFs. The evaluations in this study can be generalized to a broad range of time-series analysis  
32 that utilizes data coherence to perform ensemble stacking. Another contribution of this study is  
33 the accompanying open-source software, which can be used for general purposes in time-series  
34 stacking.

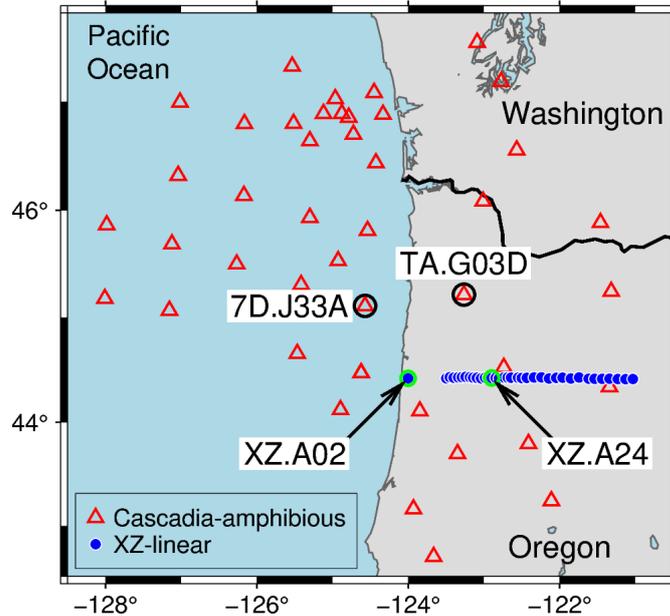
35 **Key words:** Seismic interferometry, Seismic tomography, Earthquake ground motions, Seis-  
36 mic noise, Time-series analysis, Coda waves

37 **1 INTRODUCTION**

38 Cross-correlations of ambient seismic noise have been widely used to image the Earth's elastic (L. Feng and Ritzwoller 2019;  
 39 Shapiro et al. 2005; S.-M. Wu et al. 2021; X. Yang and Gao 2018, 2020) and anelastic structure (Prieto et al. 2009), model  
 40 ground motions (Marine A Denolle et al. 2013, 2014, 2018; Kwak et al. 2017; Viens and Marine A Denolle 2019; Viens et al.  
 41 2017), and monitor transient velocity changes in the shallow subsurface (F. Brenguier et al. 2008; Clements and Marine A  
 42 Denolle 2018; Donaldson et al. 2019; K.-F. Feng et al. 2021; Olivier et al. 2019; Q.-Y. Wang et al. 2017; Z. Yang et al. 2022).  
 43 The Noise Cross-correlation Functions (NCFs) are typically computed in short-time windows (such as hours or days) after  
 44 diverse pre-processing on the raw ambient noise waveforms (Bensen et al. 2007; L. Feng and Ritzwoller 2019). Stacking of  
 45 NCFs over a longer period (such as weeks, months, or years) is a common procedure for most applications utilizing NCFs (e.g.,  
 46 Seats et al. 2012). For seismic tomography, the final stack over the entire time period is used to make waveform or travel-time  
 47 measurements. Seismic monitoring requires stacking over a subset of time windows, balancing the temporal resolution and the  
 48 coherence of the NCFs (Hadziioannou et al. 2011). These applications rely on the phase information of ballistic (first arrival)  
 49 and/or coda waves. Studies of ground motion prediction and attenuation tomography, on the other hand, require accurate  
 50 relative amplitude measurements between station pairs. Because NCFs consist primarily of dispersive surface waves, preserving  
 51 the relative amplitude also preserves the spectral content. Therefore, the performance of stacking and the preservation of either  
 52 phase or amplitude information are important to ensure the robustness of the scientific results.

53 The most commonly used stacking method is the arithmetic mean of the data over temporal or spatial samples, referred  
 54 to as Linear stacking. For NCFs, substantial temporal variation may exist across individual short time windows, which could  
 55 result from the seasonal change of the location and strength of the microseismic sources (Bensen et al. 2007; L. Ermert et  
 56 al. 2016; L. A. Ermert et al. 2021; Tian and Ritzwoller 2017; X. Yang et al. 2019), disruption from tectonic signals (Baig  
 57 et al. 2009), or unknown instrumental failures. It is important to use an appropriate stacking method to extract coherent NCFs,  
 58 particularly when strong variations of the data quality are present. Many more advanced methods have been developed to  
 59 improve the stacking of NCFs, and time-series data in general and overcome the limitations of Linear stacking. Rückemann  
 60 (2012) provides a summary of the theoretical background of several stacking methods to improve the common-mid-point  
 61 gathers in seismic reflection data. A systematical evaluation of the performance of different stacking methods in processing  
 62 real NCF data is highly desirable and required for optimal processing strategies.

63 In this paper, we compare eight algorithms used for stacking NCFs and evaluate their performance for canonical research  
 64 applications. These methods include: robust stacking (Pavlis and Vernon 2010), selective stacking (modified from Liu et al.  
 65 2009; Olivier et al. 2015), cluster stacking (a new method), Phase-Weighted Stacking (PWS; Schimmel and Paulssen 1997),  
 66 time-frequency Phase-Weighted Stacking (tf-PWS; Baig et al. 2009; Li et al. 2017; Schimmel and Gallart 2007; Schimmel  
 67 et al. 2011; Thurber et al. 2014; Zeng and Thurber 2016),  $N^{th}$ -root stacking (Millet et al. 2019; Rückemann 2012), and linear  
 68 stacking after applying an Adaptive Covariance Filter (ACF; Nakata et al. 2015). We exclude the stacking methods that use



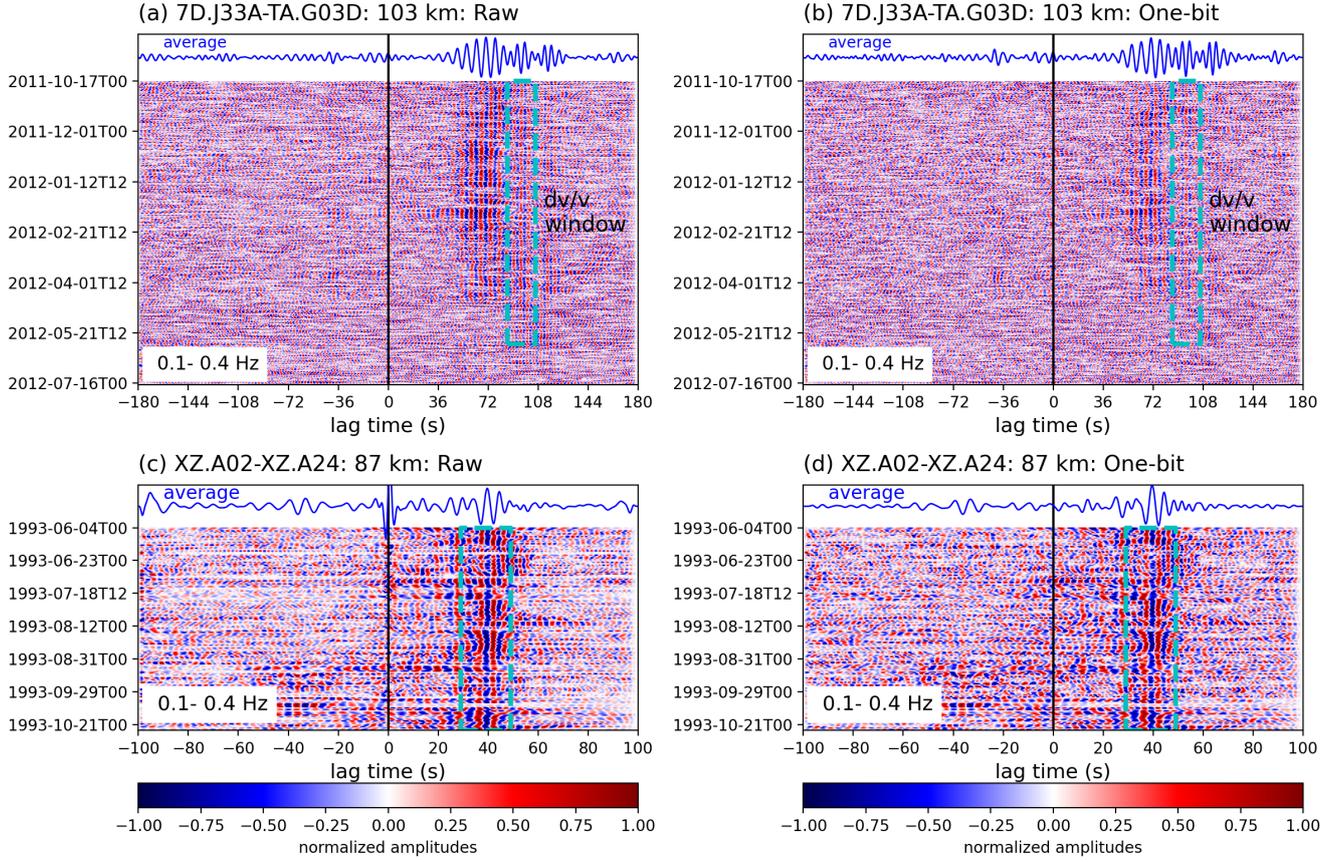
**Figure 1.** Seismic stations used in this study. The USArray Transportable Array and Cascadia Initiative Ocean Bottom Seismographs (red open triangles) form a composite dataset that is referred to as the “Amphibious” dataset. The 1993-1994 Cascadia broadband XZ linear array (blue dots) is referred to as the “XZ” dataset. Labeled stations are used as virtual sources and receivers in the examples in this paper.

69 the curvelet transform (Laurent Stehly et al. 2011) and singular value decomposition (Moreau et al. 2017), as these focus  
 70 specifically on short-term convergence alone. We assess the performance of the eight algorithms using six different metrics  
 71 relevant to specific research applications. Because the one-bit pre-processing is designed to reduce the influence of earthquake-  
 72 like transient signals and to improve the quality of individual NCFs (Bensen et al. 2007), we benchmark our tests using both  
 73 the raw and one-bit normalization pre-processing techniques. The development of new methods and computer codes and the  
 74 performance tests from this study aim to guide the community in choosing the appropriate stacking method for ambient-noise  
 75 seismology use cases, though they can also be generalized to process other time-series data.

## 76 2 AMBIENT NOISE CROSS-CORRELATIONS

77 This study uses the Pacific Northwest as a natural laboratory (Fig. 1). We gather data from 29 Cascadia Initiative Ocean  
 78 Bottom Seismographs (OBS) (network code: 7D; [https://doi.org/10.7914/SN/7D\\_2011](https://doi.org/10.7914/SN/7D_2011)), 15 US Transportable Array  
 79 stations (network code: TA; <https://doi.org/10.7914/SN/TA>), and 43 stations from the 1993-1994 Cascadia subduction  
 80 zone experiment (network code: XZ; Nabelek et al. 1993). We group the data into two datasets: 1) the composite dataset from  
 81 the Cascadia Initiative OBSs and onshore TA stations is referred to as the “Amphibious” dataset; 2) the data from the East-West  
 82 XZ linear array in northern Oregon is referred to as the “XZ” dataset. All data are publicly accessible from the seismic data  
 83 archive of the Incorporated Research Institutions for Seismology Data Management Center (IRIS DMC).

84 We use the *SeisGo* Python toolbox to download the continuous seismic waveforms and compute the NCFs (X. Yang et al.  
 85 2022a). The cross-correlation function in *SeisGo* was modified from *NoisePy* (Jiang and Marine A Denolle 2020). We download



**Figure 2.** Examples of ambient noise cross-correlation functions (NCFs) between (a-b) OBS station 7D.J33A and onshore station TA.G03D and (c-d) XZ linear array stations XZ.A02 and XZ.A24. The NCFs are filtered at 0.1-0.4 Hz. The left panels are NCFs computed with raw waveforms and the right panels are NCFs computed after applying one-bit time-domain normalization. The dashed cyan boxes mark the windows used for the analysis of the preservation of transient phase changes (Section 4.4) using (a-b) coda waves and (c-d) ballistic phases. On the top of each panel, we show the linear stack as arithmetic averages. The NCFs are color-coded by the normalized amplitudes (red is 1, blue is -1).

86 the vertical component of the continuous waveforms in 12-hour segments. We select data from 10/1/2011 to 7/31/2012 for the  
 87 Amphibious dataset and from 6/1/1993 to 5/31/1994 for the XZ dataset. We remove the instrument responses and convert  
 88 the waveforms to displacements, followed by down-sampling to 5 Hz. We compute the NCFs in 6-hour windows sliding  
 89 every 3 hours. The data is demeaned and detrended for each 6-hour segment. We attempt to remove transient signals in the  
 90 ambient noise that will contaminate the noise cross correlations by removing the windows with anomalous amplitudes. For  
 91 that, we calculate the maximum absolute raw noise amplitude of the segment and the standard deviation of the raw noise  
 92 amplitudes of all segments. We discard waveform segments with peak amplitudes greater than 10 times the standard deviation,  
 93 as implemented in *NoisePy*.

94 We construct two sets of cross-correlations using the raw waveforms (Viens et al. 2017) and waveforms normalized in the  
 95 time domain using the `sign` function (e.g., Bensen et al. 2007; Shen et al. 2012). We denote the two datasets as Raw NCFs and  
 96 One-bit NCFs, respectively. To avoid spectral leakage, the short 6-hour time windows are tapered using a Tukey window with  
 97 a cosine fraction of 0.05. We then apply a Fourier transform to the short-window segment and compute the cross-correlation in

98 the frequency domain using the following equation:

$$X = \mathcal{F}^{-1}(\mathcal{F}^*(d_s)\mathcal{F}(d_r)), \quad (1)$$

99 where  $X$  is the NCF between time series  $d_s$  (virtual source) and  $d_r$  (receiver),  $\mathcal{F}$  is the Fourier transform operator,  $\mathcal{F}^*$  stands  
100 for the complex conjugate of the Fourier transform, and  $\mathcal{F}^{-1}$  is the inverse Fourier transform operator.

101 We show a few examples of the computed NCFs (bandpass filtered at 0.1-0.4 Hz) in Fig. 2 for both pre-processing strate-  
102 gies. The asymmetry of the NCF is a known effect of noise source directionality (Stehly et al. 2006). The first-order observation  
103 is that the individual NCFs contain incoherent noise that may overwhelm the coherent signals. The NCFs from the XZ land sta-  
104 tion pair all show clear ballistic phases over the entire period range of this analysis (Fig. 2c-d). For the amphibious station pair  
105 7D.J33A-TA.G03D, clear ballistic phases are present between 50s and 100s for most of the NCFs between October 2011 and  
106 April 2012, for both Raw (Fig. 2a) and One-bit (Fig. 2b) NCFs. However, the ballistic phases are almost invisible for the NCFs  
107 after May 2012. These "noisy" NCFs may contaminate the linear stack of the NCFs. The simple time-domain representation in  
108 Fig. 2 only provides a qualitative visual assessment. We later quantify the performance using different stacking methods with  
109 multiple metrics.

### 110 3 STACKING METHODS

111 This section describes the algorithms beyond the arithmetic mean (or Linear stacking) for optimally stacking NCFs. Most  
112 of these methods are adapted from the published literature. All methods can be generalized as weighted stacking with various  
113 ways of computing the stacking weight, which could be either trace weight or sample weight. We express the weighted stacking  
114 scheme as:

$$\mathbf{b} = \sum_{i=1}^N w_i \mathbf{d}_i, \quad (2)$$

115 where  $\mathbf{b}$  is the final stack. For trace-weighted stacking,  $\mathbf{d}_i$  is the  $i^{th}$  NCF trace,  $w_i$  is the stacking weight for the  $i^{th}$  NCF trace  
116 satisfying  $\sum w_i = 1$ , and  $N$  is the total number of NCF traces. For sample-weighted stacking,  $\mathbf{d}_i$  is the  $i^{th}$  sample of the  
117 arithmetic average or linear stack of all NCF traces,  $w_i$  is the stacking weight for the  $i^{th}$  sample satisfying  $\sum w_i = 1$ , and  $N$  is  
118 the total number of samples in each NCF trace. Under the stacking formulation of Equation 2, Linear stacking is a special case  
119 of trace-weighted stacking where all traces have the same weight ( $w_i = 1$ ). In the methods described in this section, the Robust  
120 (Section 3.1), Selective (Section 3.2), and Cluster (Section 3.3) stacking methods are all trace-weighted stacking methods. The  
121 phase-weighted (Section 3.4), time-frequency phase-weighted (Section 3.5),  $N^{th}$ -root (Section 3.6), and adaptive covariance  
122 filter (Section 3.7) stacking methods are all sample-weighted stacking methods. In the following subsections, we describe the  
123 computation of the stacking weights for each method in detail.

124 **3.1 Robust stacking**

125 Pavlis and Vernon (2010) first introduced Robust stacking to improve the accuracy of picking phase arrival times in seismo-  
 126 grams from teleseismic earthquakes. We adapt this generic, iterative, weighted stacking method to process NCFs. The weight  
 127 in Robust stacking is based on waveform de-coherence and penalizes the NCF that deviates too much from a reference stack.  
 128 The weight  $w_i$  of the  $i^{th}$  NCF,  $\mathbf{d}_i$ , for the  $j^{th}$  iteration is calculated as (Pavlis and Vernon 2010):

$$w_i^j = \frac{|\mathbf{b}_j \cdot \mathbf{d}_i|}{\|\mathbf{d}_i\| \|\mathbf{r}_i\|}, \quad (3)$$

129 where  $\mathbf{b}_j$  is the reference stack of the  $j^{th}$  iteration,  $\| * \|$  is the L2-norm operator, and  $\mathbf{r}_i = \mathbf{b}_j - (\mathbf{b}_j \cdot \mathbf{d}_i)\mathbf{d}_i$  is a modified  
 130 residual quantifying the difference between the current reference stack  $\mathbf{b}_j$  and the  $i^{th}$  NCF scaled by the dot product of the  
 131 two time series. The weight  $w_i$  penalizes twice the data that does not resemble the reference stack. The first element is the dot  
 132 product between the NCF and the stack:  $\mathbf{b}_j \cdot \mathbf{d}_i / \|\mathbf{d}_i\|$ . The second is the modified residual  $r_i$ : if it is high, the  $1/\|r_i\|$  is small,  
 133 and  $w_i$  is low. The weights can be calculated over either the entire NCF or a specific time window that contains the seismic  
 134 phase of interest. For the examples in this paper, we compute the weights over the entire NCF, though our software package  
 135 allows the user to specify the time window. After computing the weights for all NCFs, we normalize them to their sum and use  
 136 them to produce the updated stack.

137 The initial reference stack  $\mathbf{b}_1$  is chosen as the median NCF, following the observation of Pavlis and Vernon (2010) that the  
 138 median is more representative of the concentration of data in the presence of outliers. In our implementation, the users may  
 139 specify another trace as the initial stack, such as the Linear stack. The iterative procedure stops when a convergence criterion  
 140 is satisfied. We adopt the criterion proposed by Pavlis and Vernon (2010):

$$\frac{|\mathbf{b}_j - \mathbf{b}_{j-1}|}{\|\mathbf{d}_j\| M} < \epsilon, \quad (4)$$

141 where  $M$  is the number of samples in each NCF time-series and  $\epsilon$  is a small number, with a default value of  $10^{-5}$ .

142 **3.2 Selective stacking**

143 In the presence of strong noise, it could be effective to stack only a subset of the NCF ensemble that exceeds a quality threshold  
 144 and to ignore the low-quality NCFs. This concept, called selective stacking, has been implemented in previous studies (e.g.,  
 145 Olivier et al. 2015; Thangraj and Pulliam 2021). The signal-to-noise ratio (SNR) or the correlation to the reference can be  
 146 used to evaluate the quality of each NCF. Olivier et al. (2015) used the SNR around the expected S-wave arrival time to  
 147 reconstruct S-waves in the stacked NCF. Liu et al. (2009) proposed the weighted stack of common-midpoint gather using  
 148 the local correlation within the moving window to improve the SNR and suppress the random noise in the stacked trace. To  
 149 enhance the coherence of the signal, we use a criterion based on the similarity, quantified as the Pearson correlation coefficient  
 150 in our implementation, between each NCF and the reference NCF. In our implementation, by default, the reference NCF is

151 initialized as the Linear stack of the entire ensemble (similar to Liu et al. 2009). As in Robust stacking, the user can specify  
 152 any trace, such as the median NCF, as the reference stack and the window used to estimate the similarity. Selective stacking  
 153 sets the weights of low-similarity NCFs to zero, computed as:

$$w_i = \begin{cases} 0, & \rho_{\mathbf{b}, \mathbf{d}_i} \leq \rho_t \\ 1, & \rho_{\mathbf{b}, \mathbf{d}_i} > \rho_t \end{cases} . \quad (5)$$

154 where  $\rho_{\mathbf{b}, \mathbf{d}_i}$  is the Pearson correlation coefficient between the individual trace and the reference NCF and  $\rho_t$  is the user-defined  
 155 threshold. Note that the criterion used in this study is equivalent to the global correlation described in Liu et al. (2009) rather  
 156 than the local correlation for the sake of simplicity in thresholding. A similarity threshold allows us to discriminate the set of  
 157 NCFs to keep or discard (weight is set to zero). We then compute the Linear stack over the subset of NCFs with a Pearson  
 158 correlation coefficient above the threshold and discard the NCFs below the threshold. Similar to robust stacking, we implement  
 159 the selective stacking method in an iterative scheme, with the same convergence criterion as in Equation 4. In our examples,  
 160 we use a correlation coefficient threshold of 0.

### 161 3.3 Cluster stacking

162 An alternative method to ranking waveforms according to a specific similarity metric is to group them into clusters and perform  
 163 the stack for each cluster. Viens and Iwata (2020) proposed the idea of clustering the NCFs using a dimensionality reduction  
 164 technique (principal component analysis), as exploited by Toghradjian et al. (2021). In our implementation, we use the  
 165 *Tslearn* Python toolkit (Tavenard et al. 2020) for k-means clustering of the NCF waveforms based on the Euclidean distance.  
 166 We impose two clusters to separate NCFs with higher quality from those with lower quality.

167 After clustering the NCFs into two clusters, the final stack  $\mathbf{b}$  is computed as a weighted stack of the two cluster centers

$$\mathbf{b} = \sum_{i=1,2} w_i C_i, \quad (6)$$

168 where  $C_i$  ( $i=1, 2$ ) are the centers (sample averages or linear stacks) of the two clusters and  $w_i$  ( $i=1, 2$ ) are the weights of the  
 169 cluster centers. The center stacking weights,  $w_i$  ( $i=1, 2$ ), are computed as

$$w_{i=1,2} = \begin{cases} \begin{cases} 0, & p_i < \max(p_1, p_2) \\ 1, & p_i \geq \max(p_1, p_2) \end{cases}, & cc < h \\ p_i / (p_1 + p_2), & cc \geq h \end{cases}, \quad (7)$$

170 where  $cc$  is the correlation coefficient between the two cluster centers  $C_1$  and  $C_2$ ,  $h$  is the similarity threshold specified by the  
 171 user, and  $p_i$  ( $i=1, 2$ ) is the relative peak amplitude of the cluster center, computed as the ratio of the maximum and root-mean-  
 172 square of the absolute amplitudes. The relative peak amplitude we use here is an equivalent measure to the signal-to-noise ratio  
 173 of the cluster center. In our examples,  $p_1$  and  $p_2$  are computed over the entire NCF. Our implementation also allows the user to  
 174 specify the window of interest to compute the maximum of the absolute amplitudes. According to Equation 7, the two centers

175 are weighted by the relative peak amplitude when their correlation coefficient exceeds the threshold ( $h=0.75$  for our examples).  
 176 Otherwise, we use the center with a higher peak amplitude as the final stack.

### 177 3.4 Phase-weighted stacking

178 Phase-weighted stacking (PWS) computes the weight for each trace by the coherency of the instantaneous phases (Schimmel  
 179 and Paulssen 1997). Our implementation of the PWS method follows the description in Schimmel and Paulssen (1997). Readers  
 180 are referred to Schimmel and Paulssen (1997) for detailed equations and procedures of the PWS method. The final stack is  
 181 constructed as a non-linear weighted stack where each sample is weighted by the instantaneous phase. The key parameter for  
 182 PWS is a harshness parameter that quantifies the fall-off of the weight of each NCF with decreasing similarity. We set the  
 183 harshness to 2, as in Schimmel and Paulssen (1997).

### 184 3.5 Time-frequency phase-weighted stacking

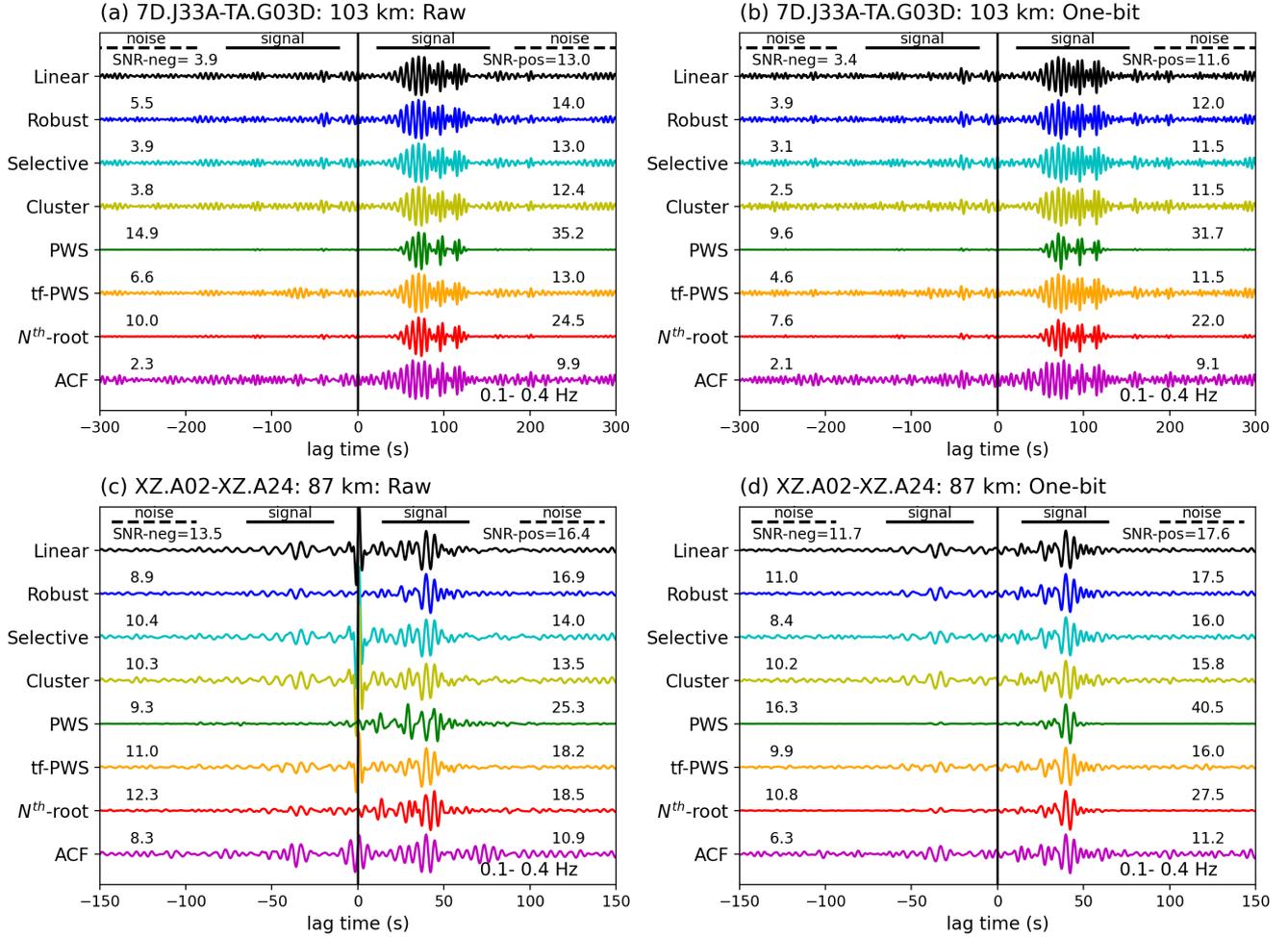
185 Schimmel and Gallart (2007) and Schimmel et al. (2011) proposed an improved phase-weighted stacking method that computes  
 186 the weight in both the time and frequency domains. This method, referred to as tf-PWS, projects each seismic trace into the  
 187 time-frequency domain through the Stockwell transform (S-transform; Stockwell et al. 1996). Baig et al. (2009) adapted the  
 188 stacking method based on a more efficient discrete orthogonal S-transform that is introduced by Stockwell (2007). The imple-  
 189 mentation of tf-PWS in this study follows the description by Schimmel et al. (2011) using the original S-transform (Equations  
 190 4-7 therein). Readers are referred to Schimmel and Gallart (2007) and Schimmel et al. (2011) for detailed formulation of  
 191 the tf-PWS stacking method. Similar to PWS, the tf-PWS is primarily controlled by a harshness parameter that determines  
 192 the sharpness of the transition between phase similarity and dissimilarity. We set the harshness to 2 for our examples, as in  
 193 Schimmel et al. (2011).

### 194 3.6 $N^{th}$ -root stacking

195  $N^{th}$ -root stacking method is commonly employed in array seismology (Kanasewich et al. 1973; Millet et al. 2019; Muirhead  
 196 1968; Rost and Thomas 2002; Rückemann 2012; Schimmel and Paulssen 1997). It is a nonlinear stacking method that takes  
 197 the  $N^{th}$ -root of the absolute amplitudes of each individual trace and sums them together. The summation is then raised to the  
 198 power of  $N$  to assign the sample weight. The polarity of each sample is recovered with a sign function of the summation. Our  
 199 implementation follows the description in Millet et al. (2019) (their equation 18) and can be summarized as:

$$\mathbf{b} = \text{sign}(\mathbf{r})|\mathbf{r}|^n, \quad (8)$$

200 where  $\mathbf{b}$  is the final stack,  $n$  is the specified order of root,  $\mathbf{r} = \frac{1}{N} \sum_{i=1}^N \text{sign}(\mathbf{d}_i)|\mathbf{d}_i|^{1/n}$ ,  $\mathbf{d}_i$  is the  $i^{th}$  NCF trace, and  $N$  is the  
 201 total number of NCF traces. We use the square root (i.e.,  $n=2$ ) in our examples.



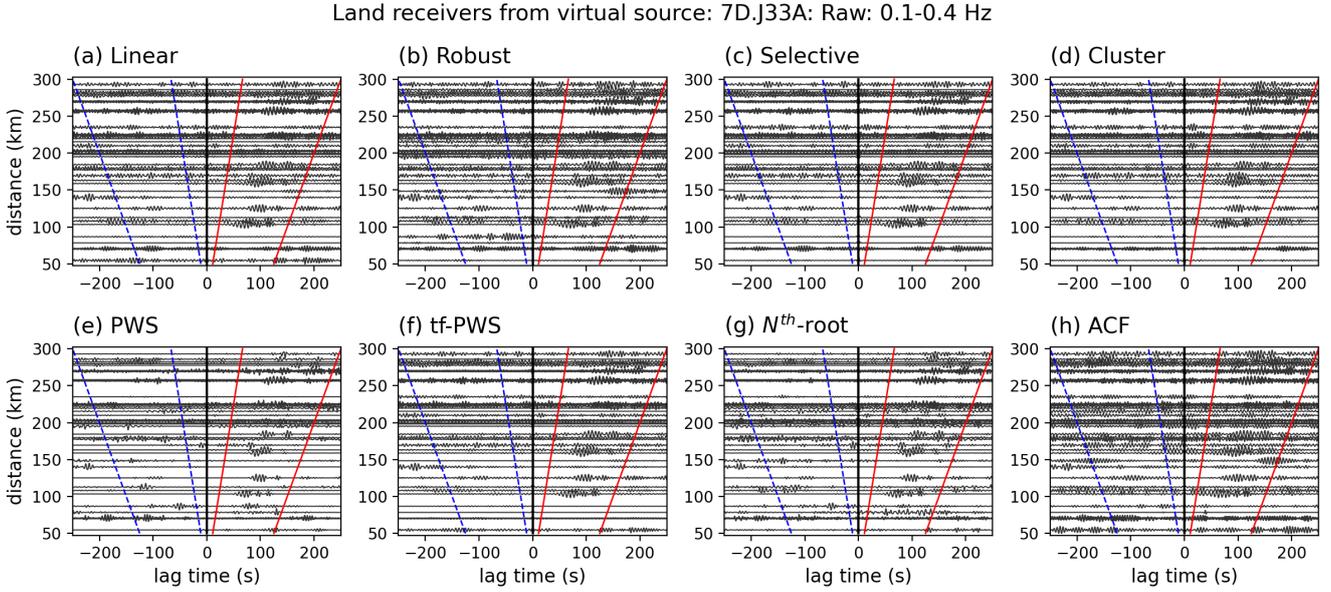
**Figure 3.** Examples of the stacked NCFs between station pairs (a-b) 7D.J33A-TA.G03D and (c-d) XZ.A02-XZ.A24, using different methods. The left panels are the stacking results for Raw NCFs and the right panels are the stacking results for One-bit NCFs. All NCFs are filtered at 0.1-0.4 Hz after stacking. The stacking algorithm is labeled on the left of each panel. The SNR in decibel (Equation 10) is indicated above each trace on each side of the correlations. The thick solid and dashed lines mark the starts and ends of the signal and noise windows, respectively.

### 202 3.7 Adaptive covariance filter stacking

203 Nakata et al. (2015) introduced an adaptive covariance filter (ACF) to suppress incoherent noise in seismic data based on  
 204 the adaptive polarization filter (Du et al. 2000; Samson and Olson 1981). We implement the ACF stacking method following  
 205 Nakata et al. (2015), which the readers are referred to for detailed formulations of the method. The final stack is the Linear  
 206 stack after applying the ACF. We use 1 as the harshness of the filter.

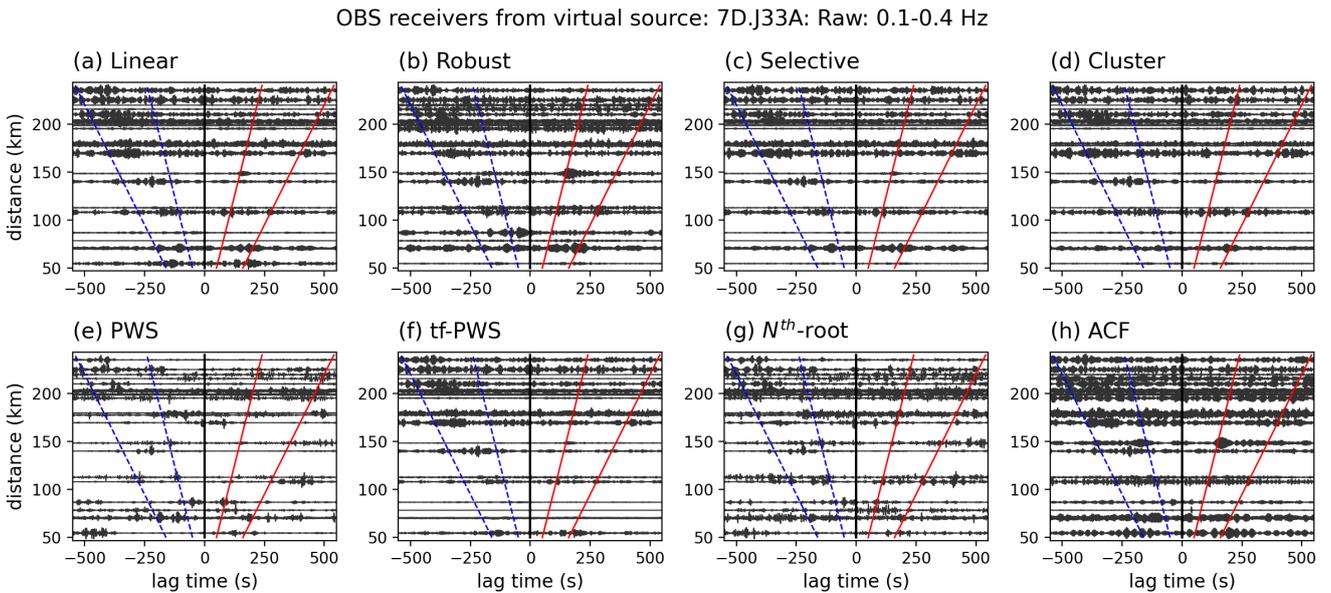
## 207 4 EVALUATION AND COMPARISON OF STACKING ALGORITHMS

208 We implement the stacking algorithms described in Section 3 as a standalone Python package *StackMaster* (X. Yang  
 209 et al. 2022b). The package is available as a repository on Python Package Index (PyPI). It can be installed with:  
 210 `pip install stackmaster`. In this paper, we install *StackMaster* with the *SeisGo* toolbox (X. Yang et al. 2022a) under

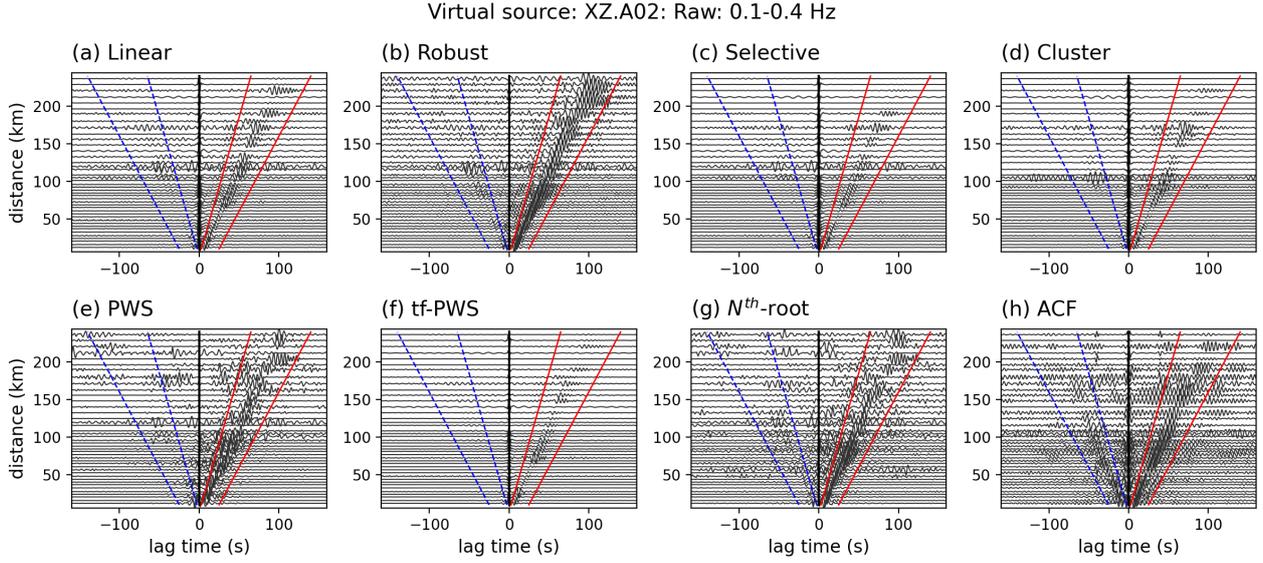


**Figure 4.** Stacked Raw NCFs of the Cascadia amphibious array from 7D.J33A to other land receivers using different stacking methods, filtered at 0.1-0.4 Hz. (a-h) The results using Linear, Robust, Selective, Cluster, PWS, tf-PWS,  $N^{th}$ -root, and ACF stacking methods, respectively. The red solid lines and the blue dashed lines outline the positive-lag signal window and the negative-lag signal window, respectively, used to compute the SNR in Fig. 7. The signal and noise windows are determined with the same method as in Fig. 3a-b. See Fig. 1 for station locations.

211 the same Anaconda environment. We apply the stacking techniques to the Amphibious and the XZ datasets. Fig. 3 shows the  
 212 stacking results for the two station pairs in Fig. 2. Figs 4-6 and S1-S3 in the supplement are the stacking results of all station  
 213 pairs from the virtual sources at 7D.J33A (Figs 4-5 and S1-S2) and at XZ.A02 (Figs 6 and S3).



**Figure 5.** Same as Fig. 4 but for NCFs from 7D.J33A to other OBS receivers. To contain the visually identified ballistic phases from these OBS station pairs, we use a different velocity range (0.5-1.0 km/s) here to predict the signal window of the weakly coherent signals. We extend the window for an additional 60 s after the latest predicted arrival. See Fig. 1 for locations of the OBS receivers.



**Figure 6.** Stacked Raw NCFs between the XZ linear array stations from XZ.A02 to other receivers, filtered at 0.1-0.4 Hz. (a-h) The results using Linear, Robust, Selective, Cluster, PWS, tf-PWS,  $N^{\text{th}}$ -root, and ACF stacking methods, respectively. The red solid lines and the blue dashed lines outline the positive signal window and the negative signal window, respectively, used to compute the SNR in Fig. 7. The signal and noise windows are determined with the same method as in Fig. 3c-d. See Fig. 1 for station locations.

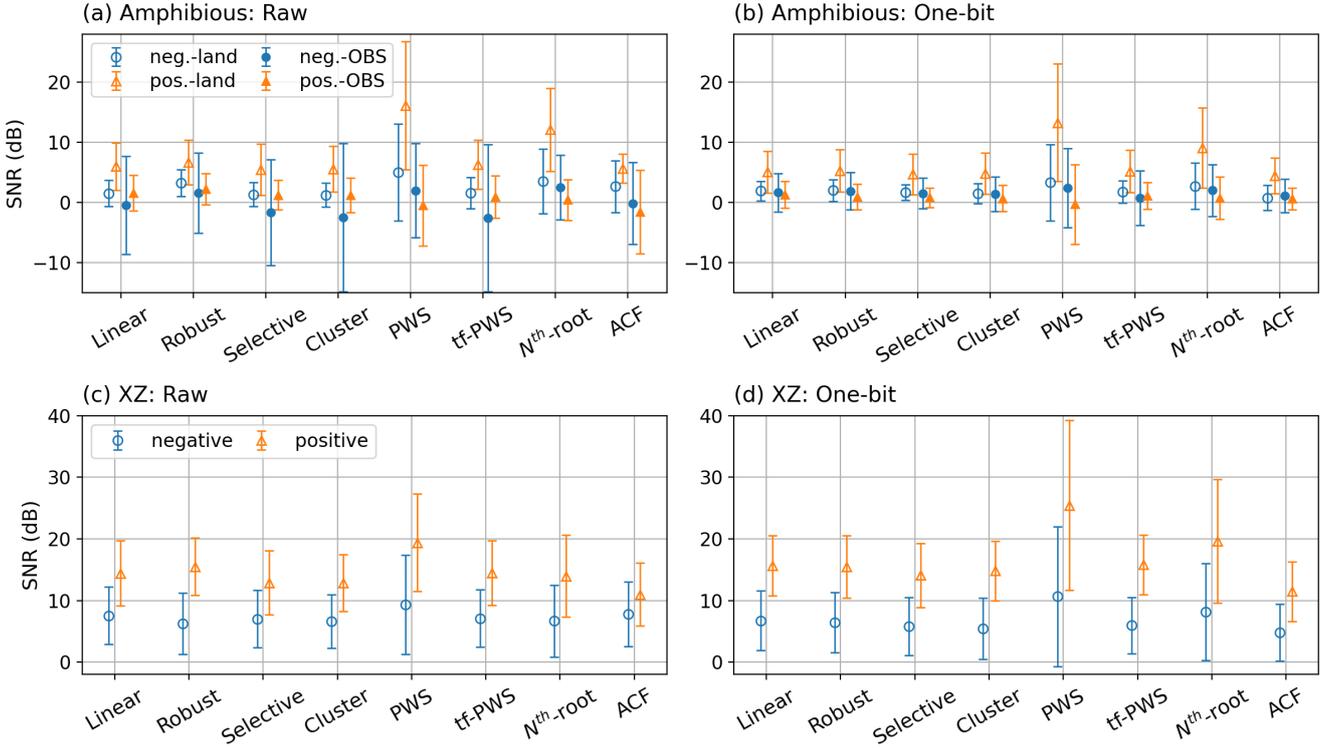
214 We then evaluate and compare the performance of these stacking methods. Recognizing that NCFs are used in multiple  
 215 applications (e.g., seismic velocity tomography, monitoring, and attenuation/ground motion analysis), we evaluate the per-  
 216 formance of the algorithm over a range of metrics: 1) signal-to-noise ratios, 2) surface wave dispersion, 3) convergence of  
 217 short-term stacks to the long-term stack, 4) transient phase changes, 5) peak amplitudes of ballistic phases, and 6) computa-  
 218 tional expense. We compare the methods below according to each metric. It is worth noting that there are multiple parameters  
 219 that can be tuned for each stacking method, though we only focus on the most commonly used or suggested parameters in this  
 220 study. In Section 5, we discuss the choice of stacking methods for different categories of applications using NCFs.

#### 221 4.1 Signal-to-noise ratios

222 We use the SNR of the ballistic phase as a proxy for the quality of the NCF stack. In this study, we define the SNR,  $R$ , as

$$R = \left[ \frac{\text{rms}(|A_{\text{signal}}|)}{\text{rms}(|A_{\text{noise}}|)} \right]^2, \quad (9)$$

223 where  $\text{rms}()$  is the root-mean-square operator,  $|A_{\text{signal}}|$  are the absolute amplitudes within the signal window, and  $|A_{\text{noise}}|$   
 224 are the absolute amplitudes within the noise window. For the NCFs from amphibious station pairs (Figs 3a-b, 4, and S1), the  
 225 signal window is defined by a fast wave traveling at 4.5 km/s, a slow wave traveling at 2 km/s, and we add 100 s to the end of  
 226 the window. For OBS station pairs (Figs 5 and S2), we use a velocity range of 0.5-1.0 km/s to predict the signal window and  
 227 add 60 s after the latest predicted arrival time. For the XZ dataset (Figs 3c-d, 6, and S3), the signal window is defined by waves  
 228 traveling between 2 km/s and 3.7 km/s, extending for an additional 20 s. For both datasets, the noise window has the same



**Figure 7.** Comparison between the mean signal-to-noise ratios (SNRs) for the NCFs shown in Figs 4-6 and S1-S3. (a-b) Mean SNRs for the Cascadia amphibious array Raw and One-bit NCFs, respectively. The SNRs for the land (open circles and triangles) and OBS (dots and filled triangles) stations are plotted separately. (c-d) Results for the XZ linear array NCFs from Raw and One-bit NCFs, respectively. The error bars show the standard deviations of the SNRs.

229 length as the signal window with an offset of 30 s after the end of the signal window. Considering the relatively large dynamic  
 230 range of the computed SNRs, we convert the ratios to decibel scales for all examples in this paper to assist the comparison and  
 231 visualization, with

$$SNR = 10 \log_{10} R. \quad (10)$$

232 It is worth noting that the SNR is unitless and the conversion in Equation (10) is mainly for scaling.

233 We observe notable variations in the SNRs of the ballistic phases retrieved using different stacking methods. From the  
 234 single-pair examples (Fig. 3), the ballistic phases are most prominent on the positive lags from all stacking results, with  
 235 relatively weaker phases on the negative lags, shown as lower SNRs overall. For the Cascadia amphibious station pair, the  
 236 SNRs range from 9.9 to 35.2 for the Raw NCFs and 9.1-31.7 for the One-bit NCFs (Fig. 3a-b). For the XZ station pair, the  
 237 SNRs range from 10.9 to 25.3 for the Raw NCFs and 11.2-40.5 for the One-bit NCFs (Fig. 3c-d). For all datasets, the highest  
 238 SNRs are achieved with the PWS method, while the ACF method produces the lowest SNRs. The stacking results using the  
 239  $N^{th}$ -root method also show relatively high SNRs. The SNRs of other stacking results are at a comparable level.

240 The stacking results of all station pairs from the same virtual source provide a more holistic comparison of the performance  
 241 of different methods (Figs 4-6 and S1-S3). We use the mean SNRs across all station pairs to quantify the comparison of stacks

242 with different methods (Fig. 7). From the visual inspection of the move-out plots (time-lags vs. inter-station distances), the  
 243 stacks of Raw (Figs 4 and 6) and One-bit (Figs S1 and S3) NCFs have comparable quality overall for both the Amphibious and  
 244 the XZ datasets. This is also evident from the comparable mean SNR values of the two pre-processing methods (Fig. 7). For  
 245 the Cascadia Amphibious dataset, most of the NCFs from the OBS receivers are relatively noisy (Figs 5 and S2), with mean  
 246 SNRs lower than those from the onshore receivers (Fig. 7a-b). This may result from the contamination of tilt and compliance  
 247 noise at most OBS stations, a well-known problem in offshore data (Tian and Ritzwoller 2017). Most of the stacked XZ NCFs  
 248 show clear ballistic phases (Figs 6 and S3), with much higher mean SNRs than those of the Amphibious dataset (Fig. 7). In  
 249 all examples with land receivers, the ballistic phases are dominantly visible at positive lag times, representing surface waves  
 250 propagating away from the virtual sources, which we focus on for the following description. For all four datasets (land receivers  
 251 only for the Amphibious NCFs), the PWS method produces the highest SNRs, while the standard deviation of the SNRs is also  
 252 the largest. For the Cascadia Amphibious NCFs (Fig. 7a-b),  $N^{th}$ -root stacking yields the second highest SNRs, while the SNRs  
 253 of other stacking results are at a comparable level of 0-10 for both the Raw and One-bit NCFs. For the XZ NCFs (Fig. 7c-d),  
 254 the lowest SNRs are observed with ACF stacking, though the ballistic phases are still clearly retrieved (Figs 6h and S3h).

## 255 4.2 Surface wave dispersion

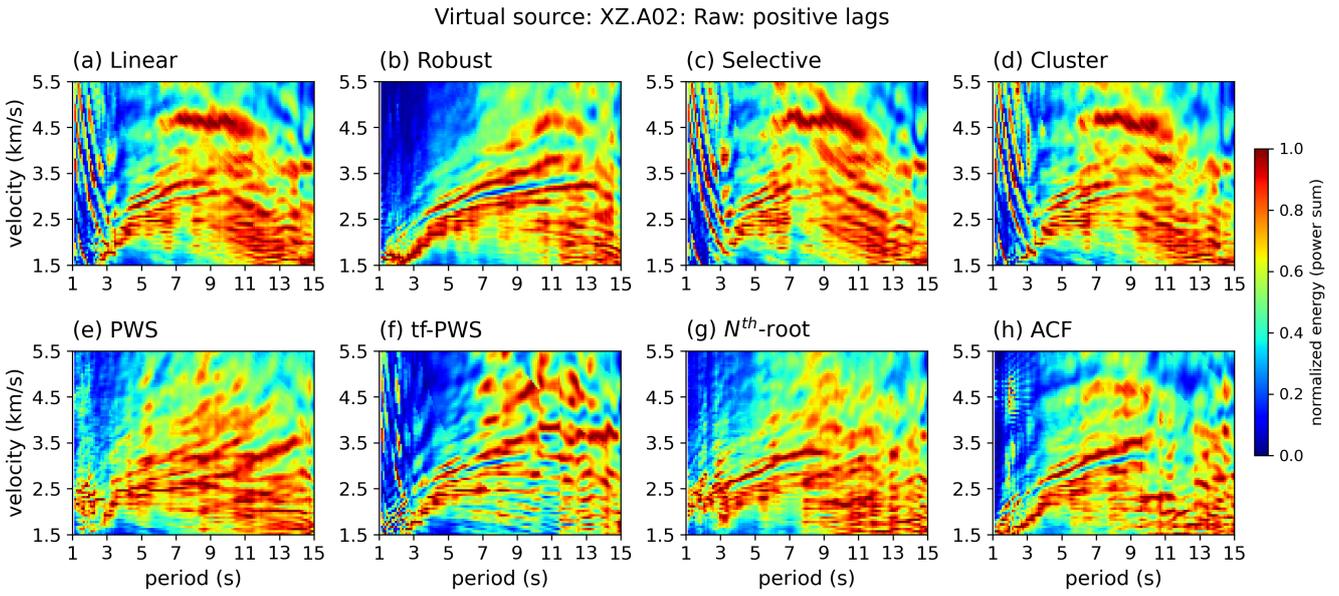
256 Surface waves are dispersive, which means that their wavespeed depends on the frequency of the wave. Lower frequency  
 257 (longer period) surface waves generally travel faster than higher frequency (shorter period) waves and are more sensitive to  
 258 greater depths. This frequency-depth characteristic makes surface waves a popular choice for elastic and anelastic seismic  
 259 tomography of the subsurface. Preserving the surface wave dispersion in the stacked NCFs is, therefore, one of the critical  
 260 metrics to evaluate the performance of different stacking methods. We assess this performance by extracting and comparing  
 261 the phase-velocity dispersion images. We use the Raw and One-bit NCFs from the XZ linear array between the virtual source  
 262 at XZ.A02 and all other receivers (Fig. 6) to evaluate this metric.

263 We follow the phase-shift dispersion analysis procedure described in Park et al. (1998, 1999) and Ryden et al. (2004).  
 264 We implement the procedure in the time domain through narrow-band filters. We narrow bandpass the seismograms using a  
 265 Butterworth filter progressively between 1 and 15 seconds period, with a moving period band of 2 seconds and a step size of  
 266 0.1 s. We then shift the seismogram with a phase shift of  $r/v$ , where  $r$  is the inter-station distance and  $v$  is the phase velocity  
 267 that varies between 1.5 to 5.5 km/s, with a step of 0.05 km/s. We trim the data over an adaptive window length that scales with  
 268 the central period, computed as

$$L_i = a_i T_i, \quad (11)$$

269 where  $L_i$  is the window length for the  $i^{th}$  period  $T_i$ .  $a_i$  is the scaling factor, which is determined by

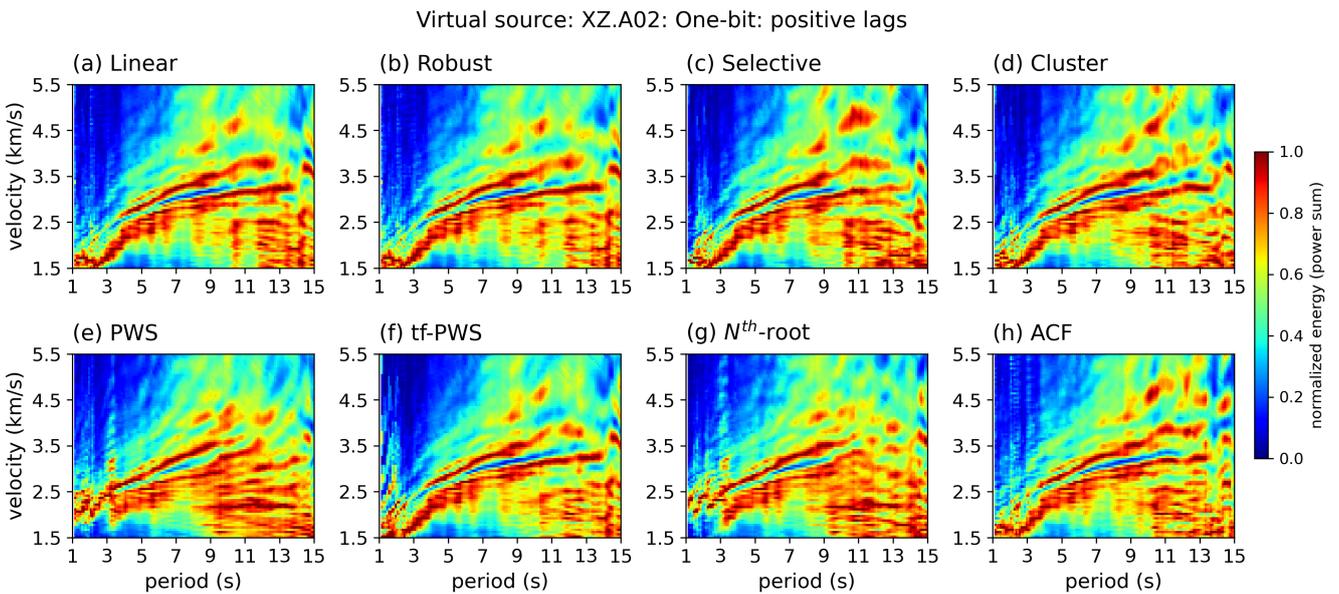
$$a_i = a_{min} + (i - 1) \frac{a_{max} - a_{min}}{N_T}, \quad (12)$$



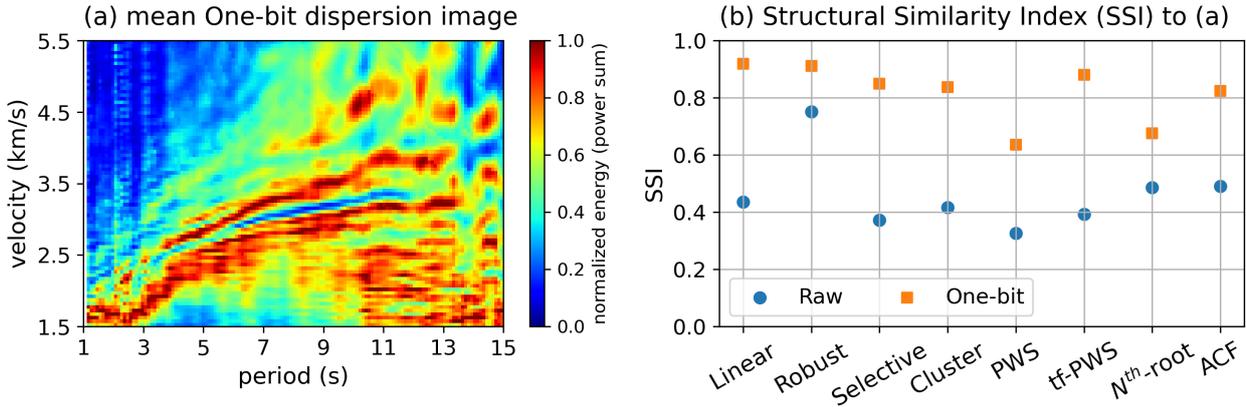
**Figure 8.** Dispersion images extracted from the Raw NCFs between the virtual source at XZ.A02 and other receivers using the time-domain phase-shift method through multichannel analysis of surface waves (e.g., Park et al. 1998, 1999; Ryden et al. 2004). (a-h) Results from the stacks using Linear, Robust, Selective, Cluster, PWS, tf-PWS,  $N^{th}$ -root, and ACF stacking methods, respectively. The color scale shows the power sum normalized at each velocity value. The NCFs are shown in Fig. 6

270 where  $a_{min}$  and  $a_{max}$  are the minimum and maximum of the scaling range and  $N_T$  is the number of period steps. For our  
 271 examples,  $a_{min} = 1$  and  $a_{max} = 2$ . Finally, to extract the dispersion image, we calculate the energy (sum of squared amplitude)  
 272 of the windowed, filtered, shifted, and stacked seismograms. The images are shown in Figs 8 and 9.

273 We apply this procedure to all station pairs with the common virtual source XZ.A02, with only results from the positive



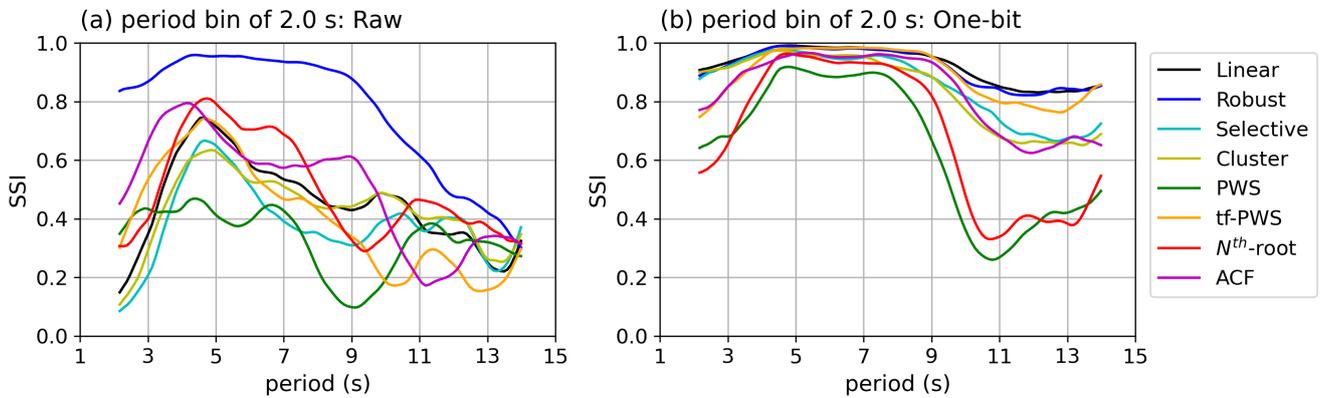
**Figure 9.** Same as Fig. 8 but for stacked One-bit NCFs as shown in Fig. S3 in the supplement.



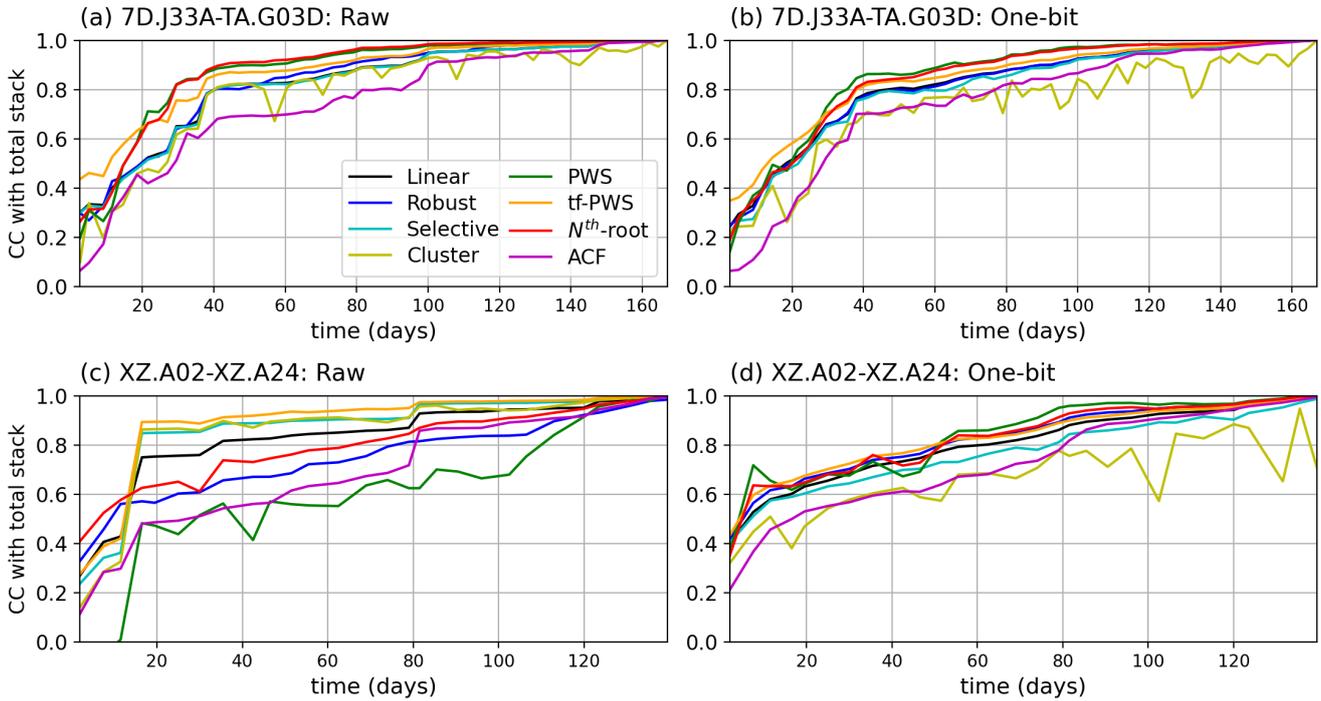
**Figure 10.** Comparison of the dispersion images in Figs 8 and 9. (a) The average dispersion image of the One-bit NCF stacks in Fig. 9, which is used as the reference for the comparison. (b) Structural Similarity Index (SSI) between individual dispersion images for Raw (dots) and One-bit (squares) NCF stacks and the reference dispersion image as in (a). The dispersion images are shown in Figs 8 and 9.

274 lags of the NCFs being shown here. We only analyze the results from station pairs with inter-station distances of at least 1.5  
 275 times the wavelength for each velocity-period pair to remain in the far-field regime.

276 The dispersion images from the One-bit stacks are largely similar to each other (Fig. 9). This contrasts with the great  
 277 variability of the dispersion images from the Raw NCF stacks (Fig. 8). We use the average dispersion image of the One-bit  
 278 results (Fig. 10a) as a reference. We compute the Structural Similarity Index (SSI; Z. Wang et al. 2004) between the reference  
 279 (Fig. 10a) and individual dispersion images from the NCF stacks using different methods (Figs 8 and 9). The SSI is widely  
 280 used in the analysis of image degradation or alteration, with 1 meaning the two images are identical and 0 meaning they are  
 281 completely different. The SSI results over the entire period range of 1-15 s for both the Raw and One-bit dispersion images are  
 282 shown in Fig. 10b. To examine the performance of different stacking methods at different period bands, we also compute the  
 283 frequency-dependent SSI, as shown in Fig. 11.



**Figure 11.** Frequency-dependent comparison of the dispersion images with the average dispersion image of the One-bit NCF stacks (Fig. 10a). (a) Structural Similarity Index (SSI) between individual dispersion images for Raw NCF stacks with a period bin of 2 s and a step of 0.1 s. The x-axis shows the central period of each bin. (b) Same as (a) but for One-bit NCF stacks. The dispersion images are shown in Figs 8 and 9.



**Figure 12.** Convergence to long-term stacks with the increasing number of NCFs, shown as the equivalent time span of NCFs in days. (a-b) Correlation coefficients (CC) between the progressive stacking results and the stacks over the entire time period for Raw and One-bit NCFs between station pair 7D.J33A-TA.G03D. The pre-stack NCFs are shown in Fig. 2a-b. We only use NCFs before 4/1/2012 for the convergence analysis to exclude the much noisier data in later dates. All stacks are filtered at 0.1-0.4 Hz. (c-d) Same as (a) and (b) but for the XZ station pair XZ.A02-XZ.A24. The pre-stack NCFs are shown in Fig. 2c-d. We use all NCFs for this station pair.

284 The reference dispersion image (Fig. 10a) resembles major features of the One-bit dispersion images using different  
 285 stacking methods (Fig. 9). Over the entire period range of 1-15 s, the dispersion images using the PWS and  $N^{th}$ -root  
 286 for One-bit NCFs differ the most from the reference, with SSI below 0.8 (Fig. 10b). All other stacking methods show higher  
 287 SSI values. In contrast with the One-bit results, most of the dispersion images for the Raw NCFs possess relatively lower SSI  
 288 values ( $< 0.6$ ), except for the Robust stacking method, which shows a SSI of close to 0.8. The frequency-dependent results  
 289 (Fig. 11) show that all One-bit NCF stacks (Fig. 11b) and the Robust stack of the Raw NCFs (Fig. 11a) retrieve the most  
 290 consistent dispersion images at the period range of 4-9 s. Outside this period range, the SSI values for the PWS and  $N^{th}$ -root  
 291 stacks decrease dramatically. All stacking results of Raw NCFs, except for the PWS result, show SSI values of  $> 0.6$  in a  
 292 narrow band of 3-6 s (Fig. 11a). In summary, the Robust stacking method preserves the dispersion information the best for the  
 293 Raw NCFs, with a dispersion image closest to the average of One-bit NCF stacks. For the One-bit NCFs, the Linear, Robust  
 294 and tf-PWS stacks perform comparably well in preserving the dispersion information over the entire examined period range  
 295 from 1 to 15 s.

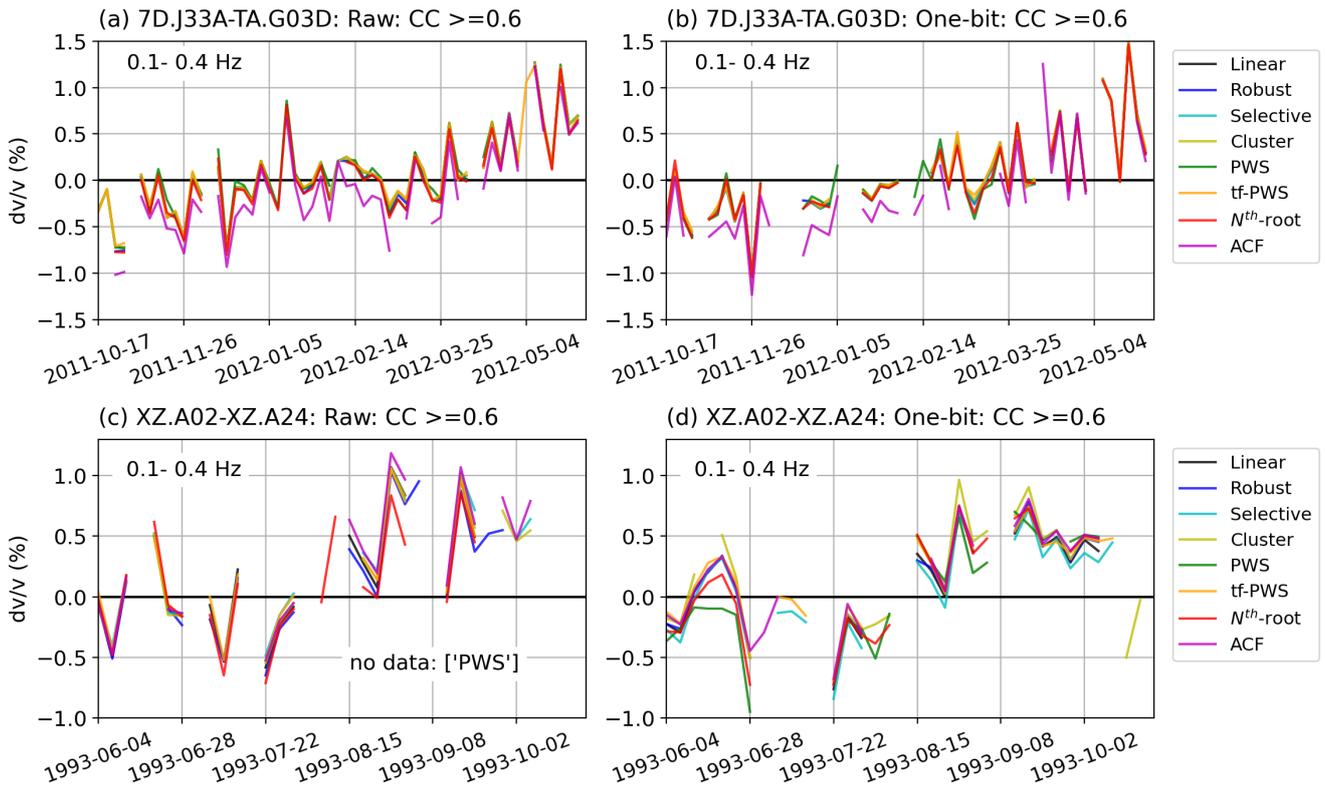
### 296 4.3 Convergence of short-term stacks to the long-term stack

297 In measuring the temporal changes associated with the elastic properties of the crust, we often stack a subset of the short-term  
 298 NCFs over an intermediate time period (e.g., F. Brenguier et al. 2008; Clements and Marine A Denolle 2018; Donaldson et al.  
 299 2019; Hadziioannou et al. 2011; Olivier et al. 2019; Seats et al. 2012; Yuan et al. 2021). The time needed to reach convergence  
 300 limits the temporal resolution of the monitoring of the change in elastic properties. Here, we quantify the *rate of convergence*  
 301 as the time duration of NCFs needed to achieve a certain threshold of the correlation coefficient between the stack of the subset  
 302 NCFs and the reference stack of NCFs over the entire period. We compute the correlation coefficient between the reference  
 303 stack and the stack of a progressively growing subset of NCFs ordered by date and time with an increment of 5 NCFs (Fig. 12).

304 The rate of convergence varies among methods (Fig. 12). Overall, the PWS, tf-PWS, and  $N^{th}$ -root stacking results have  
 305 the fastest convergence to the reference stack (Fig. 12a, b, and d), except for the Raw NCFs from the XZ station pair (Fig.  
 306 12c) where the PWS method converges the slowest. The ACF stacking result converges the slowest for the Raw NCFs of the  
 307 Cascadia amphibious station pair (Fig. 12a). The Cluster stacking method converges the slowest for the One-bit NCFs from  
 308 both station pairs (Fig. 12b and d), though it shows a fast convergence rate for the Raw NCFs of the XZ station par (Fig. 12c).  
 309 The strong fluctuation of the correlation coefficient using Cluster stacking may be due to the fact that the k-means clustering  
 310 method involves some random processes in assigning the clusters. Most stacking results achieve high ( $\geq 0.7$ ) correlation  
 311 coefficients with more than about 35 days (Fig. 12a-b). For the XZ NCFs to achieve a similar correlation coefficient, it takes  
 312 about 50 days (Fig. 12c-d). From the results shown here, the rate of convergence depends strongly on the specific dataset and  
 313 the quality of individual short-term NCFs.

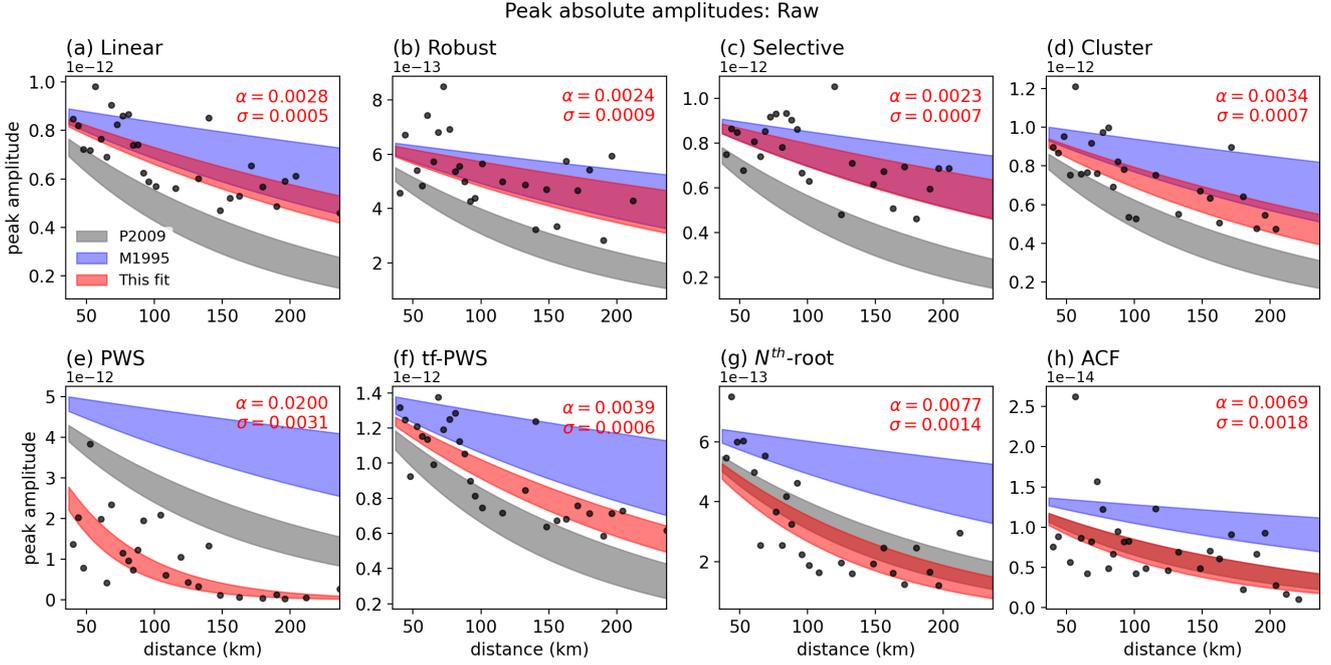
### 314 4.4 Transient phase changes

315 Seismic monitoring using ambient noise interferometry relies on the phase difference of seismic waves measured at different  
 316 lag times (e.g., F. Brenguier et al. 2008; Clements and Marine A Denolle 2018; Donaldson et al. 2019; Hadziioannou et al.  
 317 2011; Olivier et al. 2019; Seats et al. 2012; Yuan et al. 2021). We analyze how these phase changes are preserved with different  
 318 stacking methods by estimating the velocity changes ( $dv/v$ ) over time. We utilize the trace stretching method (e.g., Florent  
 319 Brenguier et al. 2008; Lobkis and Weaver 2003; A. Obermann et al. 2014; Yuan et al. 2021) to measure the  $dv/v$  between the  
 320 two example station pairs: 7D.J33A-TA.G03D and XZ.A02-XZ.A24 (Fig. 13). The trace stretching method estimates  $dv/v$  by  
 321 maximizing the correlation coefficient between the individual NCF coda with the reference coda through linearly stretching  
 322 or squeezing the waveform within the specified time window. The Python function for trace stretching is built in the *SeisGo*  
 323 interface (X. Yang et al. 2022a). For all results shown in Fig. 13, we measure the velocity changes in the frequency range of  
 324 0.1-0.4 Hz. For all datasets, we use a sub-stacking window length of 96 hours (4 days). The measuring windows are 86-106 s  
 325 for 7D.J33A-TA.G03D to capture the coda waves and 29-49 s for XZ.A02-XZ.A24 containing the ballistic phases. The  $dv/v$   
 326 measuring windows for both datasets are marked in Fig. 2.

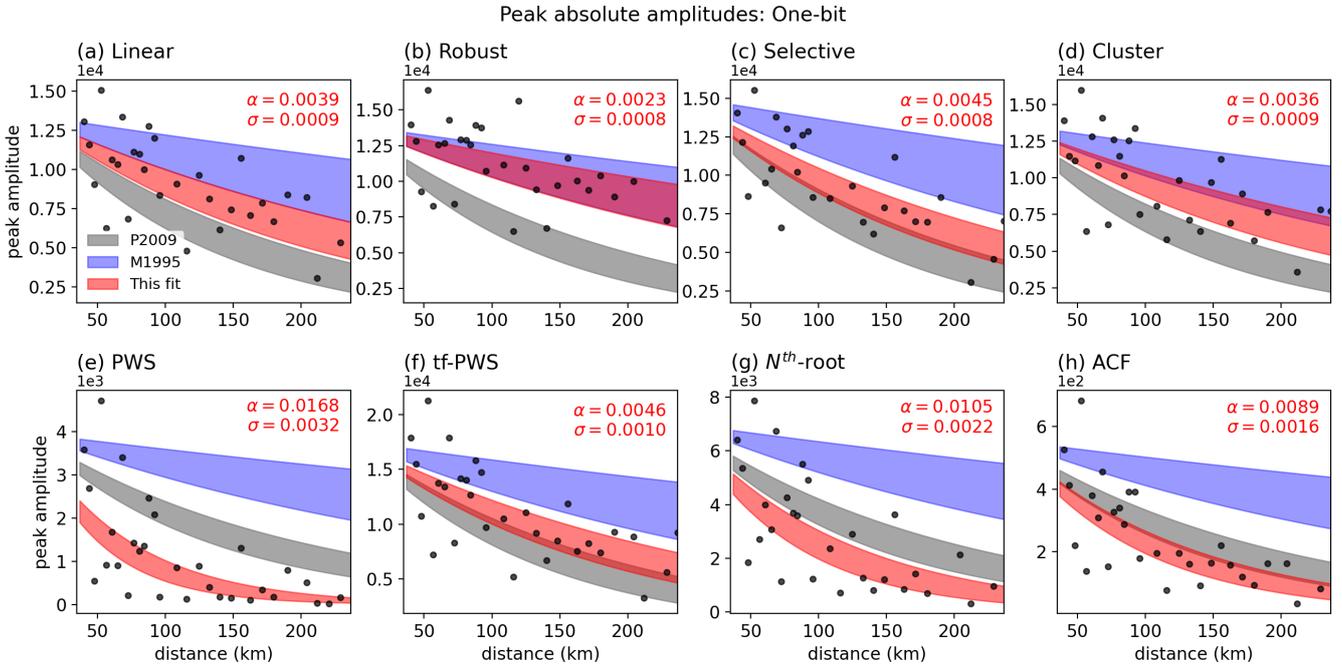


**Figure 13.** Transient velocity changes ( $dv/v$ ) using the trace stretching method measured from NCFs from (a) 7D.J33A-TA.G03D and (b) XZ.A02-XZ.A24. The pre-stack short-term NCFs and the measuring windows are shown in Fig. 2. We use coda waves for the amphibious station pair (7D.J33A-TA.G03D) and ballistic phases for the XZ station pair (XZ.A02-XZ.A24). The coda waves for the XZ station pair (both Raw and One-bit NCFs) are not coherent and produce unstable  $dv/v$  measurements, regardless of the stacking method used. For 7D.J33A-TA.G03D, we only analyze the NCFs before 6/2/2012, during which we have clear coda phases on most of the NCFs. We sub-stack the NCFs over 96 hours (4 days) for all station pairs. We only plot  $dv/v$  results with the post-stretching correlation coefficient (CC) of  $\geq 0.6$ .

327 For each station pair, different stacking methods produce very similar patterns of changes in  $dv/v$  over the observational  
 328 periods (Fig. 13). An exception is the  $dv/v$  measurements from the PWS stacking result of the Raw XZ NCFs, with stronger  
 329 variations and much lower after-stretching correlation coefficient compared to other stacking results. After applying a threshold  
 330 of  $geq$  0.6 for the post-stretching correlation coefficient in plotting Fig. 13, there is no PWS measurement left. For 7D.J33A-  
 331 TA.G03D, a general increase in seismic velocity from -0.5% to 0.5% is observed from both Raw and One-bit NCFs using all  
 332 stacking methods (Fig. 13a-b). For XZ.A02-XZ.A24, the  $dv/v$  fluctuates between -0.5% and 0.5% from June to July of 1993  
 333 (Fig. 13c-d). From August 1993 to the end of the observational period, the  $dv/v$  varies between 0% and 1% (Fig. 13c-d). While  
 334 we do not intend to interpret these  $dv/v$  measurements, we note the great similarity of the measurements across methods. All  
 335 stacking methods show comparable results in preserving the phase differences for coda waves from both Raw and One-bit  
 336 NCFs and the ballistic phases from One-bit NCFs. The PWS method fails with this metric for ballistic phases from the XZ  
 337 Raw NCFs.



**Figure 14.** Peak absolute amplitudes of the positive lags of the XZ Raw NCFs within the predicted ballistic arrival windows computed using a velocity range of 2-3.7 km/s and corrected by  $\sqrt{D}$ ,  $D$  is the inter-station distance. In each panel, we only show the attenuation parameter,  $\alpha$ , and its standard deviation,  $\sigma$ . The exponential fit from this study is shown as the red shaded area. For reference, we also show the amplitude decay estimated based on the attenuation parameters from Prieto et al. (2009) (P2009;  $\alpha=0.0064\pm 0.0013$ ; gray shaded area) and Mitchell (1995) (M1995;  $\alpha=0.002\pm 0.001$ ; blue shaded area). See Fig. 6 for the moveout plots of the stacked NCFs.



**Figure 15.** Same as Fig. 14 but for measurements from the XZ One-bit NCFs. See Fig. S3 in the supplement for the moveout plots of the stacked NCFs.

338 **4.5 Peak amplitudes of ballistic phases**

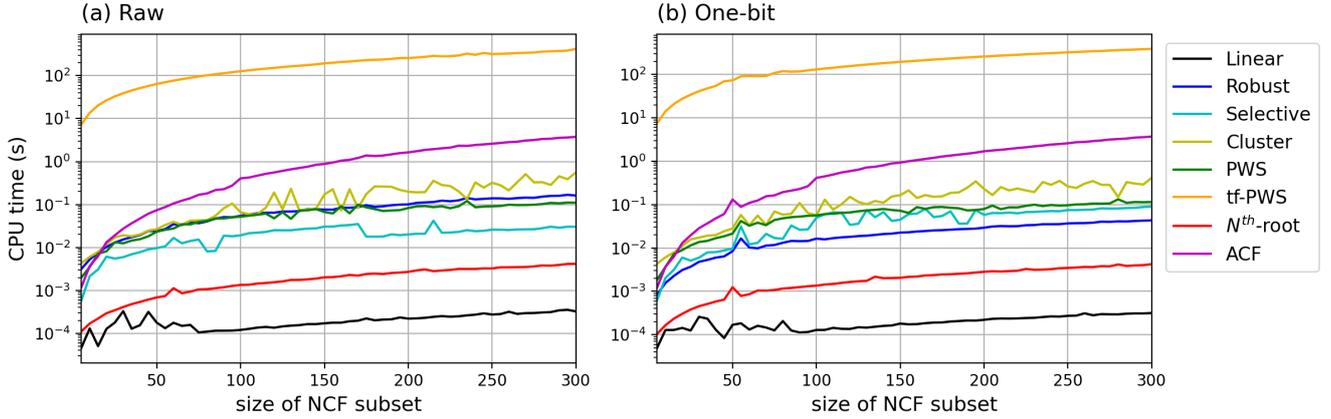
339 Important information about the Earth's anelastic structure can be retrieved from the relative amplitudes of NCFs (Prieto et al.  
 340 2009). Here, we focus on the amplitude decay with distance and ignore the spatial variations in relative amplitudes that are  
 341 subject to additional uncertainties. The NCFs chosen in this example are the same as in Fig 6 and supplementary Fig S3,  
 342 filtered at 0.1-0.4 Hz. The NCFs at each station pair are stacked over the entire duration of data availability. We then measure  
 343 the peak absolute amplitudes of the predicted ballistic waves for each station pair NCF stack within the time windows computed  
 344 with a velocity range of 2-3.7 km/s (Figs 6 and S3). The XZ broadband network is an East-West trending linear array in central  
 345 Oregon, United States (Fig. 1). It is located at the active Cascadia convergent margin, spanning from the Cascadia Volcanic Arc  
 346 in the East to the coastal mountains in the West. Considering that noise is dominantly generated by the oceanic microseisms  
 347 in this frequency range (e.g., Webb 1998; Y. Yang and Ritzwoller 2008), the XZ linear array provides an appropriate dataset  
 348 for analyzing the attenuation of surface waves extracted from NCFs, minimizing the azimuthal dependence of noise sources.  
 349 In this work, we only aim to compare the stability of the relative amplitude information with different stacking methods and  
 350 do not intend to advocate for an estimate of attenuation, which might still depend on the distribution of noise sources (Laurent  
 351 Stehly and Boué 2017). The microseismic noise is generated by the ocean and dominantly propagates eastward. Therefore,  
 352 XZ.A02 is an appropriate choice for a virtual source (Fig. 1). We only measure the attenuation from the positive lags of the  
 353 NCFs.

354 Assuming that the main signals of the NCF are fundamental-mode surface waves, the maximum absolute amplitudes of  
 355 the stacked NCFs decay with distance following the relation:

$$A(D) = A_0/\sqrt{D} \exp(-\alpha D), \quad (13)$$

356 where  $D$  is the inter-station distance,  $A_0$  is a reference amplitude at the virtual source,  $\alpha$  is a measure of "attenuation" that  
 357 could be attributed to intrinsic and scattering attenuation that further reduces the ground motion. To fit  $\alpha$ , we correct for  
 358 the geometrical spreading by scaling the amplitudes with a factor of  $\sqrt{D}$ . The peak absolute amplitudes are then fit to an  
 359 exponential function  $y = e^{-\alpha x}$ . We estimate the best fit through least square linear regression of the peak amplitudes in a  
 360 natural logarithmic space using the following steps: 1) calculate the natural log peak absolute amplitudes, 2) fit all data points  
 361 using a least square linear regression (`scipy.stats.linregress`), 3) correct the data with the best fit model and measure  
 362 misfit, 4) compute the mean and standard deviation of the misfit, 5) remove the outliers (data points that are more than one  
 363 standard deviation away from the mean), and 6) use the remaining subset of the data to repeat step-2 to get the final linear fit  
 364 parameters. The slope parameter in the linear regression from Step-2 is the attenuation factor  $\alpha$ . The error in slope estimate  
 365 given by `scipy.stats.linregress` is then used as the uncertainty of  $\alpha$ , as shown in Figs 14 and 15.

366 We only use subsets of the NCFs in Figs 6 and S3 that have inter-station distances between 37 km, which is the wavelength  
 367 of a 0.1 Hz wave traveling at a velocity of 3.7 km/s, and 240 km. The exponential fit and the parameters the uncertainties are  
 368 shown as the red shaded areas in Figs 14 and 15. For comparison, we also plot the independent attenuation measurements



**Figure 16.** Computing times spent on stacking as a function of the number of NCFs to stack in a 5-step increment for (a) Raw and (b) One-bit NCFs from station pair 7D.J33A-TA.G03D.

369 from Prieto et al. (2009) ( $\alpha=0.0064\pm 0.0013$ ), who used spectral methods to measure attenuation in the Los Angeles basin  
 370 in southern California using ambient noise NCF filtered at 0.2 Hz, and Mitchell (1995) ( $\alpha=0.002\pm 0.001$ ) for active tectonic  
 371 regions measured at 0.1-0.2 Hz using a global compilation of earthquake surface waves.

372 The decay coefficient  $\alpha$  can be measured with all methods and for all pre-processing techniques. However, there is great  
 373 variability in the model parameter among the methods (0.0023-0.02 for Raw NCFs and 0.0023-0.0168 for One-bit NCFs; Figs  
 374 14-15). For the Raw NCFs (Fig. 14), the attenuation parameters measured from the stacking results using Linear, Robust,  
 375 Selective, and Cluster methods are similar to the values by Mitchell (1995). The coefficients using the  $N^{th}$ -root and ACF  
 376 methods are comparable to that found by Prieto et al. (2009). The coefficient from the tf-PWS method falls in-between the  
 377 values provided by Mitchell (1995) and Prieto et al. (2009). For the estimates from One-bit NCFs (Fig. 15), the result using  
 378 the Robust method overlaps the most with the value proposed by Mitchell (1995). The Linear, Selective, Cluster, and tf-PWS  
 379 stacking results all fall in-between the values by Mitchell (1995) and Prieto et al. (2009). The estimates of  $\alpha$  from the  $N^{th}$ -root  
 380 and ACF stacks are similar to that used by Prieto et al. (2009). Compared to the attenuation measurements from the Raw NCFs,  
 381 the attenuation measurements from the One-bit NCFs seem to be more sensitive to the choice of stacking methods, shown as  
 382 larger variations among different methods. For both datasets, the PWS method tends to overestimate the attenuation factors,  $\alpha$ ,  
 383 with much higher values than other methods.

#### 384 4.6 Computational expenses

385 The computational efficiency of different stacking methods varies significantly among different stacking methods but does not  
 386 change between Raw and One-bit NCFs. The compute times are estimated from a single core 3.6 GHz Intel Core i9 CPU.  
 387 We compare the compute time spent stacking subsets of the NCFs (with an increment of 5 NCFs) using the different stacking  
 388 methods (Fig. 16). The tf-PWS stacking method uses the most CPU time, while Linear stacking is the fastest method (Fig. 16).  
 389 Most of the time in tf-PWS is spent on computing the Stockwell transform on individual NCFs. While our implementation

**Table 1.** Our recommendations of stacking methods for major research applications using NCFs based on the evaluation metrics in Section 4. For methods denoted with (\*), see the appropriate sections for additional discussion.

<b>Applications</b>	<b>Evaluation metrics</b>	<b>Recommendations</b>
Velocity tomography (Section 5.1)	Signal-to-noise ratio (Section 4.1), surface wave dispersion (Section 4.2), and computational expenses (Section 4.6)	Raw: Robust One-bit: Linear, Robust, Selective, ACF, Cluster
Monitoring (Section 5.2)	Signal-to-noise ratio (Section 4.1), surface-wave dispersion (Section 4.2), convergence of short-term stacks to the long-term stack (Section 4.3), transient phase changes (Section 4.4), and computational expenses (Section 4.6)	Raw: Robust One-bit: Linear, Robust, Selective, tf-PWS(*)
Anelastic properties (Section 5.3)	Signal-to-noise ratio (Section 4.1), surface wave dispersion (Section 4.2), peak amplitudes of ballistic phases (Section 4.5), and computational expenses (Section 4.6)	Raw: Robust One-bit: Robust, Cluster

390 follows that of the original Stockwell transform, Baig et al. (2009) found a more efficient algorithm to compute the Stockwell  
 391 transform. The total time to perform tf-PWS is about six orders of magnitudes longer than that of the Linear stacking method.  
 392 For example, tf-PWS takes about 400 seconds to stack 300 NCFs, while Linear stacking takes 0.0005 seconds. The ACF  
 393 stacking method is the second most expensive method in terms of computing time, with about 4 seconds to stack 300 NCFs.  
 394 This is because the ACF method needs to compute the spectrum of each individual trace as well as the cross-spectrum in  
 395 moving windows. The Robust, Selective, and Cluster methods take about 0.02-0.4 seconds to stack 300 NCFs. The  $N^{th}$ -root  
 396 method is the second fastest method following the Linear stack. These methods all scale nearly linearly with the number of  
 397 NCFs to stack.

398 **5 CHOICE OF STACKING METHOD**

399 In this section, we discuss the choice of stacking methods for different applications that utilize NCFs. We focus on the following  
 400 major applications: 1) tomography of velocity structures, 2) monitoring of transient velocity changes, and 3) characterization  
 401 of anelastic properties. These three research applications extract different information from the NCFs: 1) seismic velocity  
 402 tomography using surface waves requires the dispersion information of the ballistic surface-wave phases, 2) seismic monitoring  
 403 requires dispersion and slight variations in phase information of the ballistic phases and/or the coda waves, and 3) the imaging  
 404 of seismic attenuation and prediction of strong ground motion relies on relative amplitudes of the ballistic phases. Although  
 405 the performance could vary with different datasets, we provide here the advantages and limitations of the stacking methods for  
 406 each application in Table 1.

## 407 **5.1 Stacking for tomography of velocity structures**

408 Ambient noise tomography typically requires extracting the surface wave dispersion information from the stack of all NCFs  
 409 for each station pair (e.g., Bensen et al. 2007). The fundamental mode surface waves are most commonly visible in the data,  
 410 though there are some studies using higher modes for imaging (e.g., Jiang and Marine A. Denolle 2022; G. Wu et al. 2020).  
 411 Our recommendation for seismic velocity tomography is based on the following metrics: signal-to-noise ratio (Section 4.1),  
 412 surface wave dispersion (Section 4.2), and computational expense (Section 4.6).

413 Based on our examples in Section 4.1, except for the OBS-OBS station pairs, the PWS method produces stacks with the  
 414 highest average SNRs, though with a large variance (see Figs 4-7 and S1-S3 in the supplement). The stacks using the  $N^{th}$ -root  
 415 method also have relatively high SNRs. Other stacking methods perform at a comparable level in terms of the SNRs of the  
 416 ballistic phases. The phase dispersion is better recovered using the Robust method than others for Raw NCFs over the entire  
 417 examined period of 1-15 s (Fig. 10b), especially in the period range of 4-9 s (Fig. 11b). When using One-bit NCFs, all but  
 418 the PWS and  $N^{th}$ -root methods perform well overall in the dispersion analysis (Figs 9, 10b, and 11b). However, the high  
 419 computational cost of the tf-PWS method makes it impractical for processing large data sets for tomographic imaging (Fig.  
 420 16). In summary, our recommendations for tomographic imaging are the Robust stacking for Raw NCFs and the Linear, Robust,  
 421 Selective, Cluster, and ACF methods for One-bit NCFs.

## 422 **5.2 Stacking for monitoring of transient velocity changes**

423 Seismic monitoring uses ballistic or coda wave interferometry to infer small changes in the subsurface from short-time stacks  
 424 of NCFs (e.g., F. Brenguier et al. 2008; Clements and Marine A Denolle 2018; Donaldson et al. 2019; Lobkis and Weaver  
 425 2003; Anne Obermann and Hillers 2019). A faster convergence of the NCF would lead to a higher temporal resolution in  
 426 seismic monitoring. The convergence is often hindered and thus limits the temporal resolution (Hadziioannou et al. 2011). It is  
 427 therefore important to find the optimal length of data that yields a reasonable convergence of the NCF stack. Meanwhile, time-  
 428 lapse imaging requires that the dispersion of surface waves remains stable through time (e.g., Bergamo et al. 2016). Therefore,  
 429 our recommendation for seismic monitoring using ambient noise interferometry is based on the following additional metrics  
 430 on top of those for tomography (Sections 4.1, 4.2, and 4.6): convergence of short-term stack to long-term stack (Section 4.3)  
 431 and transient phase changes (Section 4.4).

432 Regarding the convergence metric, all stacking methods show comparable performance (Fig. 12). The relatively large  
 433 variability in the rate of convergence using the Cluster stacking method may lead to artifacts in monitoring. The ACF method is  
 434 also relatively slow in converging to the long-term stack. It is worth noting again that the rate/time of convergence also depends  
 435 on the quality of specific datasets. The dispersion analyses are most stable using the Robust method for Raw NCFs. For One-bit  
 436 NCFs, all but the PWS and  $N^{th}$ -root methods are appropriate choices (Figs 8-11).

437 For transient phase changes, all but the PWS method perform comparably well for all of the four examined examples (Fig.

438 13). The tf-PWS method may be used to process the NCFs when long computational times are acceptable to the user, though  
439 its computational efficiency needs to be improved to process large datasets (Fig. 16), or when using Graphic Processing Units  
440 (Zeng and Thurber 2016). In summary, our recommendations for seismic monitoring are the Robust method for Raw NCFs  
441 and the Linear, Robust, and Selective methods for One-bit NCFs.

### 442 5.3 Stacking for characterization of anelastic properties

443 The relative amplitudes of NCFs have been used to characterize the seismic attenuation properties of the Earth's lithosphere  
444 (Prieto et al. 2009) and the ground motion patterns (e.g., Marine A Denolle et al. 2013, 2014; Viens et al. 2017). Therefore,  
445 in addition to the metrics pertinent to tomography (Sections 4.1, 4.2, and 4.6), our recommendation for the characterization of  
446 anelastic properties using NCFs also evaluates the stability of peak absolute amplitudes of ballistic phases (Section 4.5).

447 Mitchell (1995) measured attenuation from a compilation of global earthquake records from a variety of tectonic settings,  
448 including active margins, which are similar to the setting for the XZ linear array at the Cascadia margin. Because it is measured  
449 from earthquake surface-wave data, we argue that the attenuation parameter by Mitchell (1995) can serve as an independent  
450 benchmark in our evaluation. With this criterion, the Linear, Robust, Cluster, and ACF stacking methods are ranked as the top  
451 four among all of the methods for Raw NCFs (Fig. 14). However, the requirement of a reliable measurement of frequency-  
452 dependent attenuation and dispersion (Figs 8, 10a, and 11a) would narrow the choice down to Robust stacking for Raw NCFs.  
453 For One-bit NCFs, the Robust and Cluster stacking methods rank the best among all methods. Our recommendations for  
454 attenuation and ground motion studies, or any applications utilizing relative amplitudes, are the Robust method for Raw NCFs  
455 and the Robust and Cluster methods for One-bit NCFs.

## 456 6 CONCLUSIONS

457 NCFs are widely used in seismic velocity and attenuation imaging, monitoring, and ground motion analyses. The stacking of  
458 NCFs over longer time periods is needed for most applications utilizing NCFs to increase the strength of the coherent signals.  
459 There have been many temporal stacking methods developed to improve the stacking of NCFs. We compare eight temporal  
460 stacking methods, including Linear, Robust, Selective, Cluster, Phase-Weighted, time-frequency Phase-Weighted,  $N^{th}$ -root,  
461 and Adaptive Covariance Filter stacking methods, to investigate their performance to enhance the quality of the stacked NCF.  
462 We examine the performance of these methods with six metrics, including signal-to-noise ratios, surface-wave phase velocity  
463 dispersion, the convergence of short-term stacks to the long-term stack, wavespeed changes, peak amplitudes, and computa-  
464 tional expenses. Our analyses demonstrate that although all methods are able to retrieve clear ballistic phases, their spectral  
465 contents and peak amplitudes vary strongly across methods. Based on multiple evaluation metrics, we recommend the Robust  
466 method for all three categories of applications using Raw NCFs, including velocity tomography, monitoring, and attenuation  
467 studies. For tomography using One-bit NCFs, all methods except for Phase-Weighted, time-frequency phase-weighted, and

468  $N^{th}$ -root stacking methods are good choices. For monitoring using One-bit NCFs, the Linear, Robust, and Selective stack-  
469 ing methods are preferred choices, with the possibility of using time-frequency Phase-Weighted stacking for processing small  
470 datasets. For applications utilizing One-bit NCFs to extract relative amplitude information, both the Robust and Cluster stack-  
471 ing methods perform well. The findings in this study provide a practical guideline for choosing the appropriate stacking method  
472 for major applications utilizing NCFs. This work did not address the validity and effects of pre-processing techniques on our  
473 various use cases, but future work might address this (e.g., Fichtner et al. 2020). The open-source computer codes produced in  
474 this study can also be used for general time series stacking analyses.

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482 project. J. Bryan and K. Okubo contributed to methodology development. C. Jiang, M. Denolle, and T. Clements contributed  
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#### 484 **Data Availability**

485 The seismic waveforms were downloaded from IRIS Data Management Center and processed using *SeisGo* (<https://doi.org/10.5281/zenodo.5873724>), built upon *ObsPy* (Beyreuther et al. 2010) and *NoisePy* (Jiang and Marine A Denolle  
486 2020). The computer codes for the stacking methods are available as a standalone Python package, *StackMaster*, which is  
487 archived on Zenodo (<https://doi.org/10.5281/zenodo.5951013>) and is accessible on Python Package Index (<https://pypi.org/project/stackmaster>). All Python scripts and Jupyter notebooks used in the processing and visualizing of  
488 the data and stacking results are available at [https://github.com/xtyangpsp/Paper\\_OptimalStacking](https://github.com/xtyangpsp/Paper_OptimalStacking) and are archived  
489 on Zenodo (<https://doi.org/10.5281/zenodo.6363585>).

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